

# **Documents** de travail

## **«Forecasting Public Debt in the Euro Area Using Machine Learning: Decision Tools for Financial Markets»**

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## **Forecasting Public Debt in the Euro Area Using Machine Learning: Decision Tools for Financial Markets**

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#### Abstract

The situation of public finance in the eurozone remains a burning issue for certain Euro area countries. The financial markets, the main lenders of the Member States, are more attentive than ever to any factor which could affect the trajectory of public debt in the long term. The risk of bankruptcy of a Member State and a domino effect for the entire monetary union represents the ultimate risk weighing on the Eurozone. This paper aims to forecast the public debt, with a universal model, on a national level within the Euro area. We use a dataset that includes 566 independent variables (economic, financial, institutional, political and social) for 17 Euro area countries, spanning the period from 2000 to 2022 in annual frequency. The dataset is fed to four machine learning (ML) algorithms: Decision Trees, Random Forests, XGBoost and Support Vector Machines (SVM). We also employ the Elastic-Net Regression algorithm from the area of Econometrics. The best model is an XGBoost with an out-of-sample MAPE of 8.41%. Moreover, it outperforms the projections of European Commission and IMF. According to the VIM from XGBoost, the most influential variables are the past values of public debt, the male population in the ages 50-54, the regulatory quality, the control of corruption, the female employment to population ratio for the ages over 15 and the 10 year bond spread.

#### **JEL classification:** C53; H63; H68

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**Keywords:** Public Debt; Euro Area; Machine Learning; Forecasting;

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#### 1. Introduction

The situation of public finance in the eurozone remains a burning issue for certain Euro area countries. The financial markets, the main lenders of the Member States, are more attentive than ever to any factor which could affect the trajectory of public debt in the long term. Τhe risk of bankruptcy of a Member State and a domino effect for the entire monetary union represents the ultimate risk weighing on the Eurozone.

Although there have been fiscal discipline rules since the birth of the eurozone on January 1, 1999, the trend of public debt continues a worrying dynamic for certain countries. These rules, introduced by the Stability and Growth Pact (SGP, 1996), which have been reformed several times, must combine the sound management of national public finance in eurozone countries on the one hand, but also leave Member States sufficiently margin to achieve their fiscal policy on the other hand. This dual objective, particularly tricky to achieve, was reaffirmed by the reform adopted in 2024 and which comes into force on January 1, 2025.

This reform, which reaffirms the thresholds of 3% for the public deficit and 60% for the public debt, leaves enough room for maneuver for Member States, through other indicators, but contribute to maintain the distrust of the financial markets towards certain Member States. With financial markets now being the number one lender to Member States, the existence of these rules is not enough to guarantee fiscal seriousness. It is in this context that forecasts of the level of future public debt become crucial, potentially leading rating agencies to review their assessment of the quality of public assets held.

According to Estefania‐Flores et al. (2023), there is a significant positive forecast error in debt-to-GDP ratio projections in both advanced economies and emerging markets and developing economies. This error in public debt forecasts can have serious repercussions. High, unpredicted, levels of public debt often lead to higher interest rates on government bonds, increasing the cost of borrowing for governments. This in turn can limit their ability to finance future projects. It can also lead to low investor confidence as investors become increasingly concerned about the government's ability to repay its debt, which can lead to reduced foreign investment and economic instability. The government's fiscal flexibility may also be reduced, limiting its ability to implement expansionary fiscal policies during economic downturns.

Furthermore, the level of public debt can have a significant impact on financial stability. Inflationary pressures can also threaten currency stability, making the broader financial environment more volatile and unpredictable. Strained government finances produce excessive or unsustainable public debt, raising concerns of an eminent debt restructuring or even default. Financial market disruptions, greater borrowing costs, and increased systemic risks are just a few of the negative effects that increased public debt may have. An unpredicted, high public dept can cause cascading effects, such as in the 2009 debt crises that simultaneously hit many EU countries (Ireland, Spain, Portugal, Italy and more severely Greece). Furthermore, the efficiency of the transmission mechanisms of monetary policy might be impacted by the level of public debt. High levels of public debt can discourage private investment, raise the cost of borrowing for the private sector, and reduce the effectiveness of monetary policy actions meant to promote economic growth.

Numerous methods exist for forecasting public debt, but none of them consider institutional and political factors such as the electoral cycle, government communications or the composition of budget committees, for the Euro area. The aforementioned underscore the importance of public debt management for the stability of the Euro area.

The aim of this paper is to create a universal forecasting model that can accurately predict the level of public debt on a national level within the Euro area. The proposed arsenal to complete this goal includes 4 machine learning algorithms alongside with the elastic-net regression model, as benchmark, from the area of econometrics. In this setting, complex relationships and non-linear dynamics can be identified and captured, improving forecast accuracy and enhancing the ability for policy decision-making by utilizing advanced machine learning techniques and broad indicator sets such as, economic, financial, institutional, political and social indicators, as confirmed from Belly et al. (2023). Moreover, a critical strength of the paper is the identification and ranking, according to significance, of the most influential variables in terms of public debt forecasting and the use of the Partial Dependence Plots. These tools can contribute to governments and central banks to better formulate economic policy recommendations in favor of a better monitoring of national public debt evolution.

The paper is organized as follows: in Section 2 we will present the literature review, in Section 3 we will briefly discuss the methodologies and the dataset and in Section 4 we present our empirical results. Finally, Section 5 concludes the paper.

#### 2. Literature Review

The literature on the determinants of public debt is abundant. There are various factors behind the fluctuations of public debt (Knapková et al., 2019) for the Euro area (Belly et al., 2023). They vary from historical factors (Stasavage, 2003; Page, 2018; D'Erasmo & Mendoza, 2018), to political (Di Bartolomeo et al., 2018; Ono & Uchida, 2018), and economic factors (Poghosyan, 2017; Chen et al., 2017).

Dawood et al., (2017) created models demonstrating that it is critical to incorporate variables that can detect the likelihood of spillover from the banking sector and the foreign exchange market when building an effective Early Warning System (EWS) for sovereign debt crises. Fioramanti (2008), also developed an ANN-based early warning system that can, under certain conditions, outperform more consolidated methods.

The links between government and private sector debt, the financial sector, and the political mechanisms controlling the resolution of fiscal and economic challenges (Kalemli-Özcan et al., 2016) demonstrate the necessity of testing not only financial and economic indicators, but also political ones.

Many authors focused primarily on explaining how macroeconomic indicators affected public debt. Nonetheless, numerous research (e.g. Vuckovic & Basarac Sertic, 2013; Eusepi & Wagner, 2017) have confirmed that non-economic factors have also a significant impact on public debt; but, yet, they still did not take into account the interaction of macroeconomic and non-economic factors.

For example, Estefania‐Flores et al., (2023) discovered that the forecast error on debt is larger during periods of elections. This may be a result of governments choosing to follow different regimes, not pursuing fiscal consolidation in elections periods. All these non-economic factors can have a considerable influence on the way in which the financial markets assess a country's exposure to the risk of default, particularly the rating agencies for national public debt.

#### 3. Methodology and Dataset

In this section, we will briefly discuss the various methodologies and techniques used in this research. In section 3.1, after a short introduction to machine learning and AI, the various machine learning methodologies are presented, namely Support Vector Machines, Decision Trees, Random Forests and XGBoost. In section 3.2 the Elastic-Net regression methodology is explained, from the area of econometrics. Section 3.3 presents the problem of overfitting and the various techniques used to overcome it. The Recursive Feature Elimination (RFE) technique used to select the most informative variables, is analyzed in section 3.4 and finally, in section 3.5 we discuss the Variable Importance Measure (VIM) that ranks the variables based on their contribution to a model. Finally, 3.6 describes the variables used in this paper.

#### 3.1. Machine Learning methodologies

The field of machine learning was developed in the 1950s with the goal of equipping artificial intelligence (AI) systems with the "learning" component. The fundamental concept behind machine learning is that computers can learn from data, identify patterns, and make judgments with minimal human input. This capability is essential for automated analytical model construction, which is the foundation of machine learning.

Historically, large data sets have been essential for machine learning (Gogas and Papadimitriou, 2021). The availability of high-frequency data in the finance sector has led to the application of machine learning techniques to financial data. During the past few years, several techniques and methods have been used in smaller datasets as well, such as macroeconomic ones, providing results that outperform other econometric techniques (Sermpinis et al., 2014 inflation and unemployment, Gogas et al., 2022 unemployment, Sofianos et al., 2021 output gaps).

Support Vector Machines (SVM) are a well-known classification (Support Vector Classification – SVC) and regression (Support Vector Regression – SVR) technique, used particularly when non-linear patterns in the data or complex interactions are present. Due to its capacity to handle both linear and non-linear data, SVM can be utilized in a diverse range of real-world applications, including engineering, economics, finance, and more. In situations involving datasets that are contaminated by noise, outliers, or non-linear systems SVM are coupled with the so-called "kernel trick". This kernel function projects the original data from the data space to a higher-dimensional space, the feature space, where the dataset may be simpler to separate and more precisely classified or regressed (Cortes and Vapnik, 1995).

Decision Trees (DT) is a supervised machine learning technique, applied to regression and classification problems. These are top-down, node-and branch-based structures that resemble flowcharts (Figure 1). The data is divided recursively based on the most informative characteristic of the variables (Gogas et al., 2022). For regression tasks, the decision tree calculates predictions by averaging the target variable values of the training data points assigned to the same leaf node. Each node represents a criterion for splitting, whereas each branch represents an outcome. The top node, also known as the root node, represents the complete dataset, while the remaining nodes are referred to as decision nodes. The nodes that do not split any further, also known as leaves (or terminal nodes and leaf nodes), represent the final outcomes of the decision-making process (a value of public debt to GDP ratio in our case).



*Figure 1: Example of a decision tree (Sofianos et al., 2024).*

The benefits of decision trees are their ease of comprehension and good performance with training data. However, their main weakness is that they perform badly when handling out-of-sample data, thus, they have limited generalization ability. Their usual characteristics include low bias and high variance (overfit). One strategy to get around overfitting is to use ensembling techniques, where predictions from several different machine learning models are combined. The objective of ensemble learning is to combine the strengths and weaknesses of individual models to create an optimal model that performs better than any of the individual models. This procedure, which usually yields superior accuracy and robustness, entails combining the predictions from each algorithm to create a final forecast. Bagging (Breiman, 1996) and boosting (Freund and Schapire, 1997) are the two primary ensemble techniques. In bagging, each data point can be utilized to train a new decision tree, since each observation is sampled independently. Furthermore, each observation is equally important. In contrast, boosting creates decision trees sequentially, varying the weight or importance of each observation at each iteration. This allows for greater weight to be given to misclassified or hard-to-predict data points as the algorithm attempts to improve its overall performance and correct its faults (Figure 2).

In bagging, the average score of the model is obtained through the parallel and independent training of weak learners. In regression tasks, predictions are made using the average value of the target variable from the data points of each leaf node. The random forest algorithm is the most frequently used method of bagging (Breiman, 2001), where a distinct subsample of the original dataset is selected at random with replacement for every tree (bootstrapping).

Another ensemble technique is the XGBoost (eXtreme Gradient Boosting; Chen & Guestrin, 2016). In contrast to random forest, it creates an ensemble of decision trees in a stepwise manner, with each new tree attempting to improve on the mistakes made by the one before it (boosting). Gradient boosting is a framework that enables the algorithm to grow each tree with the goal of minimizing a given objective function. This function is typically a combination of a regularization term and a loss function. XGBoost is regarded as a cutting-edge algorithm that improves the precision and accuracy of the outcomes. This methodology's effectiveness has been generally acknowledged in a number of machine learning and data mining challenges (Chen and Guestrin, 2016).



*Figure 2: An illustration of the boosting and bagging processes. In that example, the size of each observation corresponds to its importance on each tree.*

#### 3.2. Elastic Net Regression

Elastic Net regression is a hybrid model that combines the strengths of two popular regularization techniques: Lasso (L1) and Ridge (L2) regression. It addresses the limitations of each method by introducing a penalty term that is a linear combination of the L1 and L2 regularization of the coefficient vector. This allows Elastic Net to select variables and handle multicollinearity more effectively than Lasso, while still encouraging sparsity in the solution like Lasso. The penalty terms L1 and L2 and their trade-off, are controlled by parameters tuned with cross validation, offering flexibility in model complexity and feature selection. By striking a balance between variable selection and regularization, Elastic Net regression provides a powerful tool for handling high-dimensional data with correlated predictors, commonly encountered in many research contexts.

#### 3.3. Overfit

Overfitting occurs when a trained model is well-fitted to the training set but fails when applied to new and unknown data, meaning the model has low bias and high variance (Figure 3). This is also known as "low generalization ability".



*Figure 3: A visual representation of underfit, overfit and optimal fit in regression (Solanes & Radua, 2022). In underfitting the model is too simple and not able to identify the underlying pattern of the data. In overfitting, the model is too complex and fits the training data too well; thus, it is not able to identify the underlying pattern. When a model fits the data well and identifies the underlying pattern we have optimal fitting.* 



*Figure 4: The Bias-Variance trade-off. The goal is to train a model that does not overfit (high variance and low bias) or underfit (high bias and low variance). The optimal model should minimize the prediction error achieving a balance between bias and variance.* 

To test the generalization ability of our models, the dataset was divided into two subsamples: a) the training sample (in-sample), on which the algorithms were trained, and b) the test sample (out-of-sample), where the generalization ability of the trained models was tested using "unseen" data, in order to assess the models' capacity for generalization (Figure 4). To prevent overfitting, cross-validation is employed during the training phase to identify the optimal hyperparameters for the models. The insample portion of the dataset is divided into k equal-sized subsets (folds) for crossvalidation. For each distinct set of hyperparameters that is tested, the training/testing procedure is repeated k times. The testing of the model is conducted using a different fold for each iteration, whereas the training of the model is conducted using the remaining k-1 folds. The overall performance of each set of examined hyperparameters is calculated as the average performance over all test k folds (Figure 5). In our experiments, we employed a 5-fold configuration.



*Figure 5: The illustration depicts a 3-fold cross-validation procedure. Each fold represents a test sample for each combination of hyperparameters under consideration. The remaining folds are utilized to train the model. To evaluate the model (in-sample) and test it on the out-of-sample portion of the dataset, that contains data that the model has not used during training, the average performance for each combination of parameters over the test kfolds is utilized (Gogas et al., 2019).*

A variety of forecasting metrics can be calculated to assess and contrast the forecasting efficacy of our models. In this paper, we utilize the Mean Absolute Percentage Error (MAPE). This metric is the most prevalent in the relevant literature due to its simplicity and interpretability, and it is defined as:

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MAPE = \frac{1}{n} \sum_{i=1}^{n} \left| \frac{y_i - \hat{y}_i}{y_i} \right| \times 100
$$
 (1)

where  $y_i$  and  $\hat{y}_i$  are the target variable's actual and predicted values, respectively, and n is the sample size. The average mean absolute difference between the predicted and actual values is measured in percentage terms by the MAPE metric.

#### 3.4. Recursive Feature Elimination

To identify the most relevant features (variables) for the prediction problem, we employed a Recursive Feature Elimination (RFE) technique. RFE starts by fitting the model with all the features present and obtaining the importance of each feature. This can be done through a specific attribute or callable of the model (such as coefficients or feature importance). Then, the least important features are pruned from the current set of features. This process is repeated recursively on the pruned set until the desired number of features to select is finally reached. In our case, we used the Random Forest algorithm as an estimator. The Random forest ranks features based on their Gini significance, prioritizing those who are crucial for the model's performance (Guyon, Weston et al., 2002).

#### 3.5. Variable Importance Measure

The Variable Importance Measure (VIM), ranks variables based on their contribution to the model and it can be computed in tree-based models to help us break the algorithm's black box nature. The VIM calculates the impact of each attribute split point on performance, weighted by the number of observations each node handles. VIMs are then averaged across all decision trees in the model. A higher value for this metric indicates that one feature is more important for generating a prediction than another.

#### 3.6. The Dataset

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The dataset consists of 17 Euro area countries<sup>3</sup> and 566 economic, financial, political, institutional and social variables (Table 3 at appendix) at an annual frequency spanning the period from 2000 to 2022 (panel data), for a total of 340 observations. A quick summary of the data can be found in Table 1. Three main categories of data are collected; a) economic and financial data, to cover macroeconomic features of each country, b) political and institutional variables, to consider institutional and political system features and c) social variables to integrate social demo features for each country. The economic and financial data mainly extracted from different sources

<sup>&</sup>lt;sup>3</sup> From the 20 Euro Area countries, we excluded Cyprus, Malta and Croatia due to data availability restrictions. The economic weight of these 3 countries represents only 0.9% of the GDP of the euro zone (2023 GDP data).

(*Eurostat*, *the OECD* and *the World Bank*), cover traditional macroeconomic indicators (GDP, employment, inflation, international trade, international capital flows, activity by sector, public expenditure, public revenues, public deficit, public debt, 3-month short-term interest rate, 10-year bond yields, 10 year bond spread, …). Political and institutional data also come from different sources (*Worldwide Governance Indicators of the World Bank*, *the V-Dem Dataset*, *the International Country Risk Guide-Researcher Dataset* and the *International Institute for Democracy and Electoral Assistance Database)* and makes it possible to take into account the country's mode of government, the characteristics of the institutions (quality, control, etc.), the electoral system, the voting process, the result elections, respect for the rules of law, ... Social data from *the World Bank* and *the Standardized World Income Inequality Database* cover the socio-demographic characteristics of each country. Moreover, we added up to 3 lags for every variable, increasing the total number of variables to 1694. The dataset was split in two parts, the in-sample data (used for training the models) that includes 80% of the data, or 272 observations, and the out-of-sample (OOS) data, that includes 20% of the data, or 68 observations, to test the generalization ability of our models. According to this split, the OOS part consists of the last 4 years of the dataset (2019- 2022). Some missing values (less than 3%) were filled with the mean value of each variable per country.



*Table 1: Description of the data and their sources.* 



#### 4. Empirical Results

#### 4.1. Forecasting models results

For the empirical part, we first identified the 25 most informative variables, then we used them to train the models. The best models were identified through a cross validation process. Finally, we used the best model to interpret the results, break the socalled "black-box" of machine learning. This can help us to give a better economic interpretation to the results.

In the first step we use the RFE methodology to select the 25 most informative variables and then use them to train the machine learning algorithms. The 25 variables is a number that strikes a balance between model complexity and performance, reducing overfitting and computational time. We trained models with more than 25 variables but the results provided higher MAPE scores. The selected variables are presented in Table

#### 2.



*Table 2: The 25 selected variables based on the RFE technique.*



In the next step, we used a 5-fold cross-validation scheme for the hyperparameters optimization of each model. Moreover, the SVM models were coupled with the linear, the RBF and the polynomial kernels. The MAPE scores for the best trained models are presented in Figure 6.



*Figure 6: MAPE scores for the best models of each algorithm in-sample and out-of-sample (OOS).* 

According to the results, the best model, in terms of in-sample performance, is an XGBoost model, with a MAPE of 6.83% and the second-best model is an SVM model coupled with the linear kernel reaching an in-sample MAPE of 7.98%. In terms of OOS performance, the best model is also the XGBoost reaching an OOS MAPE of 8.41% and the second-best performing is the SVM coupled with the linear kernel with a MAPE of 8.43%. The decision tree model has the worst performance in-sample, while the SVM coupled with the polynomial kernel has the highest MAPE for the OOS part of the dataset. Overall, the best model is the XGBoost (Figure 7). The countries with the highest public debt to GDP ratio (in circles) are Greece and Italy and the forecasts seem to be more inaccurate for the countries with high public debt. This complies with the findings of Bachleitner & Prammer (2024). According to their results the error in the debt forecast is more pronounced for high debt countries than for low debt countries. For each model, there is very little difference between the out-of-sample MAPE and the in-sample MAPE. This suggests that these models have comparable bias and variance, or in other words, they do not overfit and have a good generalization ability.



*Figure 7: Scatter Plot of the True vs Predicted Values for the out-of-sample part of the dataset public debt to GDP ratio with the optimal XGBoost model. The countries with the highest public debt to GDP ratio (in circles) are Greece and Italy.* 

To further validate the performance of the XGBoost model, we calculated the Mean Absolute Percentage Error (MAPE) for the years  $2021$  and  $2022<sup>4</sup>$ . This evaluation compared the predictions of the XGBoost model with the forecasts of two prominent institutions: the European Commission's European Economic Forecast (Spring 2021) and the International Monetary Fund's World Economic Outlook (April 2021: Managing Divergent Recoveries). The MAPE for XGBoost was calculated at 6.49%, significantly lower than the 10.66% for the European Commission's forecasts and the 12.06% for the IMF's forecasts. These results highlight the superior accuracy of the XGBoost model in predicting economic outcomes for these years, demonstrating its robustness and reliability when compared to established forecasting methods from leading global institutions. This performance demonstrates the potential of machine learning models such as XGBoost to improve the accuracy of economic forecasts, even in the face of uncertain and rapidly changing conditions.

#### 4.2. Economic interpretation of the results

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In this research, we used the XGBoost's (Extreme Gradient Boosting) VIM (Variable Importance Measure) since this algorithm provided the best results amongst the tree-

<sup>4</sup> The comparison took place only in the years 2021 and 2022 (the most recent ones in our dataset) due to data availability.

based methodologies. The most well-known VIM of XGBoost is the gain, which refers to the improvement in accuracy achieved by the addition of a particular feature to a decision tree. Specifically, it measures the utility of each feature in the construction of the boosted trees during training. The gain for a feature is calculated by comparing the loss reduction achieved when splitting a tree node based on that feature against the distribution of instances reaching that node. The idea is that before adding a new split on a feature X to the branch, there may have been some elements that were incorrectly classified. After adding the split on this feature, there are two new branches, and each of these branches is more accurate. The gain value essentially indicates the extent to which a feature contributes to enhancing the model's performance by facilitating the splitting of data. A higher gain value signifies that a feature is more pivotal for decisionmaking within the trees, and XGBoost frequently employs this metric to ascertain feature importance and to determine the optimal splits during the tree-building process. The VIM for the 10 most important variables<sup>5</sup>, according to the XGBoost gain measure, is presented in Figure 8.



*Figure 8: The 10 most important variables calculated with the Variable Importance Measure (VIM) for the best XGBoost model. When there is no lag specified the variable is in lag 1.* 

The past values of public debt (to GDP ratio) for lags 1 and 2 are the most influential, with the highest VIM scores. The third most important variable is the male population in the ages 50-54 lag 3.

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 $5$  The results for all the variables can be found in Table 4 in the appendix.

The fourth most informative variable is the regulatory quality (Kaufmann et al., 2011). According to the World Bank database "*Regulatory Quality captures perceptions of the ability of the government to formulate and implement sound policies and regulations that permit and promote private sector development*". The Regulatory Quality Index consists of the key steps of the law - making process and includes 48 individual indicators, focusing on two main aspects: the form (expression / clarity) and content (substance / scope) of a legal act. The overall score (ranking) is given by an aggregating formula to a 0 to 100 scale. The aim of this toolkit is to identify the main weaknesses of a regulatory environment and to operate as an indicator for comparative analysis across different countries as underlined by Saravakos et al. (2022) . In Figure 9, we can observe the regulatory quality for 4 economies of the Euro area, Germany (DE), Greece, (EL), France (FR) and Italy (IT). We can observe that the two countries with the highest public debt have also a very low rank in the regulatory quality. Thus, the policies and regulations that promote private sector development is crucial for the public debt.



*Figure 9: Regulatory Quality, Percentile Rank for 4 economies of the Euro area, Germany (DE), Greece, (EL), France (FR) and Italy (IT).*

The fifth most important variable is the control of corruption (Kaufmann et al., 2011). According to the World Bank database "*Control of Corruption captures perceptions of the extent to which public power is exercised for private gain, including both petty and grand forms of corruption, as well as "capture" of the state by elites and private interests*". The measurement is based on a compilation of data from various sources. These sources include opinion surveys and assessments carried out by international

institutions, NGOs, think tanks and risk rating agencies. These sources include Transparency International, the World Economic Forum, and local organizations. The World Bank aggregates data from these multiple sources using a statistical methodology called the Unobserved Components Model (UCM). The "Control of Corruption" score (ranking) is given by an aggregating formula to a 0 to 100 scale. In Figure 10 we can observe the control of corruption for 4 economies of the Euro area, Germany (DE), Greece, (EL), France (FR) and Italy (IT). We can observe that the two countries with the highest public debt have also a very low rank in the control of corruption.



*Figure 10: Control of Corruption, Percentile Rank for 4 economies of the Euro area, Germany (DE), Greece, (EL), France (FR) and Italy (IT).*

There are other studies that highlight the influence of corruption on public debt, but not for the Euro area. Cooray et al., (2017) found that corruption has a highly statistically significant impact on public debt for 126 countries tested for the period from 1996 to 2012. In addition, Del Monte & Pennacchio, (2020) used a panel of OECD countries for the period from 1995 to 2015 and provided evidence that corruption increases public debt. Also, Liu et al., (2017), for the same time period, examined the relationship between corruption and public debt for 120 countries. They found that higher levels of corruption led to higher levels of public debt. However, a very interesting finding is that the relationship between corruption and debt was non-linear, as in our methodology. Similar results were also found for the United States (Apergis & Apergis, 2019).

The 6th most important variable is the female employment to population ratio for the ages over 15. In the  $7<sup>th</sup>$  place is the 10 Year bond spread lag 1. The rest of the variables are if parties or candidates receive either free or publicly financed access to national broadcast media industry during national elections (election free campaign media lag 2), the industry (including construction), value added and if during, before and after elections where any violence related to the conduct of the election and the campaigns (electoral violence).

To further explore the relationships between the public debt and the 10 year bond spread, we employed the Partial Dependence Plots (PDP) methodology. A Partial Dependence Plot reveals the marginal effect of the features on the predicted outcome of a machine learning model (Friedman, 2001). A Partial Dependence Plot, shows how the predicted outcome (target variable) changes as a specific feature (independent variable) varies while keeping all other features constant. It provides insights into the relationship between a single feature and the model's predictions. It is a useful tool as it enhances the interpretability of the trained machine learning model in several ways providing empirical information. The reason we chose spread to further analyze is because it can be directly controlled from the governments to alter the public debt.



*Figure 11: Partial Dependence Plot for spread.*

In Figure 11, we present the PDP of the spread and the target variable. We can observe that a) when the spread increases the public debt increases as well b) when the spread is below zero the public debt is very low and increases substantially until the spread reaches a value of 0.5 and c) when the spread is more than 1.8 the public debt increases but in a very low rate.

#### 5. Conclusion

Unpredicted high levels of public debt can have serious economic, financial and social consequences, including higher borrowing costs, reduced investor confidence and fiscal constraints that limit government spending on essential projects. It can also trigger inflationary pressures, financial instability and higher taxes, while reducing public services and employment opportunities, all of which contribute to increased uncertainty and anxiety among citizens.

In this study we attempt to forecast the public debt of Euro area countries with a universal model. We use 4 machine learning methodologies, SVM, decision trees, random forest, XGBoost and an elastic net regression from the area of econometrics. Moreover, we use a broad dataset with 566 economic, financial, political, institutional and social variables, ranging from 2000 to 2022. To the best of our knowledge, this is the first time the public debt of Euro area countries is forecasted with machine learning methodologies and such broad dataset.

The optimal XGBoost model outperformed the competition reaching an out-of-sample MAPE of 8.41% and an in-sample MAPE of 6.83%. In addition, we tested the performance of the XGBoost model by comparing its predictions with those of the European Commission and the IMF, for the years 2021 and 2022. The XGBoost model achieved a MAPE of 6.49%, outperforming the Commission's 10.66% and the IMF's 12.06%. This result highlights the accuracy of the model and the potential of machine learning models such as XGBoost to improve the accuracy of macroeconomic forecasting.

According to the XGBoost VIM, the past values of public debt to GDP ratio are the most influential. The third most important variable is the male population in the ages 50-54 lag 3 followed by the regulatory quality and the control of corruption which capture the perception by economic agents of two major characteristics for the management of public finance: the quality of regulation and the control of corruption, i.e. "*perceptions of the ability of the government to formulate and implement sound policies and regulations that permit and promote private sector development"* and *"perceptions of the extent to which public power is exercised for private gain, including both petty and grand forms of corruption, as well as "capture" of the state by elites and private interests".* Among the most influential variables, the 10 year bond spread also plays an important role.

In other words, while standard macroeconomic indicators such as past values of the public debt ratio, the working age population or even 10 year bond spread are among the most influential variables, the public finance management by government also seems to play a crucial role. Countries with the highest public debt have also a very low rank in the regulatory quality. In the same way, countries with the highest public debt have also a very low rank in the control of corruption. It is for this reason that rating agencies must also monitor the way in which economic agents perceive the management of public finance by governments.

Thus, these precise forecasts provide substantial contributions to the financial sector. By identifying macroeconomic variables (the historical values of the public debt to GDP ratio, employment rate, government spread), but also the control of corruption and the regulatory quality as key predictors, financial institutions can more effectively assess the creditworthiness and risk profiles of Euro area countries. This enables more informed lending and investment decisions, potentially lowering the cost of capital. Furthermore, understanding the impact of these indicators on public debt levels allows for better predictions of fiscal sustainability, aiding investors in portfolio diversification and risk management. For policymakers, these insights support the formulation of much more attention to public finance management (captured here by regulatory quality and control of corruption), thereby enhancing economic and financial stability of the Eurozone and thus increase investor confidence.

For future research, extending the forecasting horizon beyond one year could offer valuable insights, enabling a more comprehensive understanding of long-term trends and potential outcomes. Such an approach may also improve the robustness and applicability of the forecasting model across diverse time frames.

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### Appendix

*Table 3: List of all variables used with their source and short description.*





































*Table 4: Variable Importance Measure results, using gain, for all 25 variables for the optimal XGBoost model.*