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TECHNICAL CHANGE BIASED TOWARD THE TRADED SECTOR AND LABOR MARKET FRICTIONS*

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Abstract

This paper develops a tractable version of a two-sector open economy model with search frictions in order to account for the relative wage and the relative price effects of higher productivity growth in tradables relative to non tradables. Using a panel of eighteen OECD countries over the period 1970-2007, our estimates reveal that a 1 percentage point increase in the productivity differential between tradables and non tradables lowers the non traded wage relative to the traded wage (relative wage) by 0.22% and appreciates the relative price of non tradables by 0.64%. While the decline in the relative wage reveals the presence of mobility costs preventing wage equalization across sectors, the relative wage responses to a productivity differential display a large dispersion across countries, thus suggesting that labor market frictions vary substantially across OECD economies. Using a set of indicators capturing the heterogeneity of labor market frictions across economies, we find that the relative wage significantly declines more in countries where labor market regulation is more pronounced. These empirical findings can be rationalized in a two-sector open economy model with search in the labor market as long as we allow for an endogenous sectoral labor force participation decision. In line with our estimates, our quantitative analysis reveals that the relative wage falls more in countries where unemployment benefits are more generous, firing cost is high, the worker bargaining power is large. When calibrating the model to each OECD economy, our numerical results reveal that the model predicts the relative wage response fairly well, and to a lesser extent the relative price response.

Keywords: Productivity growth; Sectoral wages; Relative price of non tradables; Search theory; Labor market institutions
JEL Classification: E24; F16; F41; F43; J65.

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1 Introduction

Over the last fourty years, both advanced and emerging economies have experienced structural shocks driven by globalization and differential rates of technological progress. According to the conventional wisdom, trade liberalization and technological change biased toward the traded sector should be followed by intersectoral labor shifts. Labor reallocation would in turn gradually arbitrage away spatial and sectoral differences in wages. However, empirical findings cast doubt over the assumption of perfect labor mobility. Wacziarg and Wallack [2004] find that trade liberalization leads to little or no inter-industry worker reallocation, thus suggesting large switching costs across sectors. Only recently have researchers begun measuring mobility costs across sectors or regions. Adopting a structural empirical approach, Artuç et al. [2010], Dix-Carneiro [2014], Dix-Carneiro and Kovak [2015], Lee and Wolpin [2006] find substantial barriers of mobility and that wages are not equalized across sectors or regions neither in the short run nor in the long run. Despite the significance of limited labor mobility across sectors, only very few attempts have been made to investigate the consequences of higher productivity of tradables relative to non tradables when workers experience switching costs.[1] By assuming that the labor markets are subject to search frictions, this paper analyzes the long-run adjustment in the non traded wage relative to the traded wage (relative wage hereafter) following technological change biased toward the traded sector and proposes to disentangle quantitatively the implications of labor market institutions.

The literature analyzing the effects of technological biased toward the traded sector mostly focuses on the long-run movements in the relative price of non tradables.[2] The reason is that the standard theory attributed to Balassa [1964] and Samuelson [1964] (BS hereafter) imposes the assumption of perfect mobility of labor across sectors so that the sectoral wages must equalize. However, our evidence for 18 OECD countries shows that higher productivity in tradables relative to non tradables tends to lower the relative wage

[1] To our knowledge, only two papers investigate the implications of higher productivity of tradables relative to non tradables by relaxing the assumption of perfect labor mobility. Lane and Milesi-Ferretti [2004] develop an open economy setup where the output of tradable good is an endowment which implies that labor is not mobile between the two sectors. In line with their model's predictions, the authors find empirically that in the long run, improving net external positions are associated with appreciating real exchange rates. Cardi and Restout [2015] show that the neoclassical open economy model with tradables and non tradables can account for the relative price response to higher productivity of tradables relative to non tradables found in the data as long as there is a difficulty in reallocating labor across sectors. Their paper differs from this one in two important dimensions. First, in the present contribution, we estimate empirically the impact of labor market institutions' indicators such as firing cost, the generosity of the unemployment benefit system or the worker bargaining power in the determination of the relative wage response to higher productivity of tradables relative to non tradables. Second, the authors produce imperfect mobility of labor by introducing limited substitutability in hours worked along the lines of Horvath [2000]. While this approach allows the authors to estimate precisely the parameter capturing the extent of labor mobility for each country of their sample, it has the disadvantage to prevent the analysis of the role of labor market institutions by abstracting from search frictions.

[2] De Gregorio et al. [1994], Canzoneri et al. [1999], Kakkar [2003], Lane and Milesi-Ferretti [2002] document a strong and positive relationship between the relative price of non tradables and differential rates of technological progress.

of non tradables over the period 1970-2007 in all economies of our sample, and more so in countries where the labor market regulation is more pronounced. We show that these findings can be rationalized in a two sector open economy model with search in the labor markets as long as we allow for an endogenous sectoral labor force participation decision.

To set the stage of the quantitative analysis, we first assess empirically the effects of technological change biased toward the traded sector on both the relative wage and the relative price of non tradables.[3] Because all variables are non stationary, we have recourse to cointegration methods. Our estimates reveal that a 1 percentage point increase in the productivity of tradables relative to non tradables lowers the relative wage by 0.22% and appreciates the relative price by 0.64% for the whole sample. The long-run decline in the relative wage suggests the presence of labor market frictions preventing wage equalization across sectors. Moreover, when assessing the effects of technological change biased toward the traded sector at the country level, we find that estimates display a large dispersion across countries, thus suggesting a substantial heterogeneity of labor mobility costs between the economies of our sample. Using a set of indicators to capture the extent of labor market frictions, we find that the decline in the relative wage is more pronounced in countries where the unemployment benefit scheme is more generous, legal protection against dismissals is stricter, or the worker bargaining power measured by the bargaining coverage is larger.

In order to account for our evidence, we put forward a variant of the two-sector open economy model with tradables and non tradables and search in the labor market along with an endogenous labor force participation decision in the lines of Shi and Wen [1999].[4] Like Alvarez and Shimer [2011], imperfect mobility across sectors arises because searching for a job in one sector is a time-consuming and thus a costly activity. In our model, the elasticity of labor supply at the extensive margin plays a pivotal role because it measures the extent of workers' moving costs: the smaller the elasticity of labor supply, the larger the switching cost, and thus the lower the degree of labor mobility across sectors.[5] Conversely, when we let the elasticity of labor supply tend toward infinity, the case of perfect labor mobility is obtained in the long-run, as assumed by the standard BS model, so that the relative wage remains (almost) unaffected by technological change biased toward the traded sector, in

[3] We find it important to estimate the relative price effect of differential rates of technological progress in two respects. First, since our paper is closely related to the BS literature, such an analysis highlights the deviations from the standard predictions of the BS effect. Second, the relative price and relative wage are intertwined into each other as will be clearer when detailing the transmission mechanism.

[4] Our framework also builds upon Merz [1995], Andolfatto [1996]. In contrast to Merz [1995], Andolfatto [1996], Shi and Wen [1999] who construct dynamic general equilibrium models of a closed economy with labor markets characterized by search frictions, we abstract from physical capital accumulation and consider an open economy setup with tradables and non tradables. While our model is also closely related to Heijdra and Ligthart [2009], we construct a two-sector open economy model with an endogenous sectoral labor force participation decision which allows us to emphasize the role of imperfect mobility of labor.

[5] We consider an endogenous sectoral labor force participation decision by assuming that representative household members experience disutility from working and searching efforts in each sector. Relocating hours worked from one sector to another is costly as the representative household must incur a searching cost for a job in this sector; such utility loss may capture sector-specific human capital and/or geographical mobility costs. Thus, in contrast to Matsuyama [1992] who assumes the irreversibility of the career decision, workers can move between sectors, at some cost though.

contradiction with our empirical findings. While letting the elasticity of labor supply take intermediate values implies that the relative wage may fall, the size of its decline depends on the degree of labor market regulation as well. More specifically, because hiring is also a costly activity which depends on labor market institutions, firms may be reluctant to raise substantially the number of job vacancies. Intuitively, our model predicts that firms' hiring in the traded sector is more elastic to technological change in countries where the unemployment benefit replacement rate is higher or the worker bargaining power is larger. Consequently, the rise in the traded wage is more pronounced which results in a larger decline in the relative wage of non tradables. Our model also predicts that firms' hiring in the non traded sector is less elastic to productivity growth in countries where the firing cost is larger. Hence, the relative wage falls more because the non traded wage rises by a smaller amount following productivity gains.

To shed light on key factors determining the long-run adjustment in the relative wage and the relative price, we analytically break down the responses into two components: i) a labor market frictions channel (keeping net exports fixed), and ii) a labor accumulation channel triggered by the long-run adjustment in net exports. First, the model can account for the decline in the relative wage through the labor market frictions channel only if the elasticity of substitution for consumption between traded and non traded goods is larger than one. Intuitively, technological change biased toward the traded sector stimulates hiring in the traded sector since only in this case does expenditure on tradables rise relative to expenditure on non tradables. Conversely, an elasticity smaller than one raises the relative wage by increasing the share of non tradables in expenditure which has an expansionary effect on hirings in the non traded sector. Second, while the model cannot produce the decline in the relative wage found in the data through the labor market frictions channel when the elasticity of substitution is smaller than one, technological change biased toward the traded sector also exerts a negative impact on the relative wage by raising net exports in the long-run. The reason is that higher productivity induces firms to hire more. Because recruiting workers is a costly activity, the open economy runs a current account deficit to finance labor accumulation. While the open economy decumulates traded bonds along the transitional path, the trade balance must improve in the long-run for the intertemporal solvency condition to hold. Hence, through the labor accumulation channel, the demand for tradables always rises which induces traded firms to hire more, thus driving down the relative wage.

While the relative wage response is ambiguous when the elasticity of substitution between traded and non traded goods is smaller than one, our quantitative analysis reveals that, for our baseline calibration, the labor accumulation effect always more than offsets the labor market frictions effect so that the relative wage falls. Moreover, in line with our evidence, our sensitivity analysis reveals that the relative wage falls more in countries where the labor market is more regulated. More specifically, we find numerically that raising the unemployment benefit replacement rate or the worker bargaining power leads to a larger decline in the relative wage because in this case, net exports rise by a larger amount. Intuitively, such economies are characterized by a low labor market tightness which makes hiring more profitable following higher productivity. As a result, recruiting expenditure rise more, thus resulting in a larger current account deficit which must be matched in the long-run by a greater improvement in the balance of trade. Hence, the labor accumulation effect exerts a larger negative impact on the relative wage. The sensitivity analysis also reveals that the decline in the relative wage is more pronounced when increasing the firing cost because the non traded wage increases less. Intuitively, as the positive wealth effect lowers aggregate labor supply while non traded firms experience relatively low productivity gains, non traded establishments are shrinking; thus, non traded firms must pay a firing cost on reducing employment which in turn moderates the positive effect of higher productivity on hiring. While the labor accumulation effect is almost unchanged, the labor market frictions effect exerts a smaller positive impact on the non traded wage in countries where legal protection against dismissals is stricter so that the relative wage falls more following technological change biased toward the traded sector.

The final exercise we perform is to compare the responses of the relative wage and relative price for each OECD economy in our sample to our empirical estimates. To do so, we allow for two sets of parameters to vary across countries: the elasticity of substitution in consumption between tradables and non tradables and the labor market parameters that we estimate for each economy. It is found that the model predicts the relative wage decline pretty well and to a lesser extent the rise in the relative price.

Our paper is at the cross-roads of two strands of the literature investigating the adjustment of open economies to structural shocks. First, it is closely related to the BS theory which has been renewed recently, notably by Bergin et al. [2006], Ghironi and Melitz [2005]. These two papers relax the assumption of perfectly competitive goods market and show that heterogenous productivity among firms and/or entry and exit of firms amplifies the effect of higher productivity in tradables relative to non tradables on domestic prices.[6] In our paper, we consider imperfectly competitive labor markets and show that labor market frictions moderate the appreciation in the relative price of non tradables triggered by a productivity differential between tradables and non tradables by reducing the relative wage of non tradables. In this respect, our study can be viewed as complementary to the small but growing literature which investigates the quantitative implications of barriers of

[6]Ghironi and Melitz [2005] show that higher traded productivity triggers firm entry which stimulates labor demand, raises wages and thus increases traded prices, which amplifies the rise in domestic prices commonly induced by the appreciation in the price of non traded goods. According to Bergin et al. [2006], technological change biased toward the traded sector induces the least productive firms in the traded sector to cease exporting; as a result, the share of non tradables in the economy increases, thus amplifying the effect of the appreciation in the relative price of non tradables on domestic prices.

mobility following trade shocks, e.g., Kambourov [2009] and Cosar [2013].[7] We contribute to this literature by quantifying the impact of labor market institutions on sectoral wages following technological change biased toward the traded sector.

The remainder of the paper is organized as follows. In section 2, we provide evidence on the relative wage and relative price effects of higher productivity in tradables relative to non tradables in the long run. In section 3, we develop an open economy version of the two-sector model with both imperfect mobility of labor arising from searching efforts and unemployment arising from matching frictions in both sectors, and characterize the long-run equilibrium graphically. Section 4 analytically breaks down the relative price and relative wage responses to a productivity differential between tradables and non tradables. In section 5, we discuss numerical results and investigate the ability of the model to replicate our empirical findings for each OECD economy. Section 6 summarizes our main results and concludes.

2 Empirical evidence

In this section, we revisit empirically the effects of technological change biased toward the traded sector by focusing on the relative wage and the relative price responses. We denote the level of the variable in upper case, the logarithm in lower case, and the percentage deviation from its initial steady-state by a hat.[8]

2.1 Revisiting the Relative Wage and Relative Price Effects of Technological Change Biased toward the Traded Sector

To set the stage for the empirical analysis, we revisit the theory that Balassa [1964] and Samuelson [1964] developed fifty years ago to explain the appreciation of the relative price of non tradables following higher productivity growth in tradables relative to non tradables. While the original BS framework assumes perfectly competitive labor markets, we relax this assumption which allows us to highlight the implications of labor market frictions.

As it is commonly assumed, the country is small in terms of both world goods and capital markets, and thus faces an exogenous international price for the traded good $P^{T,\star}$. We assume that the law of one price holds so that $P^T = P^{T,\star}$, and normalize the price of the traded good on world good markets to unity. Each sector produces Y^j by using labor, L^j, according to a linearly homogenous function:

$$Y^j = A^j L^j, \tag{1}$$

[7] Developing and calibrating general equilibrium sectoral models of a small open economy with sector specific human capital, both Kambourov [2009] and Cosar [2013] find that human capital is a substantial barrier mobility along with firing costs for the former and search frictions for the latter.

[8] Summary statistics of the variables used in the empirical analysis, additional empirical results, and more details on the model as well as the derivations of the results which are stated below are provided in a Technical Appendix which is available at `http://www.beta-umr7522.fr/productions/WP/mainwp.php?y=2016`.

where A^j represents the labor productivity index. In order to explore the implications of labor market frictions for the relative wage and the relative price, we must introduce some notations that will be useful later.

Because firms face a cost by maintaining job vacancies, they receive a surplus equal to the marginal revenue of labor Ξ^j less the product wage W^j. Symmetrically, so as to compensate for the cost of searching for a job, unemployed workers receive a surplus equal to the product wage less the reservation wage W_R^j. We denote by Ψ^j the overall surplus created when a job-seeking worker and a firm with a job vacancy conclude a contract. The overall surplus is equal to the difference between the marginal revenue of labor and the sectoral reservation wage:

$$\Psi^j \equiv \Xi^j - W_R^j, \tag{2}$$

where $\Xi^N = PA^N$ and $\Xi^T = A^T$. Denoting by θ^j the labor market tightness in sector j, defined as the ratio of job vacancies to unemployed workers, the change of the reservation wage in percentage is proportional to the labor market tightness, i.e., $\hat{w}_R^j = \chi^j W_R^j \hat{\theta}^j$ where χ^j represents the share of the surplus associated with a labor contract in the marginal benefit of search. Intuitively, when firms post more job vacancies, the labor market tightness rises which increases the probability of finding a job and thus the reservation wage.

The product wage W^j paid to the worker in sector j is equal to the reservation wage W_R^j plus a share α_W of the overall surplus Ψ^j:

$$W^j = \alpha_W \Psi^j + W_R^j, \tag{3}$$

where the worker bargaining power α_W is assumed to be symmetric across sectors. Subtracting the traded wage from the non traded wage by using (3), and differentiating leads to an equation that relates the change in the relative wage of non tradables to the growth differential between sectoral labor market tightness and surpluses:

$$\hat{w}^N - \hat{w}^T = -\frac{\chi W_R}{W}\left(\hat{\theta}^T - \hat{\theta}^N\right) - \frac{\alpha_W \Psi}{W}\left(\hat{\Psi}^T - \hat{\Psi}^N\right), \tag{4}$$

where we assume that initially $W^j \simeq W$ and $\chi^j W_R^j \simeq \chi W_R$ and $\Psi^j \simeq \Psi$ to ease the interpretation. In a model abstracting from labor market frictions, as the standard BS model, searching for a job is a costless activity so that Ψ and χ are nil; hence sectoral wages rise at the same speed. Conversely, in a model with labor market frictions, technological change biased toward the traded sector may lower the non traded wage relative to the traded wage. The reason is as follows. First, as captured by the first term on the RHS of (4), higher productivity growth in tradables relative to non tradables induces traded firms to recruit more than non traded firms; because agents experience a utility loss when increasing the search intensity for a job in the traded sector, traded firms must increase wages to attract workers as reflected by the rise in the ratio θ^T/θ^N. Moreover, as shown by the second term on the RHS of (4), by raising Ψ^T/Ψ^N, technological change biased toward the traded sector lowers the non traded wage relative to the traded wage. Intuitively, searching for a job is time consuming and a higher Ψ^T/Ψ^N covers the increased cost of this activity, the worker obtaining a share equal to α_W.

When a labor contract is concluded with a worker, the representative firm in sector j receives the marginal revenue of labor Ξ^j which must cover the recruiting cost plus the dividend per worker equivalent to $(1-\alpha_W)\,\Psi^j$ and the wage rate paid to the worker:

$$\Xi^j = (1-\alpha_W)\,\Psi^j + W^j. \tag{5}$$

Subtracting Ξ^T from Ξ^N, and differentiating, we obtain a relationship between the relative price growth and the growth differential between sectoral productivity gains, wages and surpluses:

$$\hat{p} = \hat{a}^T - \hat{a}^N + \frac{W}{\Xi}\left(\hat{w}^N - \hat{w}^T\right) - \frac{(1-\alpha_W)\,\Psi}{\Xi}\left(\hat{\Psi}^T - \hat{\Psi}^N\right), \tag{6}$$

where we assume that initially $\Xi^j \simeq \Xi$, $\Psi^j \simeq \Psi$, and $W^j \simeq W$. According to (6), when abstracting from labor market frictions, sectoral surpluses are nil while sectoral wages increase at the same speed; as a result, the relative price of non tradables must appreciate by the same amount as the productivity differential. Unlike, in a model with labor market frictions, as captured by the second term on the RHS of (6), the relative wage of non tradables falls because traded firms have to pay higher wages to compensate for the workers' mobility costs. Moreover, as shown by the third term on the RHS of (6), since traded firms recruit more than non traded firms, the hiring cost must be covered by an increase in Ψ^T/Ψ^N, the firm obtaining a share equal to $1-\alpha_W$. Thus, by lowering the relative wage of non tradables and increasing the hiring cost in the traded sector relative to that in the non traded sector, the relative price of non tradables appreciates by less than 1% following a rise in the productivity of tradables relative to non tradables of 1%.

The relative wage and relative price equations described by (4) and (6) respectively, allow us to explain in what labor market frictions imply that sectoral wages may no longer rise at the same speed and the elasticity of the relative price of non tradables w.r.t. the productivity differential may be smaller than one. However, such conclusions are established by abstracting from the goods market equilibrium which matters as long as labor is not perfectly mobile across sectors. In section 4, we show that the full steady-state can be solved for the relative price and the relative wage, i.e., $P \equiv P^N/P^T = P\left(A^T, A^N\right)$ and $\Omega \equiv W^N/W^T = \Omega\left(A^T, A^N\right)$. Because all variables display trends, our empirical strategy consists in estimating the cointegrating relationships with the productivity discrepancy between tradables and non tradables.[9]

[9] While we have recourse to cointegration methods to estimate the relative price and relative wage effects of higher productivity in tradables relative to non tradables as in Cardi and Restout [2015], the empirical study in the present paper differs along several dimensions. First, we measure technological change with sectoral labor productivity instead of sectoral TFP. Second, our dataset includes 18 OECD countries while Cardi and Restout [2015] restrict their attention to a sample of 14 OECD economies. Third, the authors show empirically that the relative wage falls more in countries with lower intersectoral reallocation of labor.

2.2 Data Construction

Before empirically exploring the relative price and relative wage effects of a productivity differential, we briefly describe the dataset we use and provide details about data construction below and in Appendix A as well. Our sample consists of a panel of eighteen OECD countries: Australia (AUS), Austria (AUT), Belgium (BEL), Canada (CAN), Germany (DEU), Denmark (DNK), Finland (FIN), France (FRA), Ireland (IRL), Italy (ITA), Japan (JPN), Korea (KOR), Netherlands (NLD), Norway (NOR), Spain (ESP), Sweden (SWE), United Kingdom (GBR) and the United States (USA). Our sample covers the period 1970-2007 (except for Japan: 1974-2007), for eleven 1-digit ISIC-rev.3 industries.

To split these eleven industries into traded and non traded sectors, we follow the classification suggested by De Gregorio et al. [1994]. Agriculture, hunting, forestry and fishing; Mining and quarrying; Total manufacturing; Transport, storage and communication are classified as traded industries. Following Jensen and Kletzer [2006], we updated the classification of De Gregorio et al. [1994] by treating Financial intermediation as a traded industry. Electricity, gas and water supply; Construction; Wholesale and retail trade; Hotels and restaurants; Real estate, renting and business services; Community, social and personal services are classified as non traded industries.[10]

We use the EU KLEMS [2011] database which provides domestic currency series of value added in current and constant prices, labor compensation and employment (number of hours worked) for each sector j (with $j = T, N$), permitting the construction of price indices p^j (in log) which correspond to sectoral value added deflators, sectoral wage rates w^j (in log), and sectoral measures of productivities a^j (in log). The relative price of non tradables at time t in country i, $p_{i,t}$, is the log of the ratio of the non traded value added deflator to the traded value added deflator (i.e., $p_{i,t} = p^N_{i,t} - p^T_{i,t}$). The relative wage $\omega_{i,t}$ is the log of the ratio of the non traded wage to the traded wage (i.e., $\omega_{i,t} = w^N_{i,t} - w^T_{i,t}$). We use sectoral labor productivities $A^j_{i,t}$ to approximate technical change. Sectoral productivities $A^j_{i,t}$ at time t in country i are constructed from constant-price (domestic currency) series of value added $Y^j_{i,t}$ and hours worked $L^j_{i,t}$, i.e., $A^j_{i,t} = Y^j_{i,t}/L^j_{i,t}$.[11]

In the present contribution, we capture labor market institutions by using a set of three indicators and show that the decline in the relative wage is more pronounced in countries with more regulated labor markets.

[10]De Gregorio et al. [1994], classify a sector as tradable if more than 10 percent of its total production is exported. This classification has been updated by Jensen and Kletzer [2006] who use locational Gini coefficients to measure the geographical concentration of different sectors and classify sectors with a Gini coefficient below 0.1 as non-tradable and all others as tradable (the authors classify activities that are traded domestically as potentially tradable internationally).

[11]It is worthwhile mentioning that our empirical results are robust to the measure of technological change (sectoral labor productivity vs. sectoral TFP with alternative assumptions regarding the non tradable content of investment expenditure), the classification of industries between traded and non traded sectors, the measure of labor (number of hours worked vs. number of workers).

2.3 A First Glance at the Data

We begin by examining the data for the 18 OECD economies over the period 1970-2007. Figure 1 plots the average relative price growth against the average relative wage growth which have been scaled (i.e., divided) by the average productivity growth differential between tradables and non tradables. Quantitatively, the BS model predicts that a 1 percentage point increase in the productivity differential leaves unaffected the relative wage of non tradables and appreciates the relative price of non tradables by 1%. Hence, according to the BS model, all countries should be positioned at point BS along the X-axis with coordinates (1,0). However, we find that all countries are positioned to the south-west of point BS. Quantitatively, we find that a 1 percentage point increase in the productivity differential is associated with a fall in the relative wage which varies between -0.02% for Belgium and -0.41% for Denmark. Regarding the relative price, we find that its appreciation varies between 0.34% for Canada to 0.97% for Japan while Norway experiences a fall in the relative price of non tradables due to the large increase of prices in traded industries such as 'Mining and Quarrying' (which accounts for about one fourth of GDP) over 1995-2007.

The data seem to challenge the conventional wisdom that labor mobility would gradually eliminate wage differences across sectors. If it were the case, the ratio of the non traded wage to the traded wage would remain unchanged. However, we observe that the relative wage tends to fall. Moreover, because non traded wages increase by a smaller amount that if labor were perfectly mobile, the relative price of non tradables appreciates by a smaller amount than that suggested by the standard BS model. To confirm these findings, in the following, we have recourse to panel data unit root tests and cointegration methods.

< Please insert Figure 1 about here >

We test for the presence of unit roots in the logged relative wage ω (i.e., $w^N - w^T$) and in the difference between the (log) relative price p (i.e., $p^N - p^T$) and the (log) relative productivities (i.e., $a^T - a^N$). If the wage equalization hypothesis was right, sectoral wages would increase at the same speed so that the relative wage of non tradables would be stationary. As a result, the non tradable unit labor cost would rise by the same amount as the productivity differential. Hence, the difference between the (logged) relative price and the (logged) relative productivity should be stationary as well.

We consider five panel unit root tests among those most commonly used in the literature. Results are summarized in Table 1.[12] As shown in the first column Table 1, all panel unit

[12]In Table 1, LLC and Breitung are the t-statistics developed by Levin et al. [2002] and Breitung [2000] respectively. IPS denotes the Im, Pesaran and Shin's [2003] W_{tbar} test. MW (ADF) and MW (PP) are the Maddala and Wu's [1999] P test based on Augmented Dickey-Fuller and Phillips-Perron p-values respectively. Hadri corresponds to Hadri's [2000] Z_{μ} test.

root tests, reveal that the relative wage variable is non-stationary at a 5% significance level. This finding suggests that labor market frictions prevent wage equalization across sectors in the long run. Regarding the relative price of non tradables and the productivity of tradables relative to productivity of non tradables, these variables are found to be non-stationary. As shown in the last column, the difference between the relative price of non tradables and the relative productivity is integrated of order one which implies that the productivity differential is not fully reflected in the non tradable unit labor cost and thus the relative price.

< Please insert Table 1 about here >

2.4 Estimating Long-Run Relationships

Because we aim to assess the ability of the model to replicate our empirical findings, we estimate the relative wage and the relative price responses to higher productivity of tradables relative to non tradables. To do so, we regress the (log) relative wage ω and the (log) relative price p on the (log) relative productivity, respectively:

$$\omega_{i,t} = \delta_i + \beta \, . \left(a^T_{i,t} - a^N_{i,t}\right) + v_{i,t}, \tag{7a}$$

$$p_{i,t} = \alpha_i + \gamma \, . \left(a^T_{i,t} - a^N_{i,t}\right) + u_{i,t}, \tag{7b}$$

where i and t index country and time and $v_{i,t}$ and $u_{i,t}$ are i.i.d. error terms. Country fixed effects are captured by country dummies δ_i and α_i.

Because all variables are non-stationary, we have recourse to cointegration techniques. Having verified that the assumption of cointegration is empirically supported, we estimate the cointegrating relationships by using fully modified OLS (FMOLS) and dynamic OLS (DOLS) procedures for the cointegrated panel proposed by Pedroni [2000], [2001].[13] Both estimators give similar results and coefficients β and γ of the cointegrating relationships are significant at 1%. Two major results emerge. First, estimates reported in the Table 2 reveal that a 1 percentage point increase in the productivity differential between tradables and non tradables lowers the relative wage by about 0.22% and appreciates the relative price by 0.64%. Second, as shown in the second line and the third line of Table 2, the predictions of the model abstracting from labor market frictions are strongly rejected: the slope of the cointegrating vector β (γ) is statistically significantly different from zero (one).

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[13] Cointegration tests can be found in the longer version of the paper. The DOLS estimator adds q leads and lags of $\triangle(a^T - a^N)$ as additional regressors in (4). We set $q = 1$; our results were identical for $q = 2$ and $q = 3$. We also used alternative estimators: dynamic fixed effects estimator, mean group estimator (Pesaran and Smith [1995]), pooled mean group estimator (Pesaran et al. [1999]) and the panel DOLS (Mark and Sul [2003]). The results are similar and thus are relegated in the Technical Appendix.

< Please insert Table 2 about here >

< Please insert Table 3 about here >

We now assess if our conclusion for the whole sample also holds for each country. To do so we run again the regression of relative wage and relative price on relative productivity by letting β and γ vary across countries. Table 3 show DOLS and FMOLS estimates for the eighteen countries of our sample. The first result that emerges is that the responses display a large dispersion across countries. More specifically, when considering statistically significant FMOLS estimates, the elasticity of the relative wage to relative productivity varies between -0.49 for Germany to -0.08 for Norway; while the elasticity of the relative price varies between 0.36 for Denmark to about 0.90 for Japan approximately. The second result is that despite these large cross-country variations, technological change biased toward the traded sector significantly lowers the relative wage in all countries while non traded prices relative to traded prices rise less than the productivity differential.

2.5 How to Explain the Long-Run Decline in the Relative Wage?

As shown in section 2.1, the less than proportional increase in the relative price relies upon the fall in the non traded wage relative to the traded wage which so far remains explained. How to rationalize the long-run decline in the relative wage? Our panel unit root tests reveal that the sectoral wage differential persists in the long-run, thus indicating the existence of substantial mobility costs across sectors.

The standard neoclassical model abstracting from labor market frictions predicts that technological change will trigger a reallocation of resources towards sectors with higher productivity, thus progressively eliminating the wage differential. Contrary to conventional wisdom, the literature adopting a structural empirical approach has questioned the assumption of wage equalization and has uncovered substantial mobility costs. Artuç et al. [2010] estimate that inter-sectoral costs of mobility in the United States are in the order of six times annual average wages. Lee and Wolpin [2006] find that the cost of moving between the goods and the services sectors within the same occupation is estimated to be significantly larger than moving between occupations within the same sector. According to Lee and Wolpin's estimates over 1968-2000, the mobility cost between sectors ranges from 50 to 75% of average annual earnings while the intersectoral wage differential is persistent in the long-run. Using 25 years of matched employer-employee data from Brazil, Dix-Carneiro and Kovak [2015] present evidence of large mobility costs following the country's trade liberalization in the early 1990s. More precisely, it is found that local shocks have steadily growing effects on regional formal sector wages and employment for 20 years. Hence, the impact of local shocks is not dissipated over time through wage-equalizing migration.

While the causes of labor market frictions hampering labor reallocation are diverse, they can be classified into two categories: those related to the workers' characteristics, thus affecting labor supply, and those related to rigid labor markets influencing firms' labor demand. From the worker point of view, the mobility costs can be interpreted as psychological costs when switching from one sector to another (see e.g., Dix-Carneiro [2014]), geographic mobility costs (see e.g., Kennan and Walker [2011]) or can be the result of sector-specific human capital (see e.g., Lee and Wolpin [2006]). Like Alvarez and Shimer [2011], in our model presented in section 3, we consider that mobility costs experienced by workers are captured by a utility loss. More precisely, we assume an endogenous sectoral labor force participation decision which implies that the allocation of the labor force across sectors is elastic to the ratio of sectoral reservation wages. Following technological change biased toward the traded sector, traded firms have to pay higher wages in order to compensate for the workers' utility loss when switching. As a result, the relative wage of non tradables must fall, and more so the lower the elasticity of labor supply at the extensive margin.

While technological change biased toward the traded sector drives down the relative wage because traded firms have to pay higher wages than those paid by the non traded sector in order to attract workers, the size of the decline in the relative wage may vary across countries. The reason is that labor market institutions influence the elasticity of labor demand with respect to technological change. Recently, Kambourov [2009] put forward higher firing costs as an explanation of lower inter-sectoral reallocation following trade reform episodes in Latin American countries. In the same spirit, we conjecture that the degree of labor market regulation influences firms' hiring decisions and thus the relative wage response to higher productivity growth in tradables relative to non tradables.

Labor market regulation encompasses several dimensions. In our paper, we consider three aspects: the strictness of employment protection against dismissals, the generosity of unemployment benefit scheme, and the worker bargaining power. The advantage to restrict our attention to these three dimensions is that the indicators are available for almost all countries of our sample and over a long enough time horizon. In the following, we use these indicators to test our conjecture according to which the relative wage of non tradables falls more in countries where the labor market regulation is more pronounced. As will be clear later when we will further develop the transmission mechanism, the labor regulation influences the relative wage response through two channels:

- First, we expect the traded wage to increase more in countries where unemployment benefits are more generous or workers have a larger bargaining power; intuitively, as these economies display a low labor market tightness, hiring is more profitable following technological change because it is easier to fulfill job vacancies; as will be detailed subsequently, a larger increase in hirings in the short-run leads a higher rise in net exports in the long-run; consequently, labor demand in the traded sector is more elastic to productivity growth in countries where the replacement rate or the worker bargaining power is higher.

- Second, we conjecture that in countries with higher firing costs, the non traded wage should rise less. Because technological change tends to lower aggregate labor supply through the positive wealth effect while the non traded sector experiences relatively low productivity gains, the shrinking non traded establishments are subject to the redundancy cost; as a result, they are less prone to recruit more workers when productivity increases. Hence, labor demand in the non traded sector is less elastic to technological change in countries where employment protection is more pronounced.

2.6 Labor Market Regulation and the Relative Wage Response to Technological Change

To evaluate the role of labor market regulation in explaining the relationship between relative wage and relative productivity, we proceed as follows. First, we present the indicators of labor market regulation. Then we empirically explore our conjecture by using a simple split-sample analysis.

2.6.1 Measures for Labor Market Regulation

To explore its role in the determination of the relative wage response, we measure the degree of labor market regulation which commonly involves three dimensions:[14]

- The first aspect is the difficulty of redundancy that we measure by the employment protection legislation (EPL hereafter) index provided by the OECD; this index which captures the strictness of legal protection against dismissals for permanent workers has the advantage to be available for all countries of our sample over the period 1985-2007 (except for Korea, 1990-2007).[15] As emphasized by Boeri and Van Ours [2008], the measure for strictness of employment protection can be misleading because regulation was eased in most European countries for temporary contracts, such as Spain, while the regulation for workers with permanent contracts hardly changed. Moreover, at the same time, the scope of fixed-term contracts was significantly expanded. In order to have a more accurate measure of the difficulty of redundancy, we use an alternative indicator by adjusting EPL for regular workers with the share of permanent workers

[14]Summary statistics of the labor market regulation indicators used in the empirical analysis can be found in the Technical Appendix.

[15]The OECD indicator takes into account various aspects of firing cost, such as the administrative procedures, the length of the advance notice period, the amount of the severance payment, the severity of enforcement. We take the measure for strictness of employment protection for individual and collective dismissals (regular contracts).

in the economy. The EPL index, denoted by EPL_{adj}, is lower in english speaking countries and higher in Southern (see e.g., Spain), Western (see e.g., the Netherlands), and Northern (see e.g., Sweden) European countries. By and large, adjusting the EPL index by excluding from total employment workers employed with a temporary contract merely modifies the ranking of countries, except for Spain.

- The generosity of unemployment benefit systems, denoted by r, is measured by using the replacement rate provided by the OECD. The data we use for the unemployment replacement rate for both European countries and the US are taken from the OECD database which calculates the average of the net unemployment benefit (including social assistance and housing benefits) replacement rates for two earnings levels, three family situations and three durations of unemployment (1st year, 2nd and 3rd year, 4th and 5th year).[16] There is considerable heterogeneity in this indicator, which varies from a low of about 10% for Italy and 26% for the United States to a high of 78% for Denmark. As shown in the last line, the average EU-12 replacement rate is more than twice as high as the US's.

- Measuring the extent of the worker bargaining power is a difficult task. In the empirical literature, the worker bargaining power is commonly captured by the bargaining coverage; we thus use this indicator, denoted by $BargCov$, which gives the proportion of employees covered by collective bargaining. Excluding Korea since data are only available from 2002, the bargaining coverage averages 69%. While the bargaining coverage is much lower than the sample average, in English-speaking (except for Australia) and Japan, it exceeds 80% in Scandinavian countries and Western countries, except for Spain. Data are taken from the ICTWSS database (Jelle Visser [2009]).

As a first pass at gauging the role of labor market regulation in the determination of the relative wage effects of technological change biased toward the traded sector, we plot the FMOLS estimates for the relative wage responses against the three indicators capturing the extent of labor market regulation in Figure 2. More specifically, Figures 2(a), 2(b), 2(c) plot the absolute values of β_i taken from Table 3 against the EPL index adjusted with the share of permanent workers, the net unemployment benefit replacement rates, and the bargaining coverage, respectively. Because time series for the unemployment benefit replacement rate and bargaining coverage are available only from the beginning of the 2000's for Korea and thus are too short, we exclude this country from Figures 2(b) and 2(c). In line with our conjecture, the trend lines in Figures 2(a), 2(b), 2(c) show that the estimated responses of the relative wage and our three measures of labor market regulation are positively related

[16] It is worthwhile noticing that the unemployment benefit rates are very similar across counties when considering short-term unemployment (less than one year) but display considerable heterogeneity for long-term unemployment. We believe that the last measure is more able to capture the extent of generosity of the unemployment benefit scheme.

across countries.

While for an economy such as the United States, the labor market regulation is unanimously low along its three dimensions, the conclusion is not clear-cut for the majority of OECD economies; for example, while the Italian unemployment benefit scheme is the least generous, the strictness of employment protection is among the highest; conversely, while replacement rates are higher than OECD countries' average in Canada and the United Kingdom, the firing costs are low in these two economies. Because labor market regulation encompasses three dimensions, we have recourse to a principal component analysis in order to have one overall indicator encompassing all the dimensions of labor market institutions. We believe that this indicator gives a more accurate measure of the degree of labor market regulation; in particular, Figure 2(d) displays the traditional distinction between English-speaking and Continental European economies, labor markets being much less regulated in the former than the latter countries. Importantly, in accordance with our conjecture, the trend line is upward sloping, thus suggesting that technological change biased toward the traded sector lowers the relative wage more in countries where labor market regulation is more pronounced.

< Please insert Figure 2 about here >

2.6.2 Empirical results

To empirically explore our conjecture according to which the relative wage falls more following higher productivity growth in tradables relative to non tradables in countries with more regulated labor market, we perform a simple split-sample analysis. Hence, we compare the relative wage behavior of 9 countries with high and 9 economies with low labor market regulation by running the regression of the relative wage on relative productivity for each sub-sample:

$$\omega_{i,t} = \delta_i + \beta^c \left(a^T_{i,t} - a^N_{i,t}\right) + v_{i,t}, \quad c = H, L, \tag{8}$$

where β^H (β^L) captures the response of the relative wage to a productivity differential in countries with higher (lower) labor market regulation.

The DOLS and FMOLS estimates are reported in the first and the second line of Table 4 for countries with high and low labor market regulation. The two last lines of Table 4 gives the sub-sample's average of the corresponding labor market regulation index. As the results in Table 4 show, the decline in the relative wage is greater for countries with more regulated labor markets. While countries providing lower unemployment benefits experience a decline in the relative wage of -0.16% approximately, the second set of countries with generous unemployment benefits experience a decline in ω of -0.26%. A similar pattern emerges when we exploit a second dimension of labor market regulation, namely the strictness of employment protection. Since series for EPL are available over 1985-2007, we run again the regression (8) over this period to be consistent. We find that a 1 percentage point increase in the productivity differential between tradables and non tradables lowers the relative wage by 0.17% in countries with higher firing costs while ω declines by only 0.13%. Furthermore, as shown in the third column of Table 4, the worker bargaining power captured by the bargaining coverage exerts a significant impact on the relative wage response; more precisely, the relative wage falls by -0.24% instead of -0.18% in countries where the worker bargaining power is relatively higher. Finally, as displayed in the last column of Table 4, when we have recourse to a principal component analysis, we find that countries with more regulated labor markets experience a larger decline in the relative wage.

< Please insert Table 4 about here >

To conclude, this empirical evidence suggest that labor market regulation plays a key role in the determination of the relative wage response to higher productivity in tradables relative to non tradables. In the following, we develop a dynamic general equilibrium model with a traded and a non traded sector by allowing for labor market frictions. In particular, our aim is to assess its ability to account for the following set of empirical findings. A productivity differential of 1% between tradables and non tradables: i) raises the relative price of non tradables p by 0.64%, ii) lowers the relative wage ω by 0.22%, iii) ω declines more in countries where the labor market regulation is more pronounced.

3 The Framework

The country is small in terms of both world goods and capital markets, and faces a given world interest rate, $r^{\star}$.[17] The small open economy is populated by a constant number of identical households and firms that have perfect foresight and live forever. Households decide on labor market participation and consumption while firms decide on hirings. The economy consists of two sectors. One sector produces a traded good denoted by the superscript T that can be exported while the other sector produces a non-traded good denoted by the superscript N. The setup allows for traded and non-traded goods to be used for consumption. The traded good is chosen as the numeraire. The labor market, in the tradition of Diamond-Mortensen-Pissarides, consists of a matching process within each sector between the firms who post job vacancies and unemployed workers who search for a job. Time is continuous and indexed by t.

[17]The price of the traded good is determined on the world market and exogenously given for the small open economy.

3.1 Households

At each instant the representative agent consumes traded goods and non-traded goods denoted by $C^T(t)$ and $C^N(t)$, respectively, which are aggregated by a constant elasticity of substitution function:

$$C\left(C^T(t), C^N(t)\right) = \left[\varphi^{\frac{1}{\phi}}\left(C^T(t)\right)^{\frac{\phi-1}{\phi}} + (1-\varphi)^{\frac{1}{\phi}}\left(C^N(t)\right)^{\frac{\phi-1}{\phi}}\right]^{\frac{\phi}{\phi-1}}, \tag{9}$$

where φ is the weight of the traded good in the overall consumption bundle $(0 < \varphi < 1)$ and ϕ is the intratemporal elasticity of substitution $(\phi > 0)$.

The economy that we consider consists of a representative household with a measure one continuum of identical infinitely lived members. At any instant, members in the household derive utility from consumption goods C and experience disutility from working and searching efforts. More precisely, the representative household comprises members who engage in only one of the following activities: working and searching a job in each sector, or enjoying leisure. Assuming that the representative individual is endowed with one unit of time, leisure is defined as $1 - L^T(t) - L^N(t) - U^T(t) - U^N(t)$, where $L^j(t)$ denotes units of labor time and $U^j(t)$ corresponds to time spent on searching for a job in sector j (with $j = T, N$). Because the labor force is not constant, we allow for the transition between employment and unemployment and the transition between leisure and labor force. Unemployed agents are randomly matched with job vacancies according to a matching function described later. Since the timing of a match is random, agents face idiosyncratic risks. To simplify the analysis, we assume that members in the household perfectly insure each other against variations in labor income.

We consider that the utility function is additively separable in the disutility received by working and searching in the two sectors. Such a specification makes it impossible to switch from one sector to another instantaneously without going through a spell of search unemployment, as in Alvarez and Shimer [2011].[18] This can be justified on the grounds of sector-specific skills as well as geographical or psychological mobility costs. The representative household chooses the time path of consumption and labor force to maximize the following objective function:

$$U = \int_0^\infty \left\{ \frac{1}{1-\frac{1}{\sigma_C}} C(t)^{1-\frac{1}{\sigma_C}} - \frac{\zeta^T}{1+\frac{1}{\sigma_L^T}} F^T(t)^{1+\frac{1}{\sigma_L^T}} - \frac{\zeta^N}{1+\frac{1}{\sigma_L^N}} F^N(t)^{1+\frac{1}{\sigma_L^N}} \right\} e^{-\beta t} \mathrm{d}t, \tag{10}$$

where $\zeta^j > 0$, $\beta > 0$ is the consumer's subjective time discount rate, and $\sigma_C > 0$ is the intertemporal elasticity of substitution for consumption; $\sigma_L^j > 0$ is the elasticity of labor supply at the extensive margin in sector $j = T, N$; it measures the extent of workers' moving costs: the smaller the elasticity of labor supply, the larger the utility loss when

[18] Our model is also closely related to the setup by Schubert [2013] who develops a two-sector open model with search frictions to analyze the role of foreign demand on unemployment.

switching, and thus the lower the degree of labor mobility across sectors. For later use, we denote by $u^j(t)$ the sectoral unemployment rate defined as $u^j = \frac{U^j(t)}{U^j(t)+L^j(t)} = \frac{U^j(t)}{F^j(t)}$ with $F^j(t) = L^j(t) + U^j(t)$ the labor force in sector j.

At each instant of time, $m^j(t)U^j(t)$ unemployed agents find a job in sector $j = T, N$ and $s^j L^j(t)$ employed individuals lose their job. Employment in sector j evolves gradually according to:

$$\dot{L}^j(t) = m^j(t)U^j(t) - s^j L^j(t), \tag{11}$$

where $m^j(t)$ denotes the rate at which unemployed agents find jobs and s^j is the constant rate of job separation; $1/m^j(t)$ can be interpreted as the average unemployment duration; m^j is a function of labor market tightness $\theta^j(t)$ which is defined as the ratio of the number of job vacancies over unemployed agents in sector j.

Households supply $L^j(t)$ units of labor services in sector $j = T, N$ for which they receive the product wage $W^j(t)$. We denote by $A(t)$ the stock of financial wealth held by households which comprises internationally traded bonds, $B(t)$, and shares on domestic firms. Because foreign bonds and domestic shares are perfect substitutes, the stock of financial wealth yields net interest rate earnings $r^\star A(t)$. Denoting by $T(t)$ the lump-sum taxes, the flow budget constraint is equal to households' real disposable income less consumption expenditure $P_C(t)C(t)$:

$$\dot{A}(t) = r^\star A(t) + \sum_j W^j(t)L^j(t) + \sum_j R^j U^j(t) - T(t) - P_C\left(P(t)\right)C(t), \tag{12}$$

where P_C is the consumption price index which is a function of the relative price of non-traded goods P and R^j represents unemployment benefits received by job seekers in sector j.

The key equations characterizing optimal household behavior are:[19]

$$C(t) = \left(P_C(t)\lambda(t)\right)^{-\sigma_C} \tag{13a}$$

$$F^j(t) = \left\{\lambda(t)\left[m^j\left(\theta^j(t)\right)\xi^j(t) + R^j\right]\right\}^{\sigma_L^j}, \tag{13b}$$

$$\dot{\lambda}(t) = \lambda(t)\left(\beta - r^\star\right), \tag{13c}$$

$$\dot{\xi}^j(t) = \left(s^j + r^\star\right)\xi^j(t) - \left[W^j(t) - \frac{\left(F^j(t)\right)^{1/\sigma_L^j}}{\lambda(t)}\right], \tag{13d}$$

and the appropriate transversality conditions; $\lambda(t)$ and $\xi^j(t)$ denote the shadow prices of wealth and finding a job in sector j, respectively. In an open economy model with a representative household having perfect foresight, a constant rate of time preference and perfect access to world capital markets, we impose $\beta = r^\star$ in order to generate an interior

[19] First-order conditions consist of (13a) and (13c) together with $\left(F^j\right)^{1/\sigma_L^j} = m^j\xi'^{,j} + R^j\lambda$ and $\dot{\xi}' = \left(s^j + \rho\right)\xi'^{,j} - \left[\lambda W^j - \left(F^j\right)^{1/\sigma_L^j}\right]$. Denoting by $\xi^j \equiv \xi'^{,j}/\lambda$, using (13a) and (13c), we get (13b) and (13d). Since $\xi'^{,j}$ is the utility value of an additional job and λ is the marginal utility of wealth, ξ^j is the pecuniary value of an additional job.

solution. This standard assumption made in the literature implies that the marginal utility of wealth, λ, will undergo a discrete jump when individuals receive new information and must remain constant over time from then on, i.e., $\lambda(t) = \bar{\lambda}$.

Eq. (13b) shows that labor market participation is a positive function of the reservation wage $W_R^j(t)$, which is defined as the sum of the expected value of a job $m^j(t)\xi^j(t)$ and the unemployment benefit R^j. Solving eq. (13d) forward and invoking the transversality condition yields:

$$\xi^j(t) = \int_t^\infty \left[W^j(\tau) - W_R^j(\tau)\right] e^{\left(s^j + r^\star\right)(t-\tau)} \mathrm{d}\tau. \tag{14}$$

Eq. (14) states that ξ is equal to the present discounted value of the surplus from an additional job consisting of the excess of labor income over the household's outside option. Note that as described above, we consider a representative household who splits available time between leisure and market activities (i.e., time devoted to job search and work). While labor supply is elastic at the extensive margin, search effort and worked hours are supplied inelastically.[20] For the sake of clarity, we drop the time argument below when this causes no confusion.

Applying Shephard's lemma (or the envelope theorem) yields expenditure in non tradables and tradables, i.e., $PC^N = \alpha_C P_C C$, $C^T = (1-\alpha_C) P_C C$, with α_C being the share of non traded goods in consumption expenditure.[21] Intra-temporal allocation of consumption follows from the following optimal rule:

$$\left(\frac{1-\varphi}{\varphi}\right)\frac{C^T}{C^N} = P^\phi. \tag{15}$$

An appreciation in the relative price of non tradables P increases expenditure on tradables relative to expenditure on non tradables (i.e. C^T/PC^N), only when $\phi > 1$.

3.2 Firms

Each sector consists of a large number of identical firms. Both the traded and non-traded sectors use labor, L^T and L^N, according to constant returns to scale production functions, $Y^T = A^T L^T$ and $Y^N = A^N L^N$. Firms post job vacancies V^j to hire workers and face a cost per job vacancy κ^j which is assumed to be constant and measured in terms of the traded good. Firms pay the wage W^j decided by the generalized Nash bargaining solution. As producers face a labor cost W^j per employee and a cost per hiring of κ^j, the profit function of the representative firm in sector j is:

$$\pi^j = \Xi^j L^j - W^j L^j - \kappa^j V^j - x^j \,.\max\left\{0, -\dot{L}^j\right\}, \tag{16}$$

[20] More precisely, depending on the search parameters captured by s^j and m^j, labor force is split between working time and job search. Along the transitional dynamics, using the fact that $U^j = F^j - L^j$, agents supply working time L^j according to the following accumulation equation $\dot{L}^j = m^j U^j - s^j L^j = m^j F^j - \left(m^j + s^j\right) L^j$, where F^j is labor force and L^j corresponds to hours worked in sector j supplied by the representative household.

[21] Specifically, we have $\alpha_C = \frac{(1-\varphi)P^{1-\phi}}{\varphi + (1-\varphi)P^{1-\phi}}$. Note that α_C depends negatively on the relative price P as long as $\phi > 1$.

where Ξ^j is the marginal revenue of labor with $\Xi^T = A^T$ and $\Xi^N = PA^N$; x^j is a firing tax paid to the State when layoffs are higher than hirings, i.e. if $\dot{L}^j < 0$ (see e.g., Heijdra and Ligthart [2002], Veracierto [2008]). The firing tax is introduced to capture the strictness of legal protection against dismissals and is modelled as a tax on reducing employment.[22]

Denoting by f^j the rate at which a vacancy is matched with unemployed agents, the law of motion for labor is given by:

$$\dot{L}^j = f^j V^j - s^j L^j, \tag{17}$$

where $f^j V^j$ represents the flow of job vacancies which are fulfilled; note that $f^j\left(\theta^j\right)$ decreases with labor market tightness θ^j.

Denoting by γ^j the shadow price of employment to the firm, and keeping in mind that f^j is taken as given, the maximization problem yields the following first-order conditions:

$$\begin{aligned} \gamma^j + x^j &= \frac{\kappa^j}{f^j\left(\theta^j\right)}, & \text{(18a)} \\ \dot{\gamma}^j &= \gamma^j\left(r^\star + s^j\right) - \left(\Xi^j - x^j s^j - W^j\right). & \text{(18b)} \end{aligned}$$

Eq. (18a) requires the marginal cost of vacancy, κ^j, to be equal to the marginal benefit of vacancy, $f^j(.)\left(\gamma^j + x^j\right)$. Solving equation (18b) forward and invoking the transversality condition yields:

$$\gamma^j(t) = \int_t^\infty \left[\Xi^j(\tau) - x^j s^j - W^j(\tau)\right] e^{\left(s^j + r^\star\right)(t-\tau)} \mathrm{d}\tau. \tag{19}$$

Eq. (19) states that γ^j is equal to the present discounted value of the cash flow earned on an additional worker, consisting of the excess of marginal revenue of labor Ξ^j over the wage W^j and the expected firing cost $x^j s^j$. Following higher productivity A^j, the marginal revenue of labor Ξ^j rises; hence hiring becomes more profitable which induces firms to post job vacancies, but less so in countries with a higher firing cost x^j.

Differentiating $\gamma^j(t)L^j(t)$ w. r. t. time and inserting the law of motion for employment (17) together with the dynamic optimality condition (18b), solving forward, and making use of the transversality condition and eq. (18a), we get:

$$\gamma^j(t)L^j(t) = \int_t^\infty \pi^j(\tau)\, e^{-r^\star(\tau-t)} \mathrm{d}\tau. \tag{20}$$

Eq. (20) states that the value of human assets $\gamma^j L^j$ (or stock market value of the firm) is equal to the present discounted value of profits π^j.

3.3 Matching and Wage Determination

In each sector, there are job-seeking workers U^j and firms with job vacancies V^j which are matched in a random fashion. Assuming a constant returns to scale matching function, the

[22] While employment is lowered, the shrinking establishment is hiring; thus the representative firm simultaneously pays a firing tax and receives a hiring subsidy, the former being higher than the latter amount, i.e., $-x^j \dot{L}^j = x^j s^j L^j - x^j f^j V^j > 0$.

number of labor contracts M^j concluded per job seeker U^j gives the job finding rate m^j which is increasing in the labor market tightness θ^j:

$$m^j = \frac{M^j}{U^j} = X^j \left(\frac{V^j}{U^j}\right)^{\alpha_V^j} = X^j \left(\theta^j\right)^{\alpha_V}, \quad \alpha_V^j \in (0,1), \tag{21}$$

where α_V^j represents the elasticity of vacancies in job matches and X^j corresponds to the matching efficiency.[23] The number of matches M^j per job vacancy gives the worker-finding rate for the firm:

$$f^j = \frac{M^j}{V^j} = X^j \left(\theta^j\right)^{\alpha_V^j - 1}. \tag{22}$$

Eq. (22) shows that the instantaneous probability of the firm finding a worker is higher the lower the labor market tightness θ^j.

When a vacancy and a job-seeking worker meet, a rent is created which is equal to $\xi^j + \gamma^j + x^j$, where ξ^j is the value of an additional job, γ^j is the value of an additional worker, and x^j corresponds to the hiring subsidy.[24] The division of the rent between the worker and the firm is determined by generalized Nash bargaining over the wage rate:

$$\max_{W^j} \left(\xi^j\right)^{\alpha_W^j} \left(\gamma^j + x^j\right)^{1-\alpha_W^j}, \quad \alpha_W^j \in (0,1), \tag{23}$$

where α_W^j and $1 - \alpha_W^j$ correspond to the bargaining power of the worker and the firm, respectively.

Solving for (23), the product wage W^j is defined as a weighted sum of the labor marginal revenue plus the interest income from the hiring subsidy and the reservation wage:

$$W^j = \alpha_W^j \left(\Xi^j + r^\star x^j\right) + \left(1 - \alpha_W^j\right) \frac{\left(F^j\right)^{1/\sigma_L^j}}{\bar{\lambda}}. \tag{24}$$

An increase in the marginal product of labor, Ξ^j, which exerts an upward pressure on labor demand, or a rise in the labor market tightness, by raising the reservation wage (see eq. (13b)), pushes up the product wage.[25]

3.4 Government

The final agent in the economy is the government. Unemployment benefits $R^T U^T + R^N U^N$ are covered by lump-sum taxes T and the proceeds from the firing tax $\sum_j x^j \,.\max\left\{0, -\dot{L}^j\right\}$

[23] Note that the flows of workers in and out of employment are equal to each other in any symmetric equilibrium, i.e., $m^j U^j = f^j V^j$. Hence equations $\dot{L}^j = f^j V^j - s^j L^j$ and $\dot{L}^j = m^j U^j - s^j L^j$ indicate that the demand for labor indeed equates the supply.

[24] As mentioned above, the firing tax is modelled as a tax on reducing employment; because firms experience simultaneously outflow and inflow of workers, this shortcut to encompass the strictness of employment protection implies that establishments pay firing taxes and receive hiring subsidies at the same time, the former being larger than the latter amount.

[25] Note that the Nash bargaining wage depends positively on unemployment benefits R^j. To see it more formally, using the fact that $\xi^j = \frac{\alpha_W^j}{1-\alpha_W^j}\gamma^j$, $\gamma^j + x^j = \kappa^j/f^j$, $m^j/f^j = \theta^j$, we have $\left(F^j\right)^{1/\sigma_L^j}/\bar{\lambda} = \frac{\alpha_W^j}{1-\alpha_W^j}\kappa^j\theta^j + R^j$. Plugging this term into the Nash bargaining wage (24), we have:

$$W^j = \alpha_W^j \left(\Xi^j + r^\star x^j\right) + \left(1 - \alpha_W^j\right)\left[\frac{\alpha_W^j}{1-\alpha_W^j}\kappa^j\theta^j + R^j\right] = \alpha_W^j\left(\Xi^j + \kappa^j\theta^j + r^\star x^j\right) + \left(1 - \alpha_W^j\right) R^j.$$

according to the following balanced budget constraint:[26]

$$\sum_j x^j \,.\max\left\{0, -\dot{L}^j\right\} + T = \sum_j R^j U^j. \tag{25}$$

3.5 Market Clearing Conditions

Before characterizing the equilibrium dynamics and discussing the steady-state, we have to impose the market clearing condition for the non traded good according to which non traded output is only consumed domestically:

$$Y^N(t) = C^N(t). \tag{26}$$

Using the definition of the stock of financial wealth $A(t) \equiv B(t) + \gamma^T(t)L^T(t) + \gamma^N(t)L^N(t)$, differentiating with respect to time, substituting the accumulation equations of labor (11) and financial wealth (12) together with the dynamic equation for the shadow value of an additional worker (18b), using the government budget constraint (25) and the market clearing condition for the non traded good market (26), the accumulation equation for foreign assets is:

$$\dot{B}(t) = r^\star B(t) + A^T L^T(t) - C^T(t) - \kappa^T V^T(t) - \kappa^N V^N(t). \tag{27}$$

3.6 Solving the Model

In this subsection, we characterize the equilibrium dynamics and then discuss the steady-state.

3.6.1 Short-Run Solutions

We first determine short-run solutions which hold at each instant of time and are inserted into dynamic optimality conditions in order to analyze the equilibrium dynamics below. Equation (13a) can be solved for consumption:

$$C = C\left(\bar{\lambda}, P\right). \tag{28}$$

A rise in the shadow value of wealth induces agents to cut their real expenditure (i.e., $C_{\bar{\lambda}} < 0$) while an increase in the consumption price index triggered by an appreciation in the relative price of non-tradables P drives down consumption (i.e., $C_P < 0$). Inserting (28) into $C^T = (1-\alpha_C) P_C C$ and $PC^N = \alpha_C P_C C$ allows us to solve for consumption in tradables and non tradables, i.e., $C^T = C^T\left(\bar{\lambda}, P\right)$ and $C^N = C^N\left(\bar{\lambda}, P\right)$ with $C^j_{\bar{\lambda}} < 0$, $C^T_P \gtrless 0$ depending on whether $\phi \gtrless \sigma_C$ and $C^N_P < 0$.

[26] In the numerical analysis, we consider government spending for calibration purpose. In this case, eq. (25) can be rewritten as follows: $\sum_j x^j \,.\max\left\{0, -\dot{L}^j\right\} + T = \left(R^T U^T + R^N U^N\right) + G^T + PG^N$ where G^T and G^N government spending on tradables and non tradables, respectively. When $\dot{L}^j < 0$, government proceeds from the firing costs are redistributed back to agents as lump-sum transfers.

Substituting first the short-run solution for consumption in non tradables $C^N = C^N\left(\bar{\lambda}, P\right)$, the market clearing condition for the non traded good (26) can be solved for the relative price of non tradables as follows:

$$P = P\left(L^N, \bar{\lambda}, A^N\right), \tag{29}$$

where $P_{L^N} = \partial P/\partial L^N = A^N/C^N_P < 0$, $P_{\bar{\lambda}} = -C^N_{\bar{\lambda}}/C^N_P < 0$, and $P_{A^N} = \partial P/\partial A^N = L^N/C^N_P < 0$.

3.6.2 Saddle-Path Stability

We now analyze the saddle-path stability; hence, we first derive the system of differential equations. To determine the dynamic equation for labor market tightness θ^j in sector j, differentiate (18a) w. r. t. time, insert (18b), and eliminate γ^j by using (18a):

$$\dot{\theta}^j = \frac{\theta^j}{\left(1-\alpha^j_V\right)}\left\{\left(s^j + r^\star\right) - \frac{f^j\left(\theta^j\right)\left(1-\alpha^j_W\right)\Psi^j}{\kappa^j}\right\}, \tag{30}$$

where the overall surplus from an additional job in sector j denoted with Ψ^j is defined as the difference between the marginal product of labor and the reservation wage :

$$\Psi^j = \left(\Xi^j + r^\star x^j\right) - \frac{\left(F^j\right)^{1/\sigma^j_L}}{\bar{\lambda}}. \tag{31}$$

Differentiating first (13b) w. r. t. time and substituting (13d) yields the dynamic equation for job seekers:

$$\frac{1\left(F^j\right)^{\frac{1}{\sigma^j_L}-1}}{\sigma^j_L\bar{\lambda}}\dot{U}^j = \left[\frac{\left(F^j\right)^{1/\sigma^j_L}}{\bar{\lambda}} - R^j\right]\left[\left(s^j + r^\star\right) + \alpha^j_V\frac{\dot{\theta}^j}{\theta^j}\right] - m^j\left(\theta^j\right)\alpha^j_W\Psi^j - \frac{\left(F^j\right)^{\frac{1}{\sigma^j_L}-1}}{\sigma^j_L\bar{\lambda}}\dot{L}^j, \tag{32}$$

where we used the fact that $W^j - W^j_R = \alpha^j_W\Psi^j$.

Due to our assumption that disutility functions from participating in the labor market in the traded and the non traded sector are additively separable, hiring and search decisions in the traded and non traded labor markets are independent which implies that the Jacobian matrix is block recursive; hence, the saddle-path stability condition in the traded and non traded sectors can be explored separately. Inserting first appropriate short-run solutions, linearizing in the neighborhood of the steady-state, the dynamic system for the traded (non traded) sector which comprises three equations, i.e., the accumulation equation for employment (11), the dynamic equation for labor market tightness (30) and the dynamic equation for job seekers (32), we find that the determinant of the Jacobian matrix for the traded (non traded) sector is negative.[27] Hence, the linearized dynamic system possesses one negative eigenvalue denoted by ν^j_1 and two positive eigenvalues denoted by ν^j_2 and

[27] When focusing on the non traded sector, we have $\Xi^N = PA^N$; in this case, we have to insert the short-run stock solution for the relative price of non tradables (29) into the dynamic equation for θ^N and U^N.

ν_3^j. Assuming that the Hosios condition holds, i.e., setting $\alpha_W^j = \left(1-\alpha_V^j\right)$, eigenvalues satisfy $\nu_1^j < 0 < r^\star < \nu_2^j$, with $\nu_2^j = r^\star - \nu_1^j > 0$, and $\nu_3^j = s^j + r^\star > 0$. Note that when considering the traded sector, the negative and the positive eigenvalues reduce to $\nu_1^T = -\left(s^T + \tilde{m}^T\right) < 0$ and $\nu_2^T = \left(s^T + r^\star + \tilde{m}^T\right) > 0$.

Denote the long-term values with a tilde, the stable paths for employment, labor market tightness, and job seekers are given by:[28]

$$
\begin{aligned}
L^T(t) - \tilde{L}^T &= D_1^T e^{\nu_1^T t}, \quad \theta^T(t) - \tilde{\theta}^T = \omega_{21}^T D_1^T e^{\nu_1^T t}, \quad U^T(t) - \tilde{U}^T = \omega_{31}^T D_1^T e^{\nu_1^T t}, \quad (33a)\\
L^N(t) - \tilde{L}^N &= D_1^N e^{\nu_1^N t}, \quad \theta^N(t) - \tilde{\theta}^N = \omega_{21}^N D_1^N e^{\nu_1^N t}, \quad U^N(t) - \tilde{U}^N = \omega_{31}^N D_1^N e^{\nu_1^N t}, \quad (33b)
\end{aligned}
$$

where $D_1^j = L_0^j - \tilde{L}^j$ with $L_0^j = L^j(0)$ the initial level of employment in sector $j = T, N$, and ω_{ki}^j is the kth-element of eigenvector i for sector j; we have normalized ω_{11}^j to unity; it can be proven formally that $\omega_{21}^T = 0$, $\omega_{31}^T = -1$, $\omega_{21}^N < 0$, $\omega_{31}^N < 0$.

Two features of the two-sector economy's equilibrium dynamics deserve special attention. First, the dynamics for labor market tightness in the traded sector $\theta^T(t)$ degenerate as reflected by $\omega_{21}^T = 0$. Unlike, because the relative price of non tradables adjusts to clear the non traded good market while labor L^N is a state variable, $\theta^N(t)$ exhibits transitional dynamics; because $\omega_{21}^N < 0$, L^N and θ^N move in opposite directions. Second, in both sectors, the number of job seekers U^j falls as employment L^j builds up.

Inserting first the short-run solution for the relative price of non tradables (29) into $C^T = C^T\left(\bar{\lambda}, P\right)$, linearizing (27) around the steady-state, substituting formal solutions (33a)-(33b), and invoking the transversality condition, yields the stable solution for traded bonds $B(t) - \tilde{B} = \Phi^T\left(L^T(t) - \tilde{L}^T\right) + \Phi^N\left(L^N(t) - \tilde{L}^N\right)$ consistent with the intertemporal solvency condition:[29]

$$
\tilde{B} - B_0 = \Phi^T\left(\tilde{L}^T - L_0^T\right) + \Phi^N\left(\tilde{L}^N - L_0^N\right), \tag{34}
$$

where B_0 is the initial foreign asset position. Because $\Phi^T < 0$ and $\Phi^N < 0$, the current account is negatively related to changes in sectoral employment. Intuitively, to raise employment, firms must post more job vacancies; since hiring is a costly activity, recruiting expenditure rise which deteriorates the current account.

[28]Elements ω_{21}^N and ω_{31}^N of the eigenvector (associated with the stable eigenvalue ν_1^N) are:

$$
\omega_{21}^N = \frac{\left(2s^N + r^\star\right) + \left(s^N + r^\star - \nu_i^N\right)\left(\frac{s^N+\nu_i^N}{\tilde{m}^N}\right) + \tilde{m}^N\left(P_{L^N} A^N \frac{\bar{\lambda}}{v_{FF}^N} + 1\right)}{\frac{\left(m^N\right)'\tilde{U}^N}{\tilde{m}^N}\left(s^N + \tilde{m}^N + r^\star - \nu_i^N\right)} < 0, \quad \omega_{31}^N = \left(\frac{s^N + \nu_1^N}{\tilde{m}^N}\right) - \frac{(m')^N \tilde{U}^N}{\tilde{m}^N}\omega_{21}^N < 0.
$$

[29]The terms Φ^T and Φ^N are negative and given by:

$$
\Phi^T \equiv \frac{\Lambda^T}{\nu_1^T - r^\star} = -\frac{\left(A^T + \kappa^T \tilde{\theta}^T\right)}{\left(s^T + \tilde{m}^T + r^\star\right)} < 0, \quad \Phi^N \equiv \frac{\Lambda^N}{\nu_1^N - r^\star} < 0.
$$

where $\Lambda^N \equiv -C_{L^N}^T - \kappa^N \tilde{U}^N\left(1-\alpha_V^N\right)\omega_{21}^N - \frac{\kappa^N \tilde{\theta}^N\left(s^N + \nu_1^N\right)}{\tilde{m}^N} > 0$ with $C_{L^N}^T = \frac{\partial C^T}{\partial L^N}$.

3.6.3 Steady-State

We now describe the steady-state of the economy which comprises six equations. First, setting $\dot{\theta}^j = 0$ into eq. (30), we obtain the vacancy creation equation (which holds for the traded sector and non traded sector):

$$\frac{\kappa^j}{f^j\left(\tilde{\theta}^j\right)} = \frac{\left(1-\alpha_W^j\right)}{s^j + r^\star}\tilde{\Psi}^j, \quad \tilde{\Psi}^j \equiv \left(\Xi^j + r^\star x^j\right) - W_R^j, \quad j = T, N. \tag{35}$$

The LHS term of eq. (35) represents the marginal cost of recruiting in sector $j = T, N$. The RHS term represents the marginal benefit of an additional worker which is equal to the share, received by the firm, of the rent created by the encounter between a vacancy and a job-seeking worker. A rise in labor productivity raises the surplus from hiring $\tilde{\Psi}^j$; as a result, firms post more job vacancies which increases the labor market tightness $\tilde{\theta}^j$.

Second, using the fact that $\tilde{\xi}^j = \frac{\alpha_W^j}{1-\alpha_W^j}\tilde{\gamma}^j$, $\tilde{\gamma}^j + x^j = \frac{\kappa^j}{\tilde{f}^j}$ (as will be clear later, $x^T = 0$ and $x^N > 0$), $\frac{\tilde{m}^j}{\tilde{f}^j} = \tilde{\theta}^j$, to rewrite the reservation wage, the decision of search equation reads as (which holds for the traded sector and non traded sector):

$$\tilde{L}^j = \frac{\tilde{m}^j}{\tilde{m}^j + s^j}\left[\bar{\lambda}\left(\frac{\alpha_W^j}{1-\alpha_W^j}\kappa^j\tilde{\theta}^j + R^j\right)\right]^{\sigma_L^j}, \quad j = T, N, \tag{36}$$

where $\left(\frac{\alpha_W^j}{1-\alpha_W^j}\kappa^j\tilde{\theta}^j + R^j\right)$ corresponds to the reservation wage, $\tilde{W}_R^j$, reflecting the marginal benefit from search; note that we have eliminated $\tilde{U}^j$ from (13b) by using the fact that in the long-run the number of unemployed agents who find a job $\tilde{m}^j\tilde{U}^j$ and workers who lose their job $s^j\tilde{L}^j$ must equalize. According to (36), higher labor market tightness increases labor $\tilde{L}^j$ by raising the job-finding rate for the worker and thus the employment rate $\frac{\tilde{m}^j}{\tilde{m}^j+s^j}$. Moreover, for given $\bar{\lambda}$, the rise in the reservation wage $\frac{\alpha_W^j}{1-\alpha_W^j}\kappa^j\tilde{\theta}^j + R^j$ induces agents to supply more labor.

Third, setting $\dot{B} = 0$ into eq. (27), we obtain the market clearing condition for the traded good:

$$r^\star\tilde{B} + A^T\tilde{L}^T - \tilde{C}^T - \kappa^T\tilde{U}^T\tilde{\theta}^T - \kappa^N\tilde{U}^N\tilde{\theta}^N = 0, \tag{37}$$

where $\tilde{C}^T = C^T\left(\tilde{L}^N, \bar{\lambda}, A^N\right)$.

The system comprising eqs. (35)-(37) can be solved for the steady-state labor market tightness, employment, and traded bonds. All these variables can be expressed in terms of the labor productivity index A^j and the marginal utility of wealth, i.e., $\tilde{\theta} = \theta\left(A^T\right)$, $\tilde{L}^T = L^T\left(\bar{\lambda}, A^T\right)$, $\tilde{\theta}^N = \theta^N\left(\bar{\lambda}, A^N\right)$, $\tilde{L}^N = L^N\left(\bar{\lambda}, A^N\right)$, and $\tilde{B} = B\left(\bar{\lambda}, A^T, A^N\right)$.[30] Inserting first $\tilde{B} = B\left(\bar{\lambda}, A^T, A^N\right)$, and $\tilde{L}^j = L^j\left(\bar{\lambda}, A^N\right)$, the intertemporal solvency condition (34) can be solved for the equilibrium value of the marginal utility of wealth:

$$\bar{\lambda} = \lambda\left(A^T, A^N\right). \tag{38}$$

[30]Setting first $\dot{L}^j = 0$ into (11), inserting $\tilde{L}^j = L^j\left(\bar{\lambda}, A^j\right)$, one can solve for U^j; then the relationship $V^j = \theta^j U^j$ can be solved for the steady-state job vacancy in sector j.

3.7 Graphical Apparatus

Before turning to the derivation of steady-state effects of technological change biased toward the traded sector, we characterize the steady-state graphically. Because we restrict our attention on the long-run equilibrium, the tilde is suppressed for the purposes of clarity. The steady-state can be described by considering alternatively the labor market or the goods market.

When focusing on the goods market, the equilibrium can be characterized by two schedules in the $(y^T - y^N, p)$-space where we denote the logarithm in lower case. The steady state is summarized graphically in Figure 3(b).

Denoting by $\upsilon_{NX} \equiv NX/Y^T$ the ratio of net exports to traded output, combining the zero current account equation with (26) yields the goods market equilibrium (GME henceforth) schedule:[31]

$$\frac{Y^T\left(1-\upsilon_{NX}\right)}{Y^N} = \frac{C^T}{C^N}, \tag{39}$$

where $-\upsilon_{NX} = \upsilon_B - \upsilon_V^T - \upsilon_V^N$ and the allocation of aggregate consumption expenditure between traded and non traded goods follows from (15). Totally differentiating (39) and denoting the percentage deviation from its initial steady-state by a hat gives:

$$\left.\hat{y}^T - \hat{y}^N\right|^{GME} = \phi\hat{p} - \mathrm{d}\ln\left(1-\upsilon_{NX}\right). \tag{40}$$

According to (40), the GME-schedule is upward-sloping in the $(y^T - y^N, p)$-space with a slope equal to $1/\phi$. Following a rise in traded output relative to non traded output, the relative price of non tradables must appreciate to clear the goods market, and all the more so as the elasticity of substitution ϕ is smaller. The 45° dotted line allows us to consider two cases. When $\phi > 1$ ($\phi < 1$), the GME-schedule is flatter (steeper) than the 45° dotted line.

Assuming an elasticity of labor supply identical across sectors, i.e., $\sigma_L^j = \sigma_L$, so that the wealth effect does not impinge on the ratio of sectoral labor, denoting the steady-state unemployment rate in sector j by $u^j = \frac{s^j}{m^j+s^j}$ and the share of the surplus associated with a labor contract in the marginal benefit of search by $\chi^j = \frac{\frac{\alpha_W^j}{1-\alpha_W^j}\kappa^j\theta^j}{W_R^j}$, and totally differentiating (35) and (36), one obtains the labor market equilibrium (LME henceforth) schedule:

$$\left.\hat{y}^T - \hat{y}^N\right|^{LME} = -\Theta^N\hat{p} + \left(1+\Theta^T\right)\hat{a}^T - \left(1+\Theta^N\right)\hat{a}^N, \tag{41}$$

[31] Denoting by $\upsilon_B \equiv \frac{r^\star B}{Y^T}$ the ratio of interest receipts to traded output and $\upsilon_V^j \equiv \frac{\kappa^j V^j}{Y^T}$ the ratio of the cost of hiring in sector $j = T, N$ to traded output, the zero current account equation (37) implies $\upsilon_B - \upsilon_V^T - \upsilon_V^N = -\upsilon_{NX}$. While for simplicity purposes, we refer to υ_{NX} as the ratio of net exports to traded output, it also includes hiring expenditure, i.e., $NX \equiv Y^T - C^T = \mathsf{NX} + \kappa^T V^T + \kappa^N V^N$ with $\mathsf{NX} \equiv Y^T - C^T - \kappa^T V^T - \kappa^N V^N$ corresponding to the 'true' definition of the trade balance.

where we set[32]

$$\Theta^j \equiv \frac{\Xi^j \left(s^j + r^\star\right) \left[\alpha_V^j u^j + \sigma_L \chi^j\right]}{\Psi^j \left[\left(1-\alpha_V^j\right)\left(s^j + r^\star\right) + \alpha_W^j m^j\right]}, \tag{42}$$

in order to write expressions in a compact form. As depicted in Figure 3(b), the LME-schedule is downward-sloping in the $(y^T - y^N, p)$-space with a slope equal to $-1/\Theta^N$ (see eq. (41)). An appreciation in the relative price of non tradables raises the surplus from hiring which induces non traded firms to post more job vacancies. By raising the expected value of a job, the consecutive rise in the labor market tightness induces agents to increase the search intensity for a job in the non traded sector but less so as the elasticity of labor supply σ_L is lower. More precisely, lower values of σ_L indicate that workers experience a larger switching cost from one sector to another; in this configuration, the term Θ^j is smaller so that the LME-schedule is steeper. Conversely, when we let σ_L tend toward infinity, the case of perfect mobility of labor across sectors is obtained; in this configuration, the LME-schedule becomes a horizontal line.

< Please insert Figure 3 about here >

When focusing on the labor market, the model can be summarized graphically by two schedules in the $(l^T - l^N, \ln\left(\frac{\theta^T}{\theta^N}\right))$-space, as shown in Figure 3(a).

Using eq. (36) and setting $\sigma_L^j = \sigma_L$ yields the decision of search-schedule (DS henceforth):

$$\frac{L^T}{L^N} = \frac{m^T}{m^N}\frac{m^N + s^N}{m^T + s^T}\left(\frac{W_R^T}{W_R^N}\right)^{\sigma_L}, \tag{43}$$

where $W_R^j \equiv \frac{\alpha_W^j}{1-\alpha_W^j}\kappa^j\theta^j + R^j$ is the reservation wage. Totally differentiating (43) and assuming that $\alpha_V^j = \alpha_V$ and labor markets display similar features across sectors, i.e., $\chi^j \simeq \chi$, and $u^j \simeq u$ yields:

$$\left(\hat{\theta}^T - \hat{\theta}^N\right)\Big|^{DS} = \frac{1}{(\alpha_V u + \sigma_L \chi)}\left(\hat{l}^T - \hat{l}^N\right). \tag{44}$$

According to (44), the DS-schedule is upward-sloping in the $(l^T - l^N, \ln\left(\frac{\theta^T}{\theta^N}\right))$-space where the slope is equal to $\frac{1}{(\alpha_V u + \sigma_L\chi)}$. The reason is that a rise in the ratio of labor market tightness θ^T/θ^N increases the probability of finding a job in the traded sector relative to the non traded sector. Hence, a worker gets a larger share of the surplus associated with a labor contract via higher traded wage, and thereby is induced to supply more labor toward the traded sector.

[32]Totally differentiating (35) gives the deviation in percentage of the sectoral labor market tightness from its initial steady-state, i.e., $\hat{\theta}^j = \frac{\Xi^j}{\left[\left(1-\alpha_V^j\right)\Psi^j + \chi^j W_R^j\right]}\hat{\Xi}^j$. Totally differentiating (36) gives the deviation in percentage of sectoral labor from its initial steady-state, i.e., $\hat{l}^j = \left[\alpha_V^j u^j + \sigma_L\chi^j\right]\hat{\theta}^j$. Substituting the former into the latter, differentiating the production function $Y^j = A^j L^j$ to eliminate $\hat{l}^j$, and using the fact that $\chi^j W_R^j = \frac{\alpha_W^j \Psi^j}{s^j + r^\star}$ at the steady-state, one obtains $\hat{y}^j = \hat{a}^j + \Theta^j\hat{\Xi}^j$ where Θ^j is given by eq. (42).

As will be useful, we solve the goods market equilibrium (39) for the relative price of non tradables:

$$P = P\left[\left(\frac{L^T}{L^N}\right), (1-\upsilon_{NX}), \left(\frac{A^T}{A^N}\right)\right]. \tag{45}$$

Combining the vacancy creation schedule (35) and the number of matches per job vacancies (22) while assuming $\alpha_V^j = \alpha_V$, gives:

$$\frac{\kappa^T}{\kappa^N}\frac{(s^T+r^\star)}{(s^N+r^\star)}\frac{X^T}{X^N}\left(\frac{\theta^T}{\theta^N}\right)^{1-\alpha_V} = \frac{A^T + r^\star x^T - W_R^T}{P(.)\,A^N + r^\star x^N - W_R^N}. \tag{46}$$

where $P(.)$ is given by eq. (45). Totally differentiating (43) and assuming that labor markets initially display similar features across sectors, i.e., $\Xi^j \simeq \Xi$, $\Psi^j \simeq \Psi$, $\chi^j W_R^j \simeq \chi W_R$, yields:

$$\left(\hat{\theta}^T - \hat{\theta}^N\right)\Big|^{VC} = -\frac{\Xi\left(\hat{L}^T - \hat{L}^N\right)}{\phi\left[(1-\alpha_V)\,\Psi + \chi W_R\right]} + \frac{\Xi\left[(\phi-1)\left(\hat{A}^T - \hat{A}^N\right) - d\ln(1-\upsilon_{NX})\right]}{\phi\left[(1-\alpha_V)\,\Psi + \chi W_R\right]}. \tag{47}$$

According to (47), the VC-schedule is downward-sloping in the $(l^T - l^N, \ln\left(\frac{\theta^T}{\theta^N}\right))$-space where the slope is equal to $-\frac{\Xi}{\phi[(1-\alpha_V)\Psi+\chi W_R]}$. Intuitively, as hours worked are shifted toward the traded sector, non traded output declines relative to traded output; as a result, the relative price of non tradables must appreciate which encourages non traded firms to hire more workers; because the non traded sector posts more job vacancies, the ratio of labor market tightness θ^T/θ^N falls.

4 Relative Wage Adjustment and Labor Market Institutions

This section analyzes graphically and analytically the consequences on the relative wage and the relative price of an increase in relative sectoral productivity A^T/A^N. It compares the steady-state of the model before and after the productivity shock biased towards the traded sector. To shed light on the transmission mechanism, we analytically break down the relative wage and relative price effects in two components: a labor market frictions effect and a labor accumulation effect. Then we investigate how labor market institutions impinge on the relative wage adjustment.

4.1 Relative Wage and Relative Price Effects

We first explore the relative price effect of technological change biased toward the traded sector by equating demand (40) and supply (41) of tradables in terms of non tradables, both expressed in percentage deviation from its initial steady-state, to eliminate $\hat{y}^T - \hat{y}^N$. One obtains a relationship between the deviation in percentage of the relative price from its initial steady-state and the productivity growth differential between tradables and non tradables:

$$\hat{p} = \frac{(1+\Theta^T)\,\hat{a}^T - (1+\Theta^N)\,\hat{a}^N}{(\phi+\Theta^N)} + \frac{\mathrm{d}\ln(1-\upsilon_{NX})}{(\phi+\Theta^N)}, \tag{48}$$

where the term Θ^j given by eq. (42) is the elasticity of sectoral employment L^j w.r.t. the marginal revenue of labor Ξ^j. As will be clear later, Θ^j is a measure of the degree of labor mobility across sectors which captures both the size of workers' mobility costs and the extent of search frictions. In order to facilitate the discussion, we assume that $\Theta^j \simeq \Theta$.[33] Under this assumption, eq. (48) reduces to:

$$\hat{p} = \frac{(1+\Theta)\left(\hat{a}^T - \hat{a}^N\right)}{(\phi+\Theta)} + \frac{\mathrm{d}\ln\left(1-\upsilon_{NX}\right)}{\left(\phi+\Theta^N\right)}, \tag{49}$$

where $\mathrm{d}\ln\left(1-\upsilon_{NX}\right) \simeq -d\upsilon_{NX}$ by using a first-order Taylor approximation.

Eq. (49) breaks down the relative price response into two components: a labor market frictions effect and a labor accumulation effect. The first term on the RHS of eq. (49) corresponds to the labor market frictions effect. Through this channel, higher productivity growth in tradables relative to non tradables tends to appreciate the relative price. The reason is that technological change biased toward the traded sector raises traded output relative to non traded output so that the relative price of non tradables must increase to clear the goods market. Importantly, the size of the relative price appreciation is given by the elasticity $\frac{(1+\Theta)}{(\phi+\Theta)}$. When we let σ_L tend toward infinity, workers no longer experience a utility loss when shifting from one sector to another; hence the case of perfect mobility of labor across sectors is obtained as reflected by the term Θ that tends toward infinity; in this configuration, a 1 percentage point increase in the productivity differential between tradables and non tradables appreciates the relative price by 1% as well, in line with the prediction of the standard BS model.[34] Graphically, as shown in Figure 4(a), the LME-schedule is a horizontal line because the allocation of the labor force across sectors is perfectly elastic to the ratio of sectoral reservation wages. A productivity shock biased toward the traded sector shifts higher the LME-schedule which results in a relative price appreciation, from p_0 to p_{BS}, i.e., by the same amount as the productivity differential. The LME-schedule intercepts the 45° line at point BS'.

As long as $\sigma_L < \infty$, workers experience a mobility cost when moving from one sector to another; hence, the term Θ takes finite values while graphically, the LME-schedule is downward sloping in the $(y^T - y^N, p)$-space. In this configuration, the relative price of non tradables is jointly determined by technological and demand conditions. More precisely, the elasticity ϕ between traded and non traded goods in consumption plays a pivotal role in the determination of the relative price response. Graphically, technological change biased toward the traded sector shifts to the right the LME-schedule from LME_0 to LME_1: this shift corresponds to the labor market frictions effect. If $\phi > 1$, the GME-schedule is

[33] For the baseline calibration, while labor market parameters are allowed to vary across sectors Θ^T and Θ^N are very similar if not identical. It is only when the firing costs are important that Θ^T and Θ^N differ substantially.

[34] Formally, we have:

$$\lim_{\sigma_L \to \infty} \frac{(1+\Theta)}{(\phi+\Theta)} = 1.$$

flatter than the 45° line so that the intersection is at G'; since $p' < p_{BS}$, the relative price appreciates by less than the productivity differential between tradables and non tradables, in line with our empirical findings. Intuitively, when the elasticity is larger than one, households are willing to substitute traded for non traded goods so that a moderate (i.e., less than 1%) appreciation in the relative price is necessarily following a rise in the productivity differential (by 1 percentage point). Conversely, if $\phi < 1$, the relative price must appreciate more than proportionately (i.e., by more than 1%) following higher productivity of tradables relative to non tradables (by 1 percentage point). In this configuration, the GME-schedule is steeper that the 45° line so that the LME_1-schedule intercepts the GME-schedule at a point which lies to the north west of BS'. Hence, through the labor market frictions channel, a 1 percentage point increase in the productivity differential between tradables and non tradables appreciates the relative price of non tradables by less (more) than 1% if traded and non traded goods are substitutes (complements).

The second term on the RHS of eq. (49) reveals that technological change biased toward the traded sector also impinges on the relative price of non tradables by affecting net exports and hiring expenditure expressed as a share of traded output, as summarized by $d\upsilon_{NX}$. More precisely, through the labor accumulation channel, higher productivity growth in tradables relative to non tradables increases υ_{NX} which exerts a negative impact on the relative price by raising the demand for tradables in the long-run. Intuitively, higher labor productivity (i.e., a rise in A^j) raises the shadow value of an additional worker γ^j and thus induces firms in both sectors to hire more. Because job vacancies V^j are a jump variable, it overshoots on impact. Since hiring is a costly activity, recruiting expenditure rise substantially. While employment builds up, the open economy finances labor accumulation by running a current account deficit in the short-run. For the intertemporal solvency condition to hold, the decumulation of traded bonds must be offset by a steady-state increase in net exports. The combined effect of the improvement in the trade balance and permanently increased hiring expenditure has an expansionary effect on the demand for tradables which drives down the relative price of non tradables. Graphically, in terms of Figure 4(a), the labor accumulation channel shifts the GME-schedule to the right, regardless of the value of the elasticity of substitution between traded and non traded goods. It is worthwhile noticing that a change in υ_{NX} no longer impinges on the relative price p and thus the labor accumulation channel vanishes when we let σ_L tend toward infinity, i.e., if agents are not subject to switching costs from one sector to another.[35] In this case, the GME_1-schedule intercepts the LME_1-schedule at BS_1. Unlike, when $\sigma_L < \infty$, the intercept is at G_1 if $\phi > 1$. In this case, the relative price unambiguously appreciates by less than 1% following a 1 percentage point increase in the productivity differential between tradables and non tradables. While through the labor market frictions channel, $\hat{p} > 1\%$ if $\phi < 1$, the labor

[35]When $\sigma_L \to \infty$, the term $\frac{1}{\phi+\Theta}$ tends toward zero.

market accumulation channel exerts a negative impact on p, and all the more so the smaller the elasticity ϕ, as shown by the second term on the RHS of (49).

< Please insert Figure 4 about here >

We now explore the long-run response of the relative wage of non tradables to a productivity differential. To do so, we first totally differentiate the vacancy creation equation (35) that we substitute into the Nash bargaining wage (24) expressed in rate of change relative to the steady-state:[36]

$$\hat{w}^j = \Omega^j \hat{\Xi}^j, \quad \Omega^j \equiv \frac{\Xi^j}{W^j} \frac{\alpha_W^j \left[\left(1-\alpha_V^j\right)\left(s^j + r^\star\right) + m^j\right]}{\left[\left(1-\alpha_V^j\right)\left(s^j + r^\star\right) + \alpha_W^j m^j\right]} > 0, \tag{50}$$

where $\hat{\Xi}^T = \hat{a}^T$ and $\hat{\Xi}^N = \hat{p} + \hat{a}^N$. Calculating $\hat{\omega} \equiv \hat{w}^N - \hat{w}^T$ by using (50) and substituting (48) yields the deviation in percentage of the relative wage from its initial steady-state:

$$\hat{\omega} = \left\{ \Omega^N \left[\frac{\left(1+\Theta^T\right)\hat{a}^T + (\phi-1)\hat{a}^N}{\left(\phi+\Theta^N\right)} \right] - \Omega^T \hat{a}^T \right\} - \Omega^N \frac{\mathrm{d}\upsilon_{NX}}{\phi+\Theta^N}. \tag{51}$$

To facilitate the discussion, we assume that $\Theta^j \simeq \Theta$ and $\Omega^j \simeq \Omega$.[37] Under theses assumptions, eq. (51) reduces to:

$$\hat{\omega} = -\Omega \left[\frac{(\phi-1)}{\phi+\Theta}\left(\hat{a}^T - \hat{a}^N\right) + \frac{\mathrm{d}\upsilon_{NX}}{\phi+\Theta} \right]. \tag{52}$$

When assuming perfect mobility of labor across sectors, i.e., if we let σ_L tend toward infinity, we have $\Theta \to \infty$; hence eq. (52) shows that a productivity differential leaves unaffected the relative wage. Conversely, as long as workers experience a utility loss when shifting (i.e., assuming $\sigma_L < \infty$), technological change biased toward the traded sector impinges on the relative wage through two channels.

When keeping fixed υ_{NX}, eq. (52) reduces to $-\Omega\frac{(\phi-1)}{\phi+\Theta}\left(\hat{a}^T - \hat{a}^N\right)$. Hence, through the labor market frictions channel, higher productivity growth in tradables relative to non tradables lowers the relative wage ω only if $\phi > 1$. As discussed above, technological change biased toward the traded sector raises traded output relative to non traded output which appreciates the relative price of non tradables; with an elasticity of substitution ϕ greater than one, the demand for tradables rises more than proportionally. By raising the share of tradables in total expenditure, higher productivity growth in tradables relative to non

[36]Totally differentiating the wage rate W^j (24) gives:

$$\hat{w}^j = \frac{\alpha_W^j \Xi^j}{W^j}\hat{\Xi}^j + \left(1-\alpha_W^j\right)\frac{\chi^j W_R^j}{W^j}\hat{\theta}^j.$$

Totally differentiating the vacancy creation equation (35) to eliminate $\hat{\theta}^j$ in the above equation, and using the fact that at the steady-state, $\chi^j W_R^j = m^j \xi^j = \frac{m^j \alpha_W^j \Psi^j}{s^j + r^\star}$, one obtains (50).

[37]For the baseline scenario of our quantitative analysis, i.e., when calibrating to a typical OECD economy, Ω^T and Ω^N are almost identical.

tradables induces traded firms to hire more which lowers the relative wage. In terms of Figure 4(b), technological change biased toward the traded sector shifts to the right the VC-schedule from VC_0 to VC'. Unlike, with an elasticity ϕ smaller than one, the VC-schedule would shift to the left because the share of non tradables rises which has an expansionary effect on recruitment in the non traded sector. Hence, in this case, the relative wage of non tradables increases instead of declining, in contradiction with our empirical findings.

As captured by the second term on the RHS of eq. (52), technological change biased toward the traded sector also impinges on the relative wage through a labor accumulation channel. More specifically, by raising steady-state net exports, a productivity differential encourages traded firms to hire more which exerts a negative impact on the relative wage. Graphically, as depicted in Figure 4(b), higher productivity growth in tradables relative to non tradables shifts further to the right the VC-schedule from VC' to VC_1. Hence, while ω unambiguously declines if the elasticity of substitution is larger then one, when $\phi < 1$, the relative wage response to a productivity differential is ambiguous. In the latter case, technological change biased toward the traded sector drives down ω through the labor accumulation channel while it increases the relative wage through the labor market frictions channel. We address this ambiguity numerically later.

In our model, the elasticity of labor supply at the extensive margin, σ_L, plays a key role in the determination of the relative wage adjustment. When the labor force participation decision is endogenized, the situations of total immobility ($\sigma_L = 0$) and perfect mobility ($\sigma_L \to \infty$) of labor emerge as special cases. If we let $\sigma_L = 0$, the situation of total labor immobility is obtained. Because the mobility costs are prohibitive, the labor force F^j is fixed in both sectors. As will be clear later when discussing quantitative results, such a configuration reduces the likelihood that our model trustfully replicates our empirical findings. Graphically, in terms of Figure 4(b), setting $\sigma_L = 0$ rotates to the left the DS-schedule. Consequently, technological change biased toward the traded sector shifts the VC-schedule along a steeper DS-schedule. Consecutive large changes in the ratio of labor market tightness θ^T/θ^N amplify substantially the relative wage responses, thus diminishing the probability to replicate the size of the decline in ω found in the data.[38]

Conversely, when we let σ_L tend toward infinity, workers are no longer subject to switching costs; in this configuration, we have $\Theta^j \to \infty$ so that eq. (48) reduces to $\hat{p} = \left(\hat{a}^T - \hat{a}^N\right)$, as in the standard BS model. Inserting the relative price equation into $\hat{\Xi}^N = \hat{p} + \hat{a}^N$, the deviation in percentage of the relative wage from its initial steady-state (51) can be rewritten as $\hat{\omega} = \left(\Omega^N - \Omega^T\right)\hat{a}^T$. Such an equality reflects the fact that even if mobility costs are absent, technological change biased toward the traded sector may produce different sectoral

[38] It is worthwhile noticing that when $\sigma_L = 0$, the change in relative labor L^T/L^N is achieved through a decline in sectoral unemployment. For example, when $\phi > 1$, L^T/L^N unambiguously increases because more unemployed workers find a job in the traded sector while the labor force F^T is fixed.

wage responses because search parameters vary across sectors. However, the quantitative analysis conducted in section 5 reveals that the elasticity Ω^j of sectoral wages w.r.t. the marginal revenue of labor is almost identical across sectors (as long as firing costs are low), i.e., $\Omega^T \simeq \Omega^N$; hence, if $\sigma_L \to \infty$, we would have $\hat{\omega} \simeq 0$.

4.2 Implications of Labor Market Regulation

So far, we have shown that the relative wage of non tradables no longer remains fixed following technological change biased toward the traded sector because workers experience a mobility cost (as captured by $0 < \sigma_L < \infty$) which must be covered by higher wages. While searching for a job is costly because it is time consuming, in a model with search in the labor market, hiring is also a costly activity. By affecting the recruiting cost, labor market institutions determine the elasticity of labor demand to technological change. More precisely, the more labor demand in the traded sector increases relative to that in the non traded sector, the larger the decline in the relative wage of non tradables. In this section, our objective is to assess the ability of our model to account for our empirical findings established in section 2 according to which the relative wage falls more in countries where unemployment benefits are more generous, the worker bargaining power is larger or legal protection against dismissals is more stringent. Because the transmission mechanism varies according the type of labor market institution, we differentiate between the firing cost on the one hand, the generosity of the unemployment benefit scheme and the worker bargaining power on the other.

4.2.1 Implications of a Higher Firing Tax

In our model, the strictness of legal protection against dismissals is captured by a firing tax denoted by x^j paid to the State by the representative firm in the sector which reduces employment. Technological change exerts two opposite effects on labor L^j. On the one hand, by producing a positive wealth effect, as reflected by a fall in the shadow value of wealth $\bar{\lambda}$ (38), a higher productivity exerts a negative impact on employment by driving down labor supply (see (36)). On the other hand, by increasing the marginal revenue of labor, a rise in A^j induces firms to recruit more which pushes up labor. Because technological change is biased toward the traded sector, employment in the traded sector increases while labor in the non traded sector declines. According to (19), higher productivity induces non traded firms to post more job vacancies but less so as the firing tax is increased because the surplus from hiring rises by a smaller amount. Since labor demand in the non traded sector increases less in countries where the firing tax is higher, as reflected by a smaller rise in the labor market tightness θ^N, the relative wage of non tradables falls more.

The implications of a higher firing tax is depicted in Figure 5(a) where we assume an elasticity between traded and non traded goods in consumption ϕ larger than one. In this configuration, as mentioned previously, technological change biased toward the traded sector shifts to the right the VC-schedule. As highlighted in Figure 5(a), higher productivity growth in tradables relative to non tradables shifts further to the right the VC-schedule from VC' to VC'', thus resulting in a larger increase in θ^T/θ^N because hiring in the non traded sector which decumulates employment is limited by the firing tax. Consequently, the relative wage ω declines more, in line with our empirical findings, through a stronger labor market frictions effect. However, a higher firing tax also moderates the decline in the relative wage since net exports increase less. Intuitively, as recruiting expenditure are curbed by the firing tax, the productivity differential leads to a smaller current account deficit, thus moderating the necessary trade balance improvement.[39]

In terms of eq. (51), a higher firing tax (paid by non traded firms) lowers substantially the term Ω^N which is the elasticity of the non traded wage to the marginal revenue of labor.[40] The term in braces in eq. (51) which captures the labor market frictions channel is thus higher in absolute terms (or more negative) when $\phi > 1$. Conversely, when $\phi < 1$, the term in braces in eq. (51) becomes positive but smaller as the firing tax x is increased. As mentioned above, in countries where the firing tax is higher, net exports increase less which lowers $d\upsilon_{NX} > 0$ in the last term of eq. (51) and thus moderates the labor accumulation effect which exerts a negative impact on ω.[41]

In conclusion, increasing the firing tax exerts two opposite effects on the relative wage response to technological change biased toward the traded sector. On the one hand, higher productivity growth in tradables relative to non tradables produces a larger decline (if $\phi > 1$) or a smaller increase (if $\phi < 1$) in ω as x is raised by limiting the expansionary effect on labor demand in the non traded sector. On the other hand, increasing the firing tax moderates the expansionary effect of a productivity differential on the demand of tradables in the long-run (captured by $d\upsilon_{NX} > 0$) and thus the steady-state fall in the relative wage. We will address this ambiguity numerically.

4.2.2 Implications of a More Generous Unemployment Benefit Scheme or a Higher Worker Bargaining Power

In our framework, the generosity of the unemployment benefit scheme is captured by the level of R^j; unemployment benefits are assumed to be a fixed proportion r of the wage rate W^j, i.e., $R^j = rW^j$. Additionally, a higher worker bargaining power measured empir-

[39] Because our quantitative analysis shows that increasing substantially the firing tax merely affects the labor accumulation channel, for clarity purposes, we restrict our attention to the labor market frictions in Figure 5(a).

[40] A higher firing tax lowers both Ω^N and Θ^N which exerts opposite effects on the first term in braces in eq. (51). Our quantitative analysis indicates that the effect of a lower Ω^N on $\hat{\omega}$ predominates. For clarity purposes, we concentrate on this term while leaving aside the impact on Θ^N in order to avoid unnecessary complications.

[41] To be more precise, a higher firing tax lowers Ω^N and moderates the change in net exports $d\upsilon_{NX} > 0$ which exert opposite effects on $\hat{\omega}$, as shown by the last term in eq. (51); our quantitative analysis reveals that the firing tax tends to moderate the labor accumulation effect.

ically by the bargaining coverage is captured by the parameter α_W which is assumed to be identical across sectors.

In contrast to a firing tax, raising the unemployment benefit replacement rate or the worker bargaining power leads to a larger long-run rise in net exports and thus amplifies the decline in the relative wage through the labor accumulation channel. The reason is as follows. In countries where unemployment benefits are more generous or the worker bargaining power is larger, there are more job-seeking workers and less job vacancies, thus resulting in lower labor market tightness θ^j in both sectors. Consequently, following higher productivity, firms are more willing to recruit additional workers because hiring is more profitable as the probabilities of fulfilling vacancies (f^j) are much higher. Hence, the open economy experiences a larger current account deficit along the transitional path which must be matched in the long-run by a greater improvement in the balance of trade. By amplifying the rise in net exports and thus the demand for tradables, technological change biased toward the traded sector exerts a larger negative impact on the relative wage in countries with a higher replacement rate r or a larger worker bargaining power α_W. While a productivity differential lowers further the relative wage through the labor accumulation channel, it also moderates its decline through the labor market frictions channel. More precisely, larger values of r, by reducing the cost of hiring (because the probability f^j is higher), or higher values of α_W, by raising the marginal benefit of search, increase the mobility of labor across sectors (captured by Θ^j) which in turn moderates the change in the relative wage through the labor market frictions channel.

The implication of a higher replacement rate r or a larger worker bargaining power α_W is depicted in Figure 5(b) where we consider an elasticity of substitution ϕ larger than one. Figure 5(b) shows that technological change biased toward the traded sector shifts further to the right the VC-schedule from VC_1 to VC_2 in countries where the replacement rate r is higher or the worker bargaining power α_W larger. As mentioned above, the larger increase in net exports amplifies the expansionary effect on hiring in the traded sector which pushes up further the ratio of labor market tightness θ^T/θ^N. Hence, the relative wage of non tradables falls more through a stronger labor accumulation effect. Raising r or α_W also modifies the labor market frictions channel by increasing the mobility of labor across sectors.[42] Because we find numerically that modifying r or α_W merely modifies the relative wage response to technological change biased toward the traded sector through the labor market frictions channel, we restrict our attention to the labor accumulation channel in

[42] In countries with a higher worker bargaining power α_W, firms are willing to recruit more (because it is relatively less costly due to a higher probability to fill a job vacancy) while workers are less reluctant to move from one sector to another (since they receive a larger share χ of the surplus associated with a labor contract in the marginal benefit of search). In economies with a more generous unemployment benefit scheme, while workers are more reluctant to move from one sector to another (because χ falls), the vacancy creation is more elastic to technological change. Since the latter effect predominates, the labor mobility rises.

Figure 4(b).

< Please insert Figure 5 about here >

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5 Quantitative Analysis

In this section, we analyze the effects of a labor productivity differential quantitatively. For this purpose we solve the model numerically.[43] Therefore, first we discuss parameter values before turning to the long-term consequences of higher productivity in tradables relative to non tradables.

5.1 Calibration

To calibrate our model, we estimated a set of parameters so that the initial steady state is consistent with the key empirical properties of a representative OECD economy. While at the end of the section we move a step further and calibrate the model for each economy, we first have to evaluate the ability of the two-sector open economy model with labor market frictions to accommodate the decline in the relative wage. Our sample covers the eighteen OECD economies in our dataset. Since we calibrate a two-sector model with labor market frictions, we pay particular attention to match the labor market differences between the two sectors. To do so, we carefully estimate a set of sectoral labor market parameters shown in Table 10. Unemployment benefit replacement rates and the firing cost shown in the latter two columns of Table 10 correspond to averages over 1980-2007 (except Korea: 2001-2007) and 1980-2005, respectively.[44] Because we consider an open economy setup with traded and non traded goods, we calculate the non-tradable content of employment, consumption, and government spending, and the productivity in tradables in terms of non tradables, for all countries in our sample, as summarized in Table 7. Our reference period for the calibration of the non tradable share given in Table 7 is running from 1990 to 2007 while labor market parameters have been computed over various periods due to data availability. We choose the model period to be one month and therefore set the world interest rate, $r^\star$, which is equal to the subjective time discount rate, β, to 0.4%.

We start with the values of the labor market parameters which are chosen so as to match a typical OECD economy.[45] Some of the values of the labor market parameters

[43] Technically, the assumption $\beta = r^\star$ requires the joint determination of the transition and the steady state.

[44] To calibrate the labor market for the traded and the non traded sector, we need to estimate the job finding and the job destruction rate for each sector. To do so, we apply the methodology developed by Shimer [2012]. Appendix B.2 presents the source and construction of the data while more details about the measures of the job finding probability for unemployed workers and the exit probability for employed workers can be found in the Technical Appendix.

[45] Due to the availability of data, we were able to estimate sectoral unemployment rates for 10 European countries and 5 OECD economies as ILO does not provide series for sectoral employment and unemployment

can be taken directly from data, but others need to be endogenously calibrated to fit a set of labor market features. To capture the labor market of a typical OECD economy which is chosen as the baseline scenario, we take unweighed average values shown in the last line of Table 10. We set the matching efficiency in the traded (non traded) sector X^T (X^N) to 0.307 (0.262) and the job destruction rate s^T (s^N) to 1.48% (1.54%) to target an unemployment rate u^T (u^N) of 7.9% (8.3%) and a monthly job finding rate m^T (m^N) of 17.4% (17.0%). We obtain an overall unemployment rate u of 8.1% in line with our estimate shown in Table 10. To target the labor market tightness in the traded sector, $\theta^T = 0.24$, and in the non traded sector, $\theta^N = 0.34$, we set the share of recruiting costs in GDP to 2.3% by choosing $\kappa^T = 1.482$ and $\kappa^N = 0.575$. In the numerical analysis, we assume that unemployment benefits are a fixed proportion of the wage rate, i.e., $R^j = rW^j$, with r the replacement rate. The unemployment benefit replacement rate has been set to 52.4%, in line with our estimates shown in Table 10.

Because the features of labor markets vary substantially across OECD economies, we also analyze two different calibrations of the model, one aimed at capturing the U.S. labor market, the other aimed at capturing Europe with its more 'rigid' labor market. To calibrate a typical European labor market, we take the EU-12 unweighed average.[46] For both calibrations, we present the implications of a productivity differential. To capture the U.S. (EU-12) sectoral labor markets, we set the matching efficiency parameters X^T and X^N to 0.620 (0.231) and 0.521 (0.197), respectively and the job destruction rates s^T and s^N to 2.2% (1.2%) and 2.4% (1.2%), to target an unemployment rate in the traded sector u^T and in the non traded sector u^N of 4.8% (8.7%) and 5.3% (9.3%), respectively, and a monthly job finding rate m^T in the traded sector and in the non traded sector m^N of 44.4% (12.4%) and 44.0% (12.2%), respectively, in line with the data shown in Table 10. It is worth noting that this allows us to match the unemployment rate for the US and EU-12 which averages 5.2% and 9.1%. Furthermore, the replacement rate has been set to 26.1% for the U.S. and 55.9% for EU-12. To target the sectoral labor market tightness for the US (EU-12), i.e., $\theta^T = 0.43$ ($\theta^T = 0.21$) and $\theta^N = 0.65$ ($\theta^N = 0.30$), respectively, we choose $\kappa^T = 1.333$ ($\kappa^T = 1.535$) and $\kappa^N = 0.476$ ($\kappa^N = 0.597$).

Using U.S. data, Barnichon [2012] reports an elasticity of the matching function with respect to unemployed workers of about 0.6, an estimate which lies in the middle of the plausible range reported by Petrongolo and Pissarides [2001]. Hence, we set the elasticity $1 - \alpha_V^j$ (with $j = T, N$) of the matching function with respect to unemployed workers to 0.6.[47] As it is common in the literature, we impose the Hosios [1990] condition, and set

for France, the Netherlands, and Norway at a sectoral level. Regarding Korea, while ILO provides data necessary for the computation of sectoral unemployment rates, the OECD does not provide unemployment by duration for this country which prevents the computation of job finding and job destruction rates.

[46] For sectoral unemployment rates, and monthly job finding and job destruction rates, we take the EU-10 unweighed average due to data availability.

[47] Due to the lack of empirical estimates at a sectoral level, we assume $1-\alpha_V^j$ to be identical across sectors.

the worker bargaining power α_W to 0.6 in the baseline scenario but conduct a sensitivity analysis with respect to this parameter by setting α_W to 0.9 while keeping fixed $1 - \alpha_V$.

We model firing costs as a tax that firms have to pay to the State when their employment levels decline, i.e., if $\dot{L}^j < 0$. To calibrate the firing cost, we take data from Fondazione De Benedetti which provides series for the eighteen countries of our sample over the period 1980-2005. To compute the firing tax, we add the advance notice and the severance payment which are averages after 4 and 20 years of employment. Since the advance notice and the severance payment are both expressed in monthly salary equivalents, we have $x^j = \tau W^j$ with $\tau \geq 0$. Values of τ are shown in the last column of Table 10. For the baseline calibration, we set the firing tax τ to 4.2.[48] When calibrating to the US (EU-12) economy, we set $\tau = 0$ ($\tau = 4.3$).

Next, we turn to the elasticity of labor supply at the extensive margin which is assumed to be symmetric across sectors. We choose σ_L to be 0.6 in our baseline setting but conduct a sensitivity analysis with respect to this parameter.[49] Furthermore, in order to target a non tradable content of labor of 66% which corresponds to the 18 OECD countries' unweighted average shown in the last line of Table 7, we set ζ^T to 1 and ζ^N to 0.18 (see eq. (10)).

We now turn to the calibration of consumption-side parameters that we use as a baseline. In light of our discussion above, besides country's labor market regulation, ϕ plays a key role in the determination of the relative wage and relative price responses to a productivity differential. Building on our panel data estimations, we set the elasticity of substitution to 1 in the baseline calibration.[50] But we conduct a sensitivity analysis by considering alternatively a value of ϕ smaller or larger than one (i.e., ϕ is set to 0.6 and 1.5, respectively).[51] The weight of consumption in non tradables $1 - \varphi$ is set to 0.42 to target a non-tradable content in total consumption expenditure (i.e. α_C) of 42%, in line with the average of our estimates shown in the last line of Table 7. The intertemporal elasticity of substitution for consumption σ_C is set to 1.

For calibration purposes, we introduce government spending on traded and non traded

[48] As mentioned previously, because traded employment monotonically increases while the non traded sector reduces continuously employment following a productivity differential, only the non traded sector is subject to the firing tax.

[49] Using data from the Panel Study of Income Dynamics, Fiorito and Zanella [2012] find that aggregate time-series results deliver an extensive margin elasticity in the range 0.8-1.4, which is substantially larger than the corresponding estimate (0.2-0.3) reported by Chetty, Friedman, Manoli, and Weber [2011]. Using Japanese data, Kuroda and Yamamoto [2008] report a Frisch elasticity on the extensive margin which falls in the range of 0.6 to 0.8 for both sexes. By calibrating a model with endogenous participation decision, Haefke and Reiter [2011] find labor supply elasticities for the baseline case of 0.4 and 0.65 for men and women, respectively.

[50] Excluding estimates of ϕ for Italy which are negative (see Table 8), column 1 of Table 6 reports consistent estimates for the elasticity of substitution ϕ between traded and non traded goods which average to 0.9. The advantage of setting ϕ to 1 in the baseline scenario is twofold. First, the share of non traded goods in consumption expenditure α_C coincides with the weight of the non traded good in the overall consumption bundle $1 - \varphi$ if $\phi = 1$. Second, setting $\phi = 1$ implies that only the labor accumulation channel is (mostly) in effect as the labor market frictions channel almost totally vanish which allows us to highlight the intertemporal effect trigged by the hiring boom.

[51] These values for ϕ of 0.6 and 1.5 correspond roughly to the averages of estimates of ϕ for countries with $\phi < 1$ and $\phi > 1$, respectively.

goods in the setup.[52] We set G^N and G^T so as to yield a non-tradable share of government spending of 90%, and government spending as a share of GDP of 20%. Close to the averages of the values reported in the last line of Table 7, the ratios G^T/Y^T and G^N/Y^N are 4% and 35% in the baseline calibration.

We consider a permanent increase in the productivity index A^j of both sectors biased towards the traded sector so that the labor productivity differential between tradables and non tradables, i.e., $\hat{a}^T - \hat{a}^N$, is 1%. While in our baseline calibration we set $\phi = 1$, $\sigma_L = 0.6$, $\alpha_W = 0.6$, $r = 0.524$, $\tau = 4.2$, we conduct a sensitivity analysis with respect to these five parameters by setting alternatively: ϕ to 0.6 and 1.5, σ_L to 0, 0.2 and 1, α_W to 0.9, r to 0.782, and τ to 13.[53] Finally, in the latter two columns of Table 5, we compare the results for the US economy with those obtained for a typical European economy (EU-12).

5.2 Discussion

Before analyzing in the detail the role of labor market frictions in shaping the long-run dynamics of the relative price and the relative wage in response to technological change biased toward the traded sector, we recall the set of observations established in section 2. For the whole sample, our empirical findings indicate that a productivity differential of 1% lowers the relative wage by 0.22%. When performing a sample-split analysis, estimates reveal that the relative wage falls more in countries where the labor market regulation is more pronounced. We also find that the elasticity of the relative price with respect to the relative productivity is equal to 0.64 for the whole sample.

The relative wage and relative price responses are summarized in Table 5. Since the relative wage response is ambiguous when the elasticity of substitution is smaller than one, it is convenient to first discuss the numerical results in this configuration. Panels C and D of Table 5 report the long-run changes for the relative wage W^N/W^T and the relative price of non traded goods P^N/P^T expressed as a percentage. The numbers reported in the first line of each panel give the (overall) responses of these variables to 1 percentage point increase in the productivity differential between tradables and non tradables. Column 1 of Table 5 shows that when abstracting from labor market frictions, i.e., setting $\kappa^j = 0$ and $\sigma_L \to \infty$, the model cannot account for our empirical evidence. Intuitively, because hiring and searching for a job are costless activities, labor is perfectly mobile across sectors. Hence, technological change biased toward the traded sector leaves unaffected the relative wage (i.e., $\hat{\omega} = 0$). Since the non tradable unit labor cost increases at the same speed as the productivity differential, the relative price appreciates by 1%.

[52] The market clearing condition for the traded good and the non traded good at the steady-state are $r^{\star}B + Y^T = C^T + G^T + \kappa^T V^T + \kappa^N V^N$ and $Y^N = C^N + G^N$.

[53] When conducting the sensitivity analysis, we raise r from 52.4% to 78.2% and τ from 4.2 to 13, which correspond to the highest value in our sample of countries for the replacement rate and the firing cost, respectively.

Conversely, numerical results summarized in column 2 show that when calibrating to a typical OECD economy, a model with labor market frictions can produce a decline in ω and a less than proportional increase in the relative price as found in the data. To shed light on the transmission mechanism of technical change biased toward the traded sector in a model with labor market frictions, it is useful to numerically break down the responses into two channels; i) a labor market frictions channel stemming from the effect of higher productivity on hiring while keeping the trade balance fixed and ii) a labor accumulation channel arising from the long-run rise in net exports.

As shown in the second line of panels C and D, a rise by 1% in the productivity of tradables relative to non tradables raises the relative wage by 0.29% and appreciates the relative price by 1.33% through the labor market frictions effect. Intuitively, a productivity shock biased toward the traded sector increases traded output relative to non traded output, thus requiring a rise in the relative price to clear the goods market. Because ϕ is smaller than one, the relative price must appreciate more than proportionately which in turn raises the share of non tradables into expenditure and thus encourages non traded firms to recruit relatively more than traded firms. To attract workers who experience mobility costs when shifting, the non traded wage must rise relative to the traded wage. As shown in the third line of panels C and D, the labor accumulation effect counteracts the labor market frictions effect. More specifically, technological change biased toward the traded sector also raises net exports which has an expansionary effect on hiring in the traded sector, thus driving down the relative wage by 0.45%. Higher demand for tradables also depreciates the relative price by 0.47%. Importantly, the labor accumulation effect more than offsets the labor market frictions effect so that the relative wage declines by 0.16% and the relative price appreciates by 0.85%, as summarized in the first line of panels C and D.

Our model with search in the labor market and an endogenous labor force participation sheds light on two sets of factors influencing the mobility of labor across sectors and thus the relative wage response to a productivity differential: the workers' mobility cost reflected by a utility loss when increasing the search intensity for a job in one sector (as captured by σ_L) and labor market institutions (captured by α_W, r, τ) determining the elasticity of hiring to labor productivity. While columns 3 to 5 explore the consequences of the workers' mobility cost, columns 6 to 8 investigate the implications of stringent labor market regulation.

As we move from column 3 to column 5, the elasticity of labor supply at the extensive margin σ_L is raised from zero to 1 so that the workers' utility loss decline. Column 3 of panels C and D of Table 5 shows numerical results if labor is totally immobile across sectors as captured by setting $\sigma_L = 0$. In this configuration, the labor force is fixed in both sectors because the mobility cost is prohibitive. Since the decision of search is inelastic to the sectoral wage, the relative wage falls by 0.48% instead of 0.16% in the baseline scenario.

Hence, such a polar case tends to substantially overstate the decline in the relative wage and thus confirms the pivotal role of an endogenous labor force participation decision. Columns 4 and 5 of panels C and D of Table 5 analyze the effect of raising the elasticity of labor supply at the extensive margin from 0.2 to 1. Because the utility loss induced by the shift from one sector to another is lowered, the decline in the relative wage is moderated, as shown in the first line of panel C. Because the shift of labor from the non traded to the traded sector is increased, traded output rises more relative to non traded output, thus raising the appreciation in the relative price from 0.82% to 0.88%, as displayed in the first line of panel D.

Scenarios summarized in columns 6 and 7 of Table 5 show that raising the worker bargaining power α_W or the unemployment benefit replacement rate r amplifies the decline in the relative wage from 0.16% to 0.21% and 0.25%, respectively. In accordance with our model's predictions, in countries with a higher worker bargaining power or providing more generous unemployment benefits, technological change biased toward the traded sector lowers more the relative wage through the labor accumulation effect, as shown in the third line of panel C. The reason is that the elasticity of hiring to technological change is higher since the labor market tightness is initially low in both sectors. Hence, job vacancies increase substantially following a productivity shock. Higher recruiting expenditure produce larger current account deficits along the transitional paths. Consequently, net exports must rise more for the intertemporal solvency condition to hold, thus resulting in a greater expansionary effect on labor demand in the traded sector and thereby on traded wages. The stronger labor accumulation effect also moderates the appreciation in the relative price from 0.85% to 0.81% and 0.76%, as shown in the first line of panel D, because the demand for tradables increases more than in the baseline scenario. The second line of panel C also reveals that the relative wage increases less than in the baseline scenario through the labor market frictions effect. Intuitively, raising the worker bargaining power or the replacement rate increases the mobility of labor across sectors by raising the marginal benefit of search or reducing the recruiting cost (as the labor market tightness is initially low), respectively.

Column 8 of Table 5 gives results when the firing cost is about three times larger than in the baseline scenario. In accordance with our empirical findings, raising the firing cost drives down further the relative wage from -0.16% to -0.19%. As shown in the third line of panel C, the labor accumulation channel is merely affected by the firing cost. On the contrary, the second line of panel C reveals that the relative wage increases by a smaller amount because the firing cost curbs the expansionary effect of technological change on hiring by non traded firms and thus moderates the rise in the non traded wage relative to the traded wage from 0.29% to 0.25%. Moreover, as shown in the first line of panel D, countries with stringent legal protection against dismissals also experience a larger appreciation in the relative price of non tradables because traded output increases more relative to non traded output.

The latter two columns of Table 5 compare the relative wage and relative price effects of technological change biased toward the traded sector between a typical European country and the US. Because the legal protection against dismissals is stricter while unemployment benefits are higher, a typical European economy experiences a smaller increase in the non traded wage through the labor market frictions channel and a larger increase in the traded wage through the labor accumulation channel. As a result, the relative wage falls by 0.20% in EU-12 and declines by only 0.09% in the US. While a higher firing cost tends to amplify the appreciation in the relative price, a larger replacement rate tends to moderate it. The first line of panel D shows that the latter effect dominates so that a productivity differential raises the relative price of non tradables more in the US (0.90%) than in a European economy (0.82%).

We briefly discuss the scenario of an elasticity of substitution between traded and non traded goods larger than one. Panels E and F of Table 5 report the relative wage and relative price long-run responses to a productivity differential between tradables and non tradables of 1%. Because the labor accumulation channel reinforces the labor market frictions channel, the first line of panel E reveals that the model tends to overstate the decline in the relative wage when $\phi > 1$. Since in this configuration, a productivity differential of 1% appreciates the relative price less than proportionately through the labor market frictions effect while the rise in net exports depreciates p, the model tends to understate the rise in p, as shown in the first line of panel F.

Finally, we explore the relative wage and relative price effects when the elasticity of substitution between tradables and non tradables is set to one. This case is shown in panel A and panel B of Table 5. Keeping fixed net exports, higher productivity growth in tradables relative to non tradables would have no effect on the relative wage while the relative price would appreciate by 1% if labor market parameters were identical because the share of tradables in total expenditure remains unchanged. As shown in the second line of panel A, the relative wage falls very slightly though because the elasticity of hiring in the traded sector is merely higher than that in the non traded sector. The third line of panel A and B reveals that technological change biased toward the traded sector lowers substantially the relative wage and produces an appreciation in the relative price close to our estimates due to the improvement in the balance of trade. Alternative scenarios yield similar results to those discussed above and therefore do not warrant further comment.

< Please insert Table 5 about here >

5.3 Taking the Model to the Data

We now move a step further and compare the predicted values with estimates for each country and the whole sample. To do so, we use the same baseline calibration for each country, except for the elasticity of substitution ϕ between traded and non-traded goods, and labor market parameters which are allowed to vary across countries. More specifically, the elasticity of substitution ϕ between traded and non traded goods is set in accordance with its estimates shown in the first column of Table 6.[54] The parameters which capture the degree of labor market regulation such as the firing cost x, and the replacement rate r are set to their values shown in the latter two columns of Table 10. The job destruction rate s^j, and the matching efficiency X^j in sector j are set to target the unemployment rate u^j and the job finding rate m^j summarized in columns 2, 3, and in columns 5, 7 of Table 10. The costs per job vacancy κ^T and κ^N are chosen to target the aggregate labor market tightness θ shown in column 13 and the ratio of sectoral labor market tightness θ^T/θ^N obtained by dividing column 10 by column 11.[55]

Results are shown in Table 6. Columns 2 and 5 of Table 6 give the predicted responses of $\hat{\omega}$ and $\hat{p}$ to a productivity differential between tradables and non tradables by 1%. Columns 3 and 6 report FMOLS estimates of $\hat{\omega}$ and $\hat{p}$ for each country, EU-12 and the whole sample.[56] Columns 4 and 7 give the difference between the actual and the predicted values. Column 4 reveals that our model's predictions for $\hat{\omega}$ are relatively close to the evidence for almost half of the countries in our sample, including France, the UK, Ireland, Italy, Japan, the Netherlands, Spain and the United States, and to a lesser extent Germany, Austria and EU-12. The model predicts fairly well the relative price response for nine countries of our sample, including Austria, Belgium, Germany, Finland, Italy, Japan, the Netherlands, Spain, and the UK. The prediction error is also moderate in Denmark and France. It is worthwhile mentioning that, whether we focus on the relative wage or the relative price, the prediction error is large for Australia, Canada, and Norway which are important natural

[54] We also choose the weight of consumption in non tradables $1-\varphi$ to target a non-tradable content in total consumption expenditure (i.e., α_C) for each country in line with our estimates shown in column 2 of Table 7.

[55] Ideally, the recruiting cost κ^j would be set in order to target θ^j; however, the series for job vacancies by economic activity are available for a maximum of seven years. On the contrary, the OECD provides data for job openings (for the whole economy) over the period 1980-2007 allowing us to calculate the labor market tightness, i.e., $\theta = V/U$, for several countries that we target along with the ratio θ^T/θ^N by choosing κ^T and κ^N. When data for sectoral labor market tightness are not available, we target the average value θ^T/θ^N for EU-12 if the country is a member of the European Union, the average value for the US for English-speaking countries (excluding European economies), and average value for the OECD otherwise. When data for job openings are not available at an aggregate level, we first calibrate the model to EU-12 (US, OECD), in particular choosing κ^T and κ^N to target an aggregate labor market tightness θ of 0.12 (0.59, 0.18) and a ratio θ^T/θ^N of 0.75 (0.66, 0.77); then, we set κ^T and κ^N chosen for EU-12 if the country is a member of the European Union, chosen for the US for Canada, and chosen for the OECD otherwise. Finally, because labor market parameters cannot be calculated at a sectoral level for France, the Netherlands and Norway, we assume that the job destruction rate s and the matching efficiency X are identical across sectors and are chosen so as to target $u = u^j$ and $m = m^j$ shown in columns 4 and 5 of Table 10.

[56] FMOLS and DOLS cointegration procedures give very similar estimates. Since the model has been calibrated by using FMOLS estimates of ϕ, we compare predicted values with FMOLS estimates. We reach similar conclusions when using DOLS estimates.

resources exporters. Hence, for these three economies, we believe that our assumption of given terms of trade is too strong.

When calibrating to the whole sample, the model predicts remarkably well the relative wage response to a 1 percentage point increase in the productivity differential; more precisely, we find numerically a decline in the relative wage of 0.229% while in the data, ω falls by 0.223%. When we turn to the relative price, the prediction error increases substantially as our model produces an appreciation of 0.783% while we find empirically a rise of 0.636%.

< Please insert Table 6 about here >

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6 Conclusion

While the literature exploring the implications of technological change biased toward the traded sector commonly assume frictionless labor markets, our empirical results show that the non traded wage tends to decline relative to the traded wage. More specifically, using a sample of eighteen OECD countries over the period 1970-2007, we find that a rise in the productivity of tradables relative to non tradables by 1% lowers the relative wage of non tradables by 0.22%. Because the non traded wage increases at a lower speed than the traded wage, it is found empirically that the relative price of non tradables appreciates by 0.64% only instead of 1% as predicted by the standard neoclassical model abstracting from labor market frictions. When estimating the relative wage response by country, we conjecture that the large cross-country variations found in the data is the result of labor market institutions. In accordance with our interpretation, using a set of three indicators, our findings reveal that countries with stringent legal protection against dismissals, a more generous unemployment benefit scheme, or a higher bargaining coverage experience a significantly larger decline in the relative wage following higher productivity in tradables relative to non tradables.

To account for the evidence, we develop a two-sector open economy model with search in the labor market and an endogenous sectoral labor force participation decision. As in Alvarez and Shimer [2011], workers cannot reallocate hours worked from one sector to another without searching for a job in this sector. Because such an activity is costly in utility terms, workers experience a switching cost. We find analytically that two sets of parameters play a pivotal role in the determination of the relative wage response to technological change biased toward the traded sector: i) preference parameters such as the elasticity of labor supply at the extensive margin and the elasticity of substitution in consumption between tradables and non tradables, ii) parameters capturing the 'rigidities' in the labor market such as the firing tax, the unemployment benefit replacement rate and the worker bargaining power. Our quantitative analysis indicates that higher productivity growth in tradables relative to non tradables lowers the relative wage across all scenarios as long as the elasticity of labor supply that measures the workers' mobility cost takes a finite value. On the contrary, the situations of total immobility or perfect mobility of labor across sectors that emerge as special cases cannot account for the evidence. Importantly, the relative wage falls by a larger amount when raising the replacement rate or the worker bargaining power because traded firms are encouraged to hire more, thus amplifying the rise in the traded wage. Increasing the firing cost curbs hiring in the non traded sector, and thus produces a larger decline in the relative wage, in accordance with our evidence.

The final exercise we perform is to compare the responses of the relative wage and the relative price for each OECD economy in our sample to our empirical estimates. To do so, we estimate the elasticity of substitution in consumption between tradables and non tradables and the labor market parameters for each country. Allowing these two sets of pivotal parameters to vary across countries, it is found that the model predicts the adjustment of the relative wage fairly well for the whole sample and half of the countries and to a lesser extent the response of the relative price.

To conclude, our paper emphasizes that workers' switching costs and labor market institutions jointly determine mobility frictions which are key to understanding the adjustment of an open economy. While we have restricted our attention to the analysis of the effects of technological change biased toward the traded sector, OECD countries have been subject to a product market deregulation episode on an unprecedented scale over the last thirty years. Such deregulation has mainly affected non traded sectors and thus has contributed to lower the markup and stimulate employment in these industries, as documented by Bertinelli et al. [2013]. We believe that more work should be done in the future in order to disentangle quantitatively the implications of technological change and deregulation for sectoral wages, prices and labor reallocation across sectors.

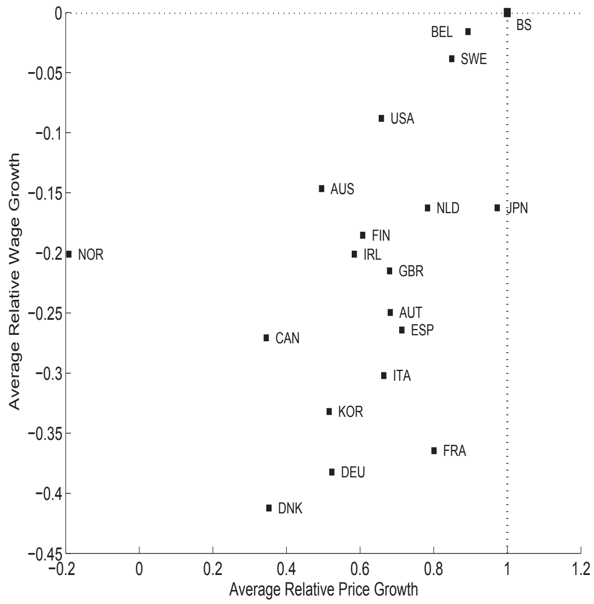


Figure 1: The Relative Price and the Relative Wage Growth. Notes: Figure 1 plots the annual average growth of the relative price of non tradables and the relative wage of non tradables, both scaled by the average productivity growth differential between tradables and non tradables, for each country of our sample over 1970-2007.

Table 1: Panel Unit Root Tests (p-values)

Test	Stat	Variables			
		ω	p	$a^T - a^N$	$p - (a^T - a^N)$
Levin et al. [2002]	t-stat	0.075	0.376	0.998	0.510
Breitung [2000]	t-stat	0.273	0.667	0.760	0.124
Im et al. [2003]	W-stat	0.558	1.000	1.000	0.999
Maddala and Wu [1999]	ADF	0.329	0.972	1.000	0.950
	PP	0.289	0.953	0.999	0.983
Hadri [2000]	Z_μ-stat	0.000	0.000	0.000	0.000

Notes: For all tests, except for Hadri [2000], the null of a unit root is not rejected if p-value $\geq$ 0.05 at a 5% significance level. For Hadri [2000], the null of stationarity is rejected if p-value $\leq$ 0.05 at a 5% significance level.

Table 2: Panel Cointegration Estimates of β and γ for the Whole Sample (eqs. (7))

	Relative wage eq. (7a)		Relative price eq. (7b)	
	DOLS	FMOLS	DOLS	FMOLS
$(a^T - a^N)$	-0.223^a (-29.72)	-0.223^a (-33.85)	0.646^a (76.543)	0.636^a (83.01)
$t(\beta) = 0$	0.000	0.000		
$t(\gamma) = 1$			0.000	0.000
Number of countries	18	18	18	18
Number of observations	680	680	680	680

Notes: all regressions include country fixed effects. Heteroskedasticity and autocorrelation consistent t-statistics are reported in parentheses. ^{a} denotes significance at 1% level. The rows $t(\beta) = 0$ and $t(\gamma) = 1$ report the p-value of the test of $H_0 : \beta = 0$ and $H_0 : \gamma = 1$ respectively.

Table 3: Panel Cointegration Estimates of β_i and γ_i for Each Country (eqs. (7))

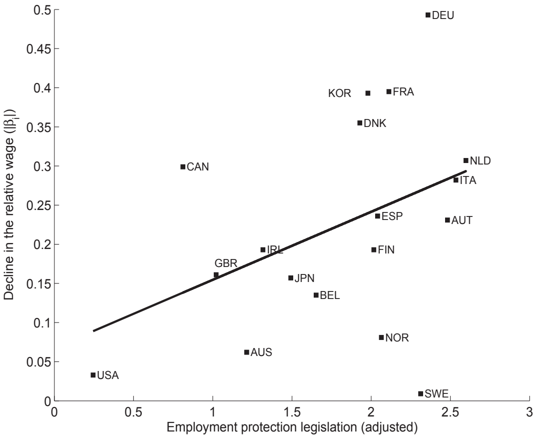
Country	Relative wage equation $\hat{\beta}_i^{DOLS}$	$\hat{\beta}_i^{FMOLS}$	Relative price equation $\hat{\gamma}_i^{DOLS}$	$\hat{\gamma}_i^{FMOLS}$
AUS	-0.047	-0.062^b	0.567^a	0.559^a
	(-1.51)	(-2.19)	(10.95)	(10.88)
AUT	-0.220^a	-0.231^a	0.687^a	0.689^a
	(-12.62)	(-13.95)	(20.14)	(21.89)
BEL	-0.150^a	-0.135^a	0.732^a	0.740^a
	(-6.36)	(-5.74)	(17.49)	(17.52)
CAN	-0.298^a	-0.299^a	0.549^a	0.524^a
	(-6.11)	(-7.19)	(4.95)	(5.19)
DEU	-0.502^a	-0.493^a	0.532^a	0.517^a
	(-20.60)	(-22.90)	(9.76)	(10.70)
DNK	-0.366^a	-0.355^a	0.361^a	0.357^a
	(-4.96)	(-5.86)	(9.51)	(12.63)
ESP	-0.231^a	-0.236^a	0.689^a	0.709^a
	(-8.30)	(-11.10)	(19.14)	(21.50)
FIN	-0.197^a	-0.193^a	0.645^a	0.628^a
	(-11.14)	(-12.99)	(19.98)	(23.02)
FRA	-0.396^a	-0.395^a	0.787^a	0.790^a
	(-6.56)	(-7.00)	(29.79)	(31.01)
GBR	-0.152^b	-0.161^a	0.842^a	0.810^a
	(-2.35)	(-2.94)	(6.63)	(7.41)
IRL	-0.187^a	-0.193^a	0.554^a	0.562^a
	(-3.64)	(-4.20)	(18.09)	(19.20)
ITA	-0.265^a	-0.282^a	0.761^a	0.727^a
	(-10.04)	(-11.74)	(23.91)	(23.34)
JPN	-0.161^a	-0.157^a	0.879^a	0.898^a
	(-8.05)	(-9.29)	(42.50)	(41.06)
KOR	-0.403^a	-0.393^a	0.529^a	0.532^a
	(-10.77)	(-12.53)	(40.46)	(45.58)
NLD	-0.331^a	-0.307^a	0.724^a	0.731^a
	(-5.90)	(-5.82)	(15.95)	(18.04)
NOR	-0.071^a	-0.081^a	0.094	0.034
	(-5.84)	(-6.17)	(0.75)	(0.29)
SWE	-0.020	-0.009	0.908^a	0.882^a
	(-0.66)	(-0.52)	(11.23)	(18.13)
USA	-0.017	-0.033	0.784^a	0.765^a
	(-0.69)	(-1.47)	(23.50)	(24.80)
EU-12	-0.252^a	-0.249^a	0.685^a	0.679^a
	(-26.89)	(-30.24)	(58.20)	(64.78)
All sample	-0.223^a	-0.223^a	0.646^a	0.636^a
	(-29.72)	(-33.85)	(76.543)	(83.01)

Notes: Heteroskedasticity and autocorrelation consistent t-statistics are reported in parentheses. ^{a}, ^{b} and ^{c} denote significance at 1%, 5% and 10% levels.

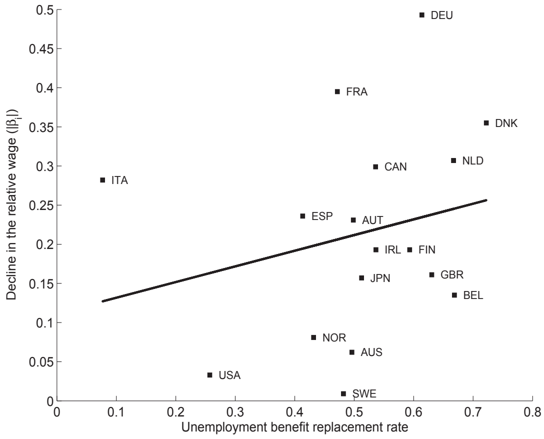
Table 4: Panel Cointegration Estimates of β for subsamples (eq. (8))

LMR	r		EPL$_{adj}$		BargCov		LMR	
	DOLS	FMOLS	DOLS	FMOLS	DOLS	FMOLS	DOLS	FMOLS
β^H	-0.261^a	-0.255^a	-0.165^a	-0.172^a	-0.242^a	-0.238^a	-0.166^a	-0.173^a
	(-23.04)	(-25.65)	(-30.29)	(-32.59)	(-22.18)	(-24.91)	(-31.68)	(-33.20)
β^L	-0.158^a	-0.166^a	-0.130^a	-0.130^a	-0.180^a	-0.185^a	-0.113^a	-0.112^a
	(-16.34)	(-19.14)	(-13.97)	(-11.57)	(-17.25)	(-19.93)	(-10.74)	(-8.26)
$t(\hat{\beta}_{low} = \hat{\beta}_{high})$	0.000	0.000	0.000	0.000	0.000	0.011	0.000	0.000
Time period	1970-2007		1985-2007		1970-2007		1985-2007	
Countries	17		18		17		17	
Observations	642		414		642		390	
mean LMR (high)	0.609		2.280		0.864		1.376	
mean LMR (low)	0.389		1.296		0.448		-0.578	

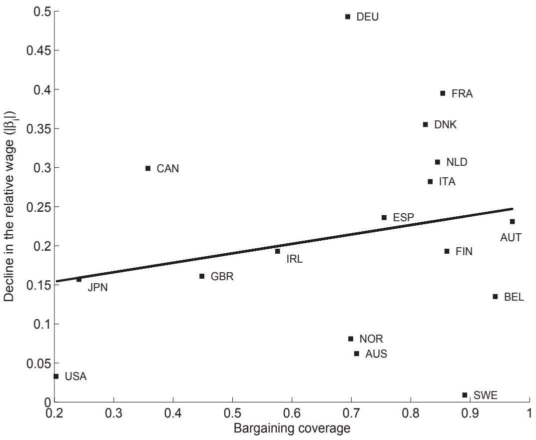
Notes: ^{a} denotes significance at 1% level. The row $t(\hat{\beta}^L = \hat{\beta}^H)$ reports the p-value of the test of $H_0 : \hat{\beta}^L = \hat{\beta}^H$. r is the unemployment benefits replacement rate, EPL_{adj} the strictness of employment protection against dismissals, $BargCov$ the bargaining coverage and LMR the labor market regulation index obtained by using a principal component analysis.



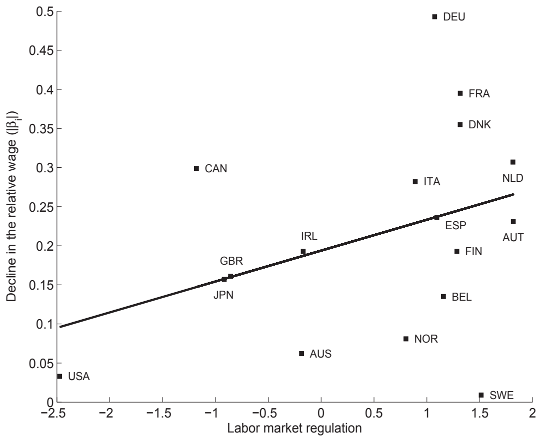
(a) Relative Wage Responses against Firing Cost



(b) Relative Wage Responses against Generosity of Unemployment Benefit Scheme

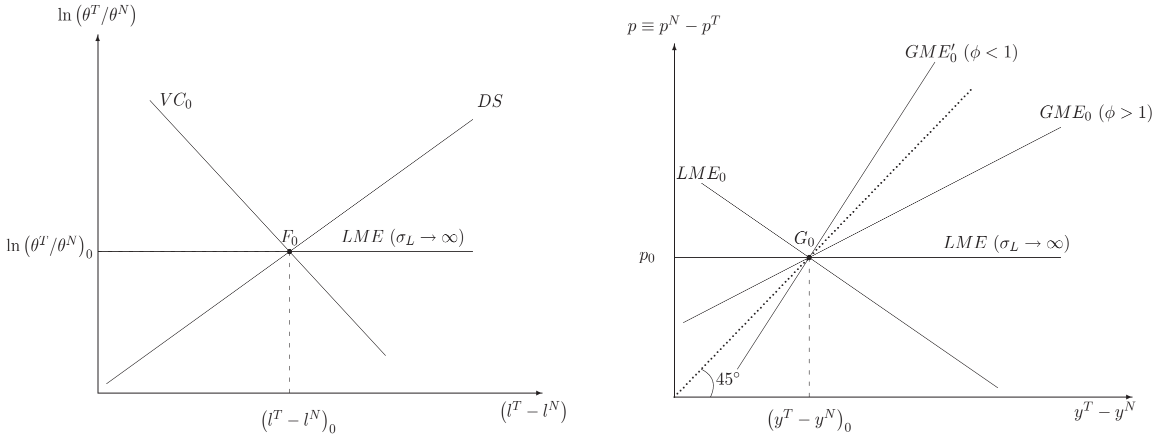


(c) Relative Wage Responses against Worker Bargaining Power



(d) Relative Wage Responses against Labor Market Regulation Index

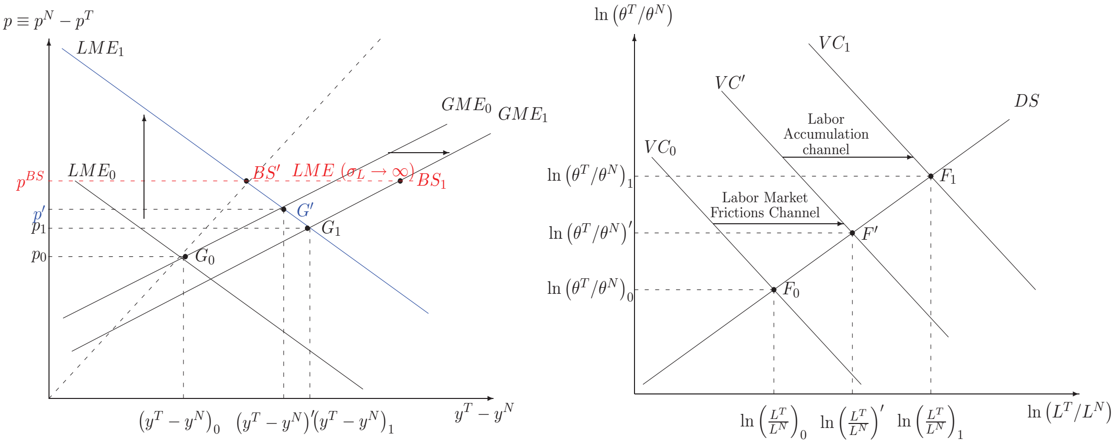
Figure 2: Labor Market Regulation and The Relative Wage Response to Technological Change Biased toward the Traded Sector Notes: Figure 2 plots fully modified OLS estimates of relative wage responses to a labor productivity differential against indicators of labor market regulation. Horizontal axis displays the FMOLS estimates for each country which are taken from Table 3. For easier reading, we show the absolute value of the change in the relative wage (i.e., $|\beta_i|$). Firing cost is captured by the employment protection legislation index adjusted with the share of permanent workers in the economy (source: OECD); the generosity of unemployment benefit scheme is measured by the average of net unemployment benefit replacement rates for three duration of unemployment (source: OECD); the worker bargaining power is measured by the bargaining coverage (source: Visser [2009]); in Figure 2(d), we have recourse to a principal component analysis in order to have one overall indicator encompassing the three dimensions of labor market regulation.



(a) $(l^T - l^N, \ln(\theta^T/\theta^N))$-space

(b) $(y^T - y^N, p)$-space

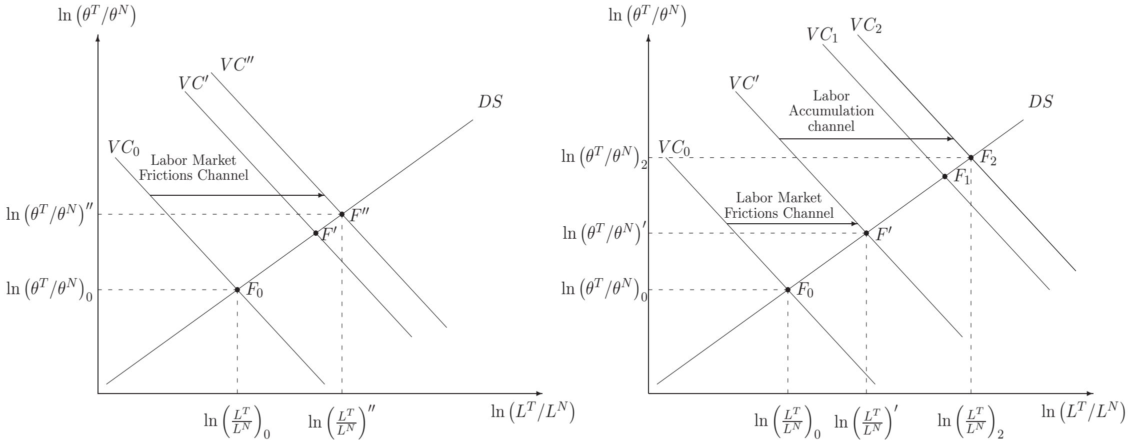
Figure 3: Steady-State



(a) $(y^T - y^N, p)$-space

(b) $(l^T - l^N, \ln(\theta^T/\theta^N))$-space

Figure 4: Long-Run Relative Price and Relative Wage Effects of Technological Change Biased toward the Traded Sector



(a) Consequences of a higher firing tax

(b) Consequences of a higher replacement rate or worker bargaining power

Figure 5: Implications for the Relative Wage Response of Labor Market Regulation in the $(l^T - l^N, \ln(\theta^T/\theta^N))$-space

Table 5: Long-Term Relative Price and Relative Wage Responses to a Productivity Differential between Tradables and Non Tradables (in %)

	BS	OECD	Labor force			Bargaining power	Replacement rate	Firing	EU-12	US
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)
	$(u=0)$	$(u=8.1\%)$	$(\sigma_L=0)$	$(\sigma_L=0.2)$	$(\sigma_L=1)$	$(\alpha_W=0.9)$	$(r=0.782)$	$(\tau=13)$	$(u=9.1\%)$	$(u=5.2\%)$
$\phi=1$										
A.Relative Wage										
Relative wage, $\hat{\omega}$	0.00	-0.31	-0.59	-0.43	-0.25	-0.35	-0.37	-0.34	-0.34	-0.25
Labor market frictions effect	0.00	-0.02	-0.04	-0.02	-0.02	-0.03	-0.03	-0.06	-0.03	-0.00
Labor accumulation effect	0.00	-0.29	-0.55	-0.42	-0.22	-0.32	-0.34	-0.28	-0.31	-0.24
B.Relative Price										
Relative price, $\hat{p}$	1.00	0.70	0.42	0.57	0.77	0.66	0.63	0.73	0.67	0.74
Labor market frictions effect	0.00	1.01	0.99	1.01	1.01	1.01	1.00	1.04	1.01	1.00
Labor accumulation effect	0.00	-0.31	-0.57	-0.44	-0.24	-0.34	-0.37	-0.30	-0.32	-0.24
$\phi<1$										
C.Relative Wage										
Relative wage, $\hat{\omega}$	0.00	-0.16	-0.48	-0.20	-0.14	-0.21	-0.25	-0.19	-0.20	-0.09
Labor market frictions effect	0.00	0.29	0.52	0.45	0.21	0.27	0.25	0.25	0.28	0.32
Labor accumulation effect	0.00	-0.45	-1.00	-0.64	-0.35	-0.47	-0.50	-0.44	-0.48	-0.40
D.Relative Price										
Relative price, $\hat{p}$	1.00	0.85	0.53	0.82	0.88	0.81	0.76	0.89	0.82	0.90
Labor market frictions effect	0.00	1.33	1.57	1.49	1.26	1.31	1.30	1.37	1.33	1.32
Labor accumulation effect	0.00	-0.47	-1.03	-0.66	-0.37	-0.49	-0.54	-0.47	-0.49	-0.40
$\phi>1$										
E.Relative Wage										
Relative wage, $\hat{\omega}$	0.00	-0.44	-0.68	-0.58	-0.36	-0.47	-0.47	-0.47	-0.46	-0.39
Labor market frictions effect	0.00	-0.25	-0.34	-0.30	-0.22	-0.25	-0.24	-0.29	-0.25	-0.24
Labor accumulation effect	0.00	-0.19	-0.34	-0.29	-0.14	-0.23	-0.24	-0.18	-0.21	-0.15
F.Relative Price										
Relative price, $\hat{p}$	1.00	0.57	0.32	0.42	0.65	0.54	0.52	0.59	0.54	0.60
Labor market frictions effect	0.00	0.77	0.68	0.72	0.81	0.78	0.78	0.79	0.77	0.76
Labor accumulation effect	0.00	-0.21	-0.36	-0.31	-0.16	-0.24	-0.26	-0.20	-0.22	-0.15

Notes: Effects of a 1 percentage point increase in the labor productivity differential between tradables and non tradables. Panels A and B show the deviation in percentage relative to steady-state for the relative price of non tradables $p \equiv p^N - p^T$ and the relative wage of non traded workers $\omega \equiv w^N - w^T$, respectively, and break down changes in a labor market frictions effect (keeping unchanged net exports NX), and a labor capital accumulation effect (stemming from the hiring boom causing a current account deficit in the short-run and therefore requiring a steady-state improvement in the balance of trade). While panels A and B show the results when setting ϕ to one, panels C and D show results for $\phi < 1$ and panels E and F show results for $\phi > 1$; ϕ is the elasticity of substitution between tradables and non tradables; σ_L is the elasticity of labor supply at the extensive margin; α_W corresponds to the worker bargaining power; r is the unemployment benefits replacement rate; τ measures the strictness of employment protection expressed in monthly salary equivalents (with $x = \tau .W$ where x is the firing tax).

Table 6: Comparison of Predicted Values with Empirical Estimates

Country	Parameter	Relative wage response			Relative price response		
	(1)	(2)	(3)	(4)	(5)	(6)	(7)
	Substitutability ϕ	$\hat{\omega}^{predict}$	$\hat{\omega}^{FMOLS}$	(3)-(2)	$\hat{p}^{predict}$	$\hat{p}^{FMOLS}$	(6)-(5)
AUS	0.295	0.179	-0.062	-0.241	1.179	0.559	-0.620
AUT	1.019	-0.337	-0.231	0.106	0.691*	0.689	-0.002
BEL	0.749	-0.294	-0.135	0.159	0.724*	0.740	0.0160
CAN	0.439	0.009	-0.299	-0.308	1.017	0.524	-0.493
DEU	1.126	-0.423	-0.493	-0.070	0.572*	0.517	-0.055
DNK	1.925	-0.527	-0.355	0.172	0.473	0.357	-0.116
ESP	0.782	-0.286*	-0.236	0.050	0.760*	0.709	-0.051
FIN	1.043	-0.384	-0.193	0.191	0.628*	0.628	0.000
FRA	0.896	-0.355*	-0.395	-0.040	0.650	0.790	0.140
GBR	0.477	-0.049*	-0.161	-0.112	0.956*	0.810	-0.146
IRL	0.321	-0.171*	-0.193	-0.022	0.831	0.562	-0.269
ITA	-	-0.272*	-0.282	-0.010	0.729*	0.727	-0.002
JPN	0.713	-0.152*	-0.157	-0.005	0.860*	0.898	0.038
KOR	2.914	-0.677	-0.393	0.284	0.379	0.532	0.153
NLD	0.644	-0.286*	-0.307	-0.021	0.711*	0.731	0.020
NOR	1.004	-0.292	-0.081	0.211	0.705	0.034	-0.671
SWE	0.329	0.134	-0.009	-0.143	1.161	0.882	-0.279
USA	0.699	-0.037*	-0.033	0.004	0.972	0.765	-0.207
EU-12	0.599	-0.160	-0.249	-0.089	0.855	0.679	-0.176
Whole sample	0.800	-0.229*	-0.223	0.006	0.783	0.636	-0.147

Notes: ϕ is the intratemporal elasticity of substitution between traded goods and non traded goods; because estimates of ϕ for Italy are inconsistent, its value is left blank. We denote by superscripts "predict" and "FMOLS" the numerically computed values and fully modified OLS estimates taken from Table 3, respectively; columns (4) and (7) show the difference between FMOLS estimates and predicted values for percentage changes in the relative wage and the relative price of non tradables. * indicates that the predicted value falls in the confidence interval; we calculate 99% confidence intervals based on estimated standard deviations of β and γ obtained when running the regression (7a) and (7b), respectively, for each country, EU-12 and the whole sample.

A Data for Empirical Analysis

Coverage: Our sample consists of a panel of 18 countries: Australia (AUS), Austria (AUT), Belgium (BEL), Canada (CAN), Germany (DEU), Denmark (DNK), Spain (ESP), Finland (FIN), France (FRA), the United Kingdom (GBR), Ireland (IRL), Italy (ITA), Japan (JPN), Korea (KOR), the Netherlands (NLD), Norway (NOR), Sweden (SWE), and the United States (USA). The period is running from 1970 to 2007, except for Japan (1974-2007).

Sources: We use the EU KLEMS [2011] database (the March 2011 data release) for all countries of our sample with the exceptions of Canada and Norway. For these two countries, sectoral data are taken from the Structural Analysis (STAN) database provided by the OECD [2011]. Both the EU KLEMS and STAN databases provide annual data at the ISIC-rev.3 1-digit level for eleven industries.

The eleven industries are split into tradables and non tradables sectors. To do so, we adopt the classification proposed by De Gregorio et al. [1994]. Following Jensen and Kletzer [2006], we have updated this classification by treating "Financial Intermediation" as a traded industry. We construct traded and non traded sectors as follows (EU KLEMS codes are given in parentheses):

- **Traded Sector**: "Agriculture, Hunting, Forestry and Fishing" (A-B), "Mining and Quarrying" (C), "Total Manufacturing" (D), "Transport, Storage and Communication" (I) and "Financial Intermediation" (J).
- **Non Traded Sector**: "Electricity, Gas and Water Supply" (E), "Construction" (F), "Wholesale and Retail Trade" (G), "Hotels and Restaurants" (H), "Real Estate, Renting and Business Services" (K) and "Community Social and Personal Services" (L-Q).

Once industries have been classified as traded or non traded, for any macroeconomic variable X, its sectoral counterpart X^j for $j = T, N$ is constructed by adding the X_k of all sub-industries k classified in sector $j = T, N$ as follows $X^j = \sum_{k \in j} X_k$. In the following, we provide details on data construction (mnemonics are in parentheses):

- **Relative wage of non tradables**, Ω, is calculated as the ratio of the nominal wage in the non traded sector W^N to the nominal wage in the traded sector W^T, i.e., $\Omega = W^N/W^T$. The sectoral nominal wage W^j for sector $j = T, N$ is calculated by dividing labor compensation in sector j (LAB) by total hours worked by persons engaged (H_EMP) in that sector.
- **Relative price of non tradables**, P, corresponds to the ratio of the value added deflator of non traded goods P^N to the value added deflator of traded goods P^T, i.e., $P = P^N/P^T$. The sectoral value-added deflator P^j for sector $j = T, N$ is calculated by dividing value added at current prices by value added at constant prices in sector j. Series for sectoral value added at current prices (VA) (constant prices (VA_QI) resp.) are constructed by adding value at current (constant resp.) prices of all sub-industries in sector $j = T, N$.
- **Relative productivity of tradables**, A^T/A^N, is calculated as the ratio of traded real labor productivity A^T to the non traded real labor productivity A^N. To measure real labor productivity in sector $j = T, N$, we divide value-added at constant prices in sector j (VA_QI) by total hours worked by persons engaged (H_EMP) in that sector.

To empirically assess the role of labor market regulation in the determination of the relative price and relative wage responses to higher productivity growth in tradables relative to non tradables, we use a number of indicators which capture the extent of rigidity of labor markets. We detail below the sources:

- **Employment protection legislation**, denoted by EPL, is an index available on an annual basis developed by the OECD which is designed as a multi-dimensional indicator of the strictness of a comprehensive set of legal regulations governing hiring and firing employees on regular contracts. Source: OECD Labour Market Statistics database. Data coverage: 1985-2007 (1990-2007 for KOR). Because the legal protection for workers with temporary contracts has been eased in most European countries, we follow Boeri and Van Ours [2008] and construct an alternative index in order to have a more accurate measure of employment protection. This indicator, denoted by EPL^{adj}, is computed by adjusting EPL with the share of permanent workers in the economy (share$_{perm}$) according to EPL^{adj} = EPL $\times$ share$_{perm}$. Source for share$_{perm}$: OECD Labour Market Statistics database. Data coverage: 1985-2007 (1990-2007 for KOR).
- The generosity of the unemployment benefit scheme, r_{it} in country i at time t, is commonly captured by the **unemployment benefit replacement rate**. The replacement rate measure is defined as the average of the net unemployment benefit (including social assistance and housing benefit) replacement rates for two earnings levels and three family situations, and for three durations of unemployment (1 year, 2&3 years, 4&5 years). Source: OECD, Benefits and

Wages Database. Data coverage: 2001-2007. In order to have longer time series, we calculated r over the period running from 1970 to 2000, by using the growth rate of the historic OECD measure of benefit entitlements which is defined as the average of the gross unemployment benefit replacement rates for two earnings levels, three family situations and three durations of unemployment. Source: OECD, Benefits and Wages Database. Data coverage: 1970-2001 for all countries while data are unavailable for Korea.

- The worker bargaining power is measured by the **collective bargaining coverage**, BargCov_{it}, which corresponds to the employees covered by collective wage bargaining agreements as a proportion of all wage and salary earners in employment with the right to bargaining. Source: Data Base on Institutional Characteristics of Trade Unions, Wage Setting, State Intervention and Social Pacts, 1960-2009 (ICTWSS), version 3.0, Jelle Visser [2009]. Data coverage: 1970-2007 for AUS, AUT, CAN, DEU, DNK, FIN, GBR, IRL, ITA, JPN, SWE and USA, 1970-2005 for NLD and NOR, 1970-2002 for BEL and FRA, 1977-2004 for ESP and 2002-2006 for KOR.

B Data for Calibration

B.1 Non Tradable Share

Table 7 shows the non-tradable content of labor, consumption, government spending, and gives the share of government spending on the traded and non traded goods in the sectoral output. The last column of Table 7 also shows the ratio of traded real labor productivity to the non traded real labor productivity, A^T/A^N. Our sample consists of 18 OECD countries mentioned in section A, including 12 European countries plus Australia, Canada, Korea, Japan, Norway, the United-States. Our reference period for the calibration corresponds to the period 1990-2007. The choice of this period has been dictated by data availability.

To calculate the non-tradable share of employment we split the eleven industries into traded and non-traded sectors by adopting the classification proposed by De Gregorio et al. [1994] and updated by Jensen and Kletzer [2006] (Source: EU KLEMS [2011]). The non-tradable share of labor, shown in column 1 of Table 7 averages to 66%.

To split consumption expenditure (at current prices) into consumption in traded and non traded goods, we made use of the Classification of Individual Consumption by Purpose (COICOP) published by the United Nations (Source: United Nations [2012]). Among the twelve items, the following ones are treated as consumption in traded goods: "Food and Non-Alcoholic Beverages", "Alcoholic Beverages Tobacco and Narcotics", "Clothing and Footwear", "Furnishings, Household Equipment", "Transport", "Miscellaneous Goods and Services". The remaining items are treated as consumption in non traded goods: "Housing, Water, Electricity, Gas and Fuels", "Health", "Communication", "Education", "Restaurants and Hotels". Because the item "Recreation and Culture" is somewhat problematic, we decided to consider it as both tradable (50%) and non tradable (50%) with equal shares. Data coverage: 1990-2007 for AUS, AUT, CAN, DNK, FIN, FRA, GBR, ITA, JPN, KOR, NLD, NOR, and USA, 1991-2007 for DEU, 1993-2007 for SWE, 1995-2007 for BEL and ESP and 1996-2007 for IRL. Note that the non-tradable share of consumption shown in column 2 of Table 7 averages to 42%, in line with the share reported by Stockman and Tesar [1995].

Sectoral government expenditure data (at current prices) were obtained from the Government Finance Statistics Yearbook (Source: IMF [2011]) and the OECD General Government Accounts database (Source: OECD [2012b]). Adopting Morshed and Turnovsky's [2004] methodology, the following four items were treated as traded: "Fuel and Energy", "Agriculture, Forestry, Fishing, and Hunting", "Mining, Manufacturing, and Construction", "Transport and Communications". Items treated as non traded are: "Government Public Services", "Defense", "Public Order and Safety", "Education", "Health", "Social Security and Welfare", "Environment Protection", "Housing and Community Amenities", "Recreation Cultural and Community Affairs". Data coverage: 1990-2007 for BEL, DNK, FIN, GBR, IRL, ITA, JPN, NOR and USA, 1990-2006 for CAN, 1991-2007 for DEU, 1995-2007 for AUT, ESP, FRA, NLD and SWE and 2000-2007 for KOR (data are not available for AUS). The non-tradable component of government spending shown in column 3 of Table 7 averages to 90%. While government spending as a share in GDP is shown in column 4, the proportion of government spending on the traded and non traded good (i.e., G^T/Y^T and G^N/Y^N) are shown in columns 5 and 6 of Table 7. They average 5% and 29%, respectively.

The last column of Table 7 displays the ratio of labor productivity of tradables relative to non tradables (A^T/A^N) averaged over the period 1990-2007 for all countries. Source: the EU KLEMS [2011] and STAN database. As shown in column 7, the traded sector is in average 28 percent more productive than the non traded sector.

B.2 Elasticity of Substitution in consumption (ϕ)

To estimate the elasticity of substitution in consumption ϕ between traded and non traded goods, we first derive a testable equation by inserting the optimal rule for intra-temporal allocation of consumption (15) into the goods market equilibrium which gives $\frac{C^T}{C^N} = \frac{Y^T - NX - E^T}{Y^N - E^N}$ where $NX \equiv \dot{B} - r^\star B$ is net exports, $E^T \equiv G^T + I^T + F$ (with $F \equiv \kappa^T V^T + \kappa^N V^N$) and $E^N \equiv G^N + I^N$; note that we include investment in order to be consistent with accounting identities. Inserting the optimal rule for intra-temporal allocation of consumption (15) into the goods market equilibrium, and denoting the ratio of E^T to traded value added adjusted with net exports at current prices by $\upsilon_{E^T} = \frac{P^T E^T}{P^T Y^T - P^T NX}$, and the ratio of $E^N \equiv G^N + I^N$ to non traded value added at current prices by $\upsilon_{E^N} = \frac{P^N E^N}{P^N Y^N}$, the goods market equilibrium can be rewritten as follows $\frac{\left(Y^T - NX\right)\left(1-\upsilon_{E^T}\right)}{Y^N\left(1-\upsilon_{E^N}\right)} = \left(\frac{\varphi}{1-\varphi}\right) P^\phi$. Isolating $\left(Y^T - NX\right)/Y^N$ and taking logarithm yields $\ln\left(\frac{Y^T - NX}{Y^N}\right) = \alpha + \phi \ln P$ where $\alpha \equiv \ln\left(\frac{1-\upsilon_E^N}{1-\upsilon_E^T}\right) + \ln\left(\frac{\varphi}{1-\varphi}\right)$. Adding an error term μ, we estimate ϕ by running the regression of the (logged) output of tradables adjusted with net exports at constant prices in terms of output of non tradables on the (logged) relative price of non tradables:

$$\ln\left(\frac{Y^T - NX}{Y^N}\right)_{i,t} = f_i + f_t + \alpha_i t + \phi_i \ln P_{i,t} + \mu_{i,t}, \tag{53}$$

where f_i and f_t are the country fixed effects and time dummies, respectively. Because the term α is composed of ratios which may display a trend over time, we add country-specific linear trends, as captured by $\alpha_i t$.

Instead of using time series for sectoral value added, we can alternatively make use of series for sectoral labor compensation. Multiplying both sides of $\frac{\left(Y^T - NX\right)\left(1-\upsilon_{E^T}\right)}{Y^N\left(1-\upsilon_{E^N}\right)} = \left(\frac{\varphi}{1-\varphi}\right) P^\phi$ by $\frac{P^T}{P^N}$ and then by $\frac{\rho^T}{\rho^N}$ with $\rho^j = \frac{W^j L^j}{P^j Y^j}$, denoting by $\gamma^T = \left(W^T L^T - \rho^T P^T NX\right)$ (with $\rho_T \equiv \frac{W^T L^T}{P^T Y^T}$) and $\gamma^N = W^N L^N$, and taking logarithm yields $\ln\left(\frac{\gamma^T}{\gamma^N}\right) = \eta + (\phi - 1)\ln P$ where η is a term composed of both preference (i.e., φ) and production (i.e., ρ^j) parameters, and the (logged) ratio of E^T (E^N) to $W^T L^T - \rho^T P^T NX$ ($W^N L^N$). We thus estimate ϕ by exploring alternatively the following empirical relationship:

$$\ln\left(\gamma^T/\gamma^N\right)_{i,t} = g_i + g_t + \eta_i t + \delta_i \ln P_{i,t} + \zeta_{i,t}, \tag{54}$$

where $\delta_i = (\phi_i - 1)$; g_i and g_t are the country fixed effects and time dummies, respectively; we add country-specific trends, as captured by $\eta_i t$, because η is composed of ratios that may display a trend over time.

Time series for sectoral value added at constant prices, labor compensation, and the relative price of non tradables are taken from EU KLEMS [2011] (see section A). Net exports correspond to the external balance of goods and services at current prices taken from OECD Economic Outlook Database. To construct time series for net exports at constant prices NX, data are deflated by the traded value added deflator of traded goods (i.e., P^T).

Since the LHS term of (53) and (54) and the relative price of non tradables as well display trends, we ran unit root and then cointegration tests. Having verified that these two assumptions are empirically supported, we estimate the cointegrating relationships by using DOLS and FMOLS estimators for cointegrated panel proposed by Pedroni [2000], [2001]. DOLS and FMOLS estimates are reported in Table 8, considering alternatively eq. (53) or eq. (54). Estimates of ϕ are reported in column 1 of Table 6 when calibrating the model for each country. As a reference model, we consider FMOLS estimates when exploring the empirical relationship (53); running regression (53) gives an estimate for the whole sample of 0.800 which is close to the value documented by Mendoza [1995] who reports an estimate of 0.74. As shown in Table 8, the estimated value of ϕ for Belgium is statistically significant only when exploring the empirical relationship (54) for this economy; in column 1 of Table 6, we set ϕ to 0.749 for Belgium. Because estimates for Italy are negative by using alternatively eq. (53) or eq. (54), the estimate of ϕ for this country is left blank in column 1 of Table 6 and ϕ is set to our panel data estimation for EU-12, i.e., 0.599, when calibrating the model for each country.

B.3 Labor Market Variables

We now describe the data employed to calibrate the model, focusing on labor market variables:

- **Sectoral unemployment rate** denoted by u^j ($j = T, N$) is the number of unemployed workers U^j in sector j as a share of the labor force $F^j \equiv L^j + U^j$ in this sector. LABORSTA database from ILO provides series for unemployed workers by economic activity for fifteen OECD countries out of eighteen in our sample. The longest available period ranges from

Table 7: Data to Calibrate the Two-Sector Model (1990-2007)

Countries	Non tradable Share			G^j/Y^j			Relative Productivity
	Labor	Consumption	Gov. Spending	G/Y	G^T/Y^T	G^N/Y^N	A^T/A^N
	(1)	(2)	(3)	(4)	(5)	(6)	(7)
AUS	0.68	0.43	n.a.	0.18	n.a.	n.a.	1.30
AUT	0.64	0.42	0.90	0.19	0.05	0.27	1.05
BEL	0.68	0.42	0.91	0.22	0.06	0.30	1.28
CAN	0.69	0.43	0.91	0.20	0.05	0.30	1.32
DEU	0.65	0.40	0.91	0.19	0.05	0.27	1.00
DNK	0.68	0.42	0.94	0.26	0.05	0.36	1.17
ESP	0.66	0.46	0.88	0.18	0.06	0.24	1.18
FIN	0.63	0.43	0.89	0.22	0.06	0.34	1.47
FRA	0.69	0.40	0.94	0.23	0.05	0.31	1.05
GBR	0.70	0.40	0.93	0.20	0.04	0.29	1.54
IRL	0.62	0.43	0.89	0.17	0.04	0.28	1.83
ITA	0.63	0.37	0.91	0.19	0.05	0.27	1.00
JPN	0.64	0.43	0.86	0.16	0.06	0.22	0.96
KOR	0.58	0.44	0.76	0.12	0.06	0.18	1.53
NLD	0.70	0.40	0.90	0.23	0.07	0.32	1.38
NOR	0.66	0.39	0.88	0.21	0.06	0.34	1.44
SWE	0.68	0.45	0.92	0.27	0.06	0.39	1.42
USA	0.73	0.51	0.90	0.16	0.05	0.20	1.12
EU-12	0.66	0.42	0.91	0.21	0.05	0.30	1.28
Mean	0.66	0.42	0.90	0.20	0.05	0.29	1.28

1987 to 2007. On average, our data covers 12.8 years per country. Series cover 18 sectors, according to ISIC Rev.3.1 classification. To construct L^j and U^j for $j = T, N$, we map the classification used previously to compute series for sectoral wages, prices and real labor productivity indexes (see section A) into the 1-digit ISIC-rev.3 classification. The mapping was clear for all industries except for "Not classifiable by economic activity" (1-digit ISIC-Rev.3, code: X) when constructing L^j and U^j, and, "Unemployed seeking their first job" to identify U^j. These two categories have been split between tradables and non tradables according to the shares of total unemployment (excluding the two sectors) between tradables and non tradables by year and country. In a few rare cases, the sum of sectoral employment provided by ILO did not correspond to total unemployment. These differences were usually due to missing data for some industries in the sectoral databases. In these cases, we added these differences in level, keeping however the share of each sector constant. In Table 9 we provide an overview of the classifications used to construct traded and non traded sectors variables. Once industries have been classified as traded or non traded, series for unemployed and employed workers are constructed by adding unemployed and employed workers of all sub-industries k in sector $j = T, N$ in the form $U^j = \sum_{k \in j} U_k$ and $L^j = \sum_{k \in j} L_k$. Data coverage: AUS (1995-2007), AUT (1994-2007), BEL (2001-2007), CAN (1987-2007), DEU (1995-2007), DNK (1994-1998 and 2002-2004), ESP (1992-2007), FIN (1995-2007), GBR (1988-2007), IRL (1986-1997), ITA (1993-2007), JPN (2003-2007), KOR (1992-2007), SWE (1995-2007) and USA (2003-2007). Data for unemployed workers by economic activity are not available for FRA, NLD and NOR.

- **Sectoral labor market tightness** denoted by θ^j ($j = T, N$) is calculated as the ratio of job vacancies in sector j (V^j) to the number of unemployed workers in that sector (U^j). To construct θ^j, we collect information on job vacancies and unemployed workers by economic activity. Sources for V^j: Job Openings and Labor Turnover Survey (JOLTS) provided by the Bureau of Labor Statistics (BLS) for USA, Eurostat database (NACE 1-digit) for a range of European Countries, Labour Market Statistics from the Office for National Statistics for the UK. Sources for U^j: Current Population Survey (CPS) published by the BLS for USA and LABORSTA (ILO) for European Countries.[57] As shown in Table 9, the level of detail in the definition of traded and non traded sectors differs across databases in two dimensions. First, the number of items to split disaggregated data varies across nomenclatures from a low eleven categories in the Eurostat database to a high of eighteen items in the LABORSTA database. Second, the definitions of items are not harmonized across the different sets of data.

[57] The JOLTS and CPS databases provide (not seasonally adjusted) monthly data on vacancies and unemployed workers. We convert monthly data series into annual data series by summing the twelve monthly data points.

Table 8: Estimates of the Elasticity of Substitution in Consumption between Tradables and Non Tradables (ϕ)

Country	$\hat{\phi}_i^{DOLS}$ eq. (53) (1)	$\hat{\phi}_i^{FMOLS}$ eq. (53) (2)	$\hat{\phi}_i^{DOLS}$ eq. (54) (3)	$\hat{\phi}_i^{FMOLS}$ eq. (54) (4)
AUS	0.081 (0.74)	0.295^a (3.09)	0.011 (0.08)	0.375^b (2.39)
AUT	0.574 (1.62)	1.019^a (2.99)	0.910^a (3.77)	1.414^a (4.98)
BEL	−0.268 (−1.58)	0.034 (0.17)	0.393^a (3.41)	0.749^a (4.60)
CAN	0.308^b (2.04)	0.439^a (3.75)	0.332^b (2.18)	0.569^a (4.94)
DEU	0.976^a (3.46)	1.126^a (2.99)	1.190^a (4.34)	1.363^a (3.47)
DNK	1.243 (1.24)	1.925^a (2.76)	1.698^b (2.35)	1.320^a (2.73)
ESP	0.527^a (3.31)	0.782^a (4.71)	0.177 (0.90)	0.355^c (1.71)
FIN	1.556^a (10.13)	1.043^a (9.30)	2.061^a (8.62)	1.412^a (8.45)
FRA	0.880^a (4.75)	0.896^a (6.29)	1.169^a (4.46)	1.048^a (5.58)
GBR	0.688^a (8.76)	0.477^a (9.57)	1.424^a (14.39)	1.183^a (15.03)
IRL	0.074 (0.28)	0.321 (1.48)	0.485 (0.89)	0.126 (0.28)
ITA	-0.365^a (−3.44)	−0.260 (−1.50)	-0.427^a (−3.04)	−0.206 (−1.17)
JPN	0.832^a (3.96)	0.713^a (3.25)	0.681^a (4.52)	0.655^a (4.55)
KOR	0.626 (0.52)	2.914^a (4.16)	1.006 (1.26)	2.237^a (4.60)
NLD	0.832^a (2.65)	0.644^c (1.93)	0.523^c (1.92)	0.412 (1.10)
NOR	1.138^a (7.26)	1.004^a (9.81)	2.080^a (14.42)	2.056^a (13.51)
SWE	0.364^b (2.24)	0.329^a (3.52)	1.073^a (5.85)	0.915^a (7.16)
USA	0.486 (1.37)	0.699^a (3.27)	0.571 (0.90)	0.804^b (2.07)
EU-12	0.590^a (9.65)	0.599^a (11.84)	0.890^a (26.17)	0.832^a (16.18)
Whole sample	0.586^a (11.63)	0.800^a (16.86)	0.853^a (24.52)	0.933^a (28.55)

Notes: Data coverage: 1970-2007 (except Japan: 1974-2007). All regressions include country fixed effects, time dummies and country specific trends. ^{a}, ^{b} and ^{c} denote significance at 1%, 5% and 10% levels. Heteroskedasticity and autocorrelation consistent t-statistics are reported in parentheses.

To generate sectoral variables in a consistent and uniform way, series on disaggregated data for vacancies and unemployed workers are added up to form traded and non traded sectors following, as close as possible, the classification we used for value added, hours worked and labor compensation. Once industries have been classified as traded or non traded, series for employment vacancies (unemployed workers resp.) are constructed by adding job openings (unemployed workers resp.) of all sub-industries k in sector $j = T, N$ in the form $V^j = \sum_{k \in j} V_k$ ($U^j = \sum_{k \in j} U_k$ resp.). Data coverage for V^j and U^j: AUT (2004-2005), DEU (2006-2007), FIN (2002-2007), GBR (2001-2007), SWE (2005-2007) and USA (2001-2007).

- **Aggregate labor market tightness** denoted by θ is also computed because series for θ^j are available over a too short time horizon and for a few countries only; θ is calculated as the ratio of job vacancies to registered unemployment. Source: Registered Unemployed and Job Vacancies Dataset, OECD. Coverage: AUS (1980-2007), BEL (1982-2003), DEU (1980-2007), ESP (1980-2004), FIN (1981-2007), GBR (1980-2007), NOR (1980-2007), SWE (1982-2007).

- **Job finding rate** denoted by m^j ($j = T, N$) is computed at a sectoral level by adopting the methodology proposed by Shimer [2012]. As Shimer [2012], we ignore movements in and out of the overall labor force. Since we compute the job finding rate for the traded and the non traded sector, we have to further assume that labor force is fixed at a sectoral level, i.e., we ignore reallocation of labor across sectors. More details on the model and the derivation of the results below can be found in the Technical Appendix. The monthly job finding rate $m^{j,<1}(t)$ for sector j at time t is computed as follows:

$$m^{j,<1}(t) = -\ln\left(1 - M^{j,<1}(t)\right), \tag{55}$$

where t indexes months and the probability of finding a job $M^{j,<1}$ within one month is given by

$$M^{j,<1}(t) = 1 - \left[\frac{\left(1 - \alpha^{<1}(t)\right) U^j(t)}{U^j(t-1)}\right], \tag{56}$$

with $\alpha^{j,<1}(t) = \frac{U^{j,<1}(t)}{U^j(t)}$ the share of unemployment less than one month ($U^{j,<1}(t)$) among total monthly unemployment ($U^j(t)$) in sector j. Source: LABORSTA database from ILO for data on employment and unemployment at the sectoral level, and, OECD for unemployment by duration.

- **Job destruction rate** denoted by s^j ($j = T, N$) is estimated by solving this equation:

$$U^j(t) = \psi^j(t)\frac{s^j(t)}{s^j(t) + m^{j,<1}(t)}\left(U^j(t) + L^j(t)\right) + \left(1 - \psi^j(t)\right) U^j(t-1), \tag{57}$$

where ψ^j is the monthly rate of convergence to the long-run sectoral unemployment rate:

$$\psi^j(t) = 1 - e^{-\left(s^j(t) + m^{j,<1}(t)\right)}. \tag{58}$$

When estimating s^j by using (57), the unemployment rate has not necessarily reached its long-run equilibrium. Since we calibrate the model so that the initial steady state is consistent with the empirical properties of each OECD economy, we have computed values for s^j which are consistent with the steady-state sectoral unemployment rate $u^j = \frac{s^j}{s^j + m^j}$ where u^j is the actual value taken from the data and m^j is computed by using (55). Reassuringly, average values for job destruction rates obtained from eq. (57) are close to those derived from the long-run equilibrium of the unemployment rate. More details can be found in the Technical Appendix.

- **Unemployment benefit net replacement rate** denoted by r is shown in column 14 of Table 10 and is defined in section A. Replacement rates are averaged over 1980-2007 for all countries except Korea (2001-2007). Average EU-12 unemployment benefit replacement rate shown in Table 10 is the unweighted average of twelve EU members' replacement rates. Source: OECD, Benefits and Wages Database.

- **Firing cost** denoted by τ is shown in the last column of Table 10 is a measure of the strictness of legal protection against dismissals captured by the firing tax $x = \tau .W$ in our model; it is calculated as the sum of the average advance notice and average severance payment after 4 and 20 years of employment. τ is expressed in monthly salary equivalents and is averaged over the period 1980-2005. See Aleksynska and Schindler [2011] for details of construction of variables. Source: Fondazione de Benedetti.

Series of employment and unemployment by economic activity provided by ILO are not available for France, the Netherlands, Norway; while such data is available for Korea, unemployment by duration provided by the OECD is not available and thus prevents the estimation of the monthly job finding and job destruction rates. For these four countries, we proceeded as follows:

- **Monthly job finding rates** denoted by m come from Hobijn and Sahin [2009] who give average values for France (1975-2004), the Netherlands (1983-2004), Norway (1983-2004). For Korea, we average the job finding rates taken from Chang et al. [2004] over 1993-1994.
- **Unemployment rate** denoted by u is is the number of unemployed people as a percentage of the labor force. Coverage: FRA (1975-2004), the NLD (1983-2004), NOR (1983-2004). Source: OECD, LFS database.
- **Monthly job separation rate** denoted by s is computed so as to be consistent with the steady-state unemployment rate given by $u = \frac{s}{s+m}$.

Table 9: Sectoral Classifications for Labor Market Variables

Sector	EU KLEMS/STAN	LABORSTA Employment	LABORSTA Unemployment	JOLTS (BLS)	CPS (BLS)	EUROSTAT
Tradables	Agriculture, Hunting, Forestry and Fishing (AtB)	Agriculture, Hunting, Forestry and Fishing (A-B)	Agriculture, Hunting, Forestry (A) Fishing (B)		Agriculture	Agriculture and fishing
	Mining and Quarrying (C)	Mining and Quarrying (C)	Mining and Quarrying (C)	Mining and logging	Mining and quarrying	Mining and quarrying
	Total Manufacturing (D)	Manufacturing (D)	Manufacturing (D)	Manufacturing	Manufacturing	Manufacturing
	Transport and Storage and Communication (I)	Transport, Storage and Communications (I)	Transport, Storage and Communications (I)	Transportation Information	Transportation and utilities Information	Transport, storage and communication
	Financial Intermediation (J)	Financial Intermediation (J)	Financial Intermediation (J)	Finance and insurance	Financial activities	Financial intermediation
			Unemployed seeking their first job			
Non Tradables	Electricity, Gas and Water Supply (E)	Electricity, Gas and Water Supply (E)	Electricity, Gas and Water Supply (E)			Electricity, gas and water supply
	Construction (F)	Construction (F)	Construction (F)	Construction	Construction	Construction
	Wholesale and Retail Trade (G)	Wholesale and Retail Trade (G)	Wholesale and Retail Trade (G)	Wholesale trade Retail trade	Wholesale and retail trade	Wholesale and retail trade
	Hotels and Restaurants (H)	Hotels and Restaurants (H)	Hotels and Restaurants (H)			Hotels and restaurants
	Real Estate, Renting and Business Activities (K)	Real Estate, Renting and Business Activities (K)	Real Estate, Renting and Business Activities (K)	Real estate and rental Business services	Business services	Real estate, renting and business activities
	Community Social and Personal Services (LtQ)	Public Adm., Defence and Compulsory Social Security (L)	Public Adm., Defence and Compulsory Social Security (L)	Government	Government workers	Public adm. and community services
		Education (M)	Education (M)	Education and health	Education and health services	
		Health and Social Work (N)	Health and Social Work (N)			
		Other Community, Social and Personal Service Activities (O)	Other Community, Social and Personal Service Activities (O)	Leisure and hospitality	Leisure and hospitality	
		Households with Employed Persons (P)	Households with Employed Persons (P)			
		Extra-Territorial Organizations and Bodies (Q)	Extra-Territorial Organizations and Bodies (Q)			
		Not classifiable by economic activity (X)	Not classifiable by economic activity (X)	Other services	Other services	
			Unemployed seeking their first job			
Unclassified					Self-employed, unincorporated and unpaid family workers	

Table 10: Data to Calibrate the Labor Market

Country	Period	u^T	u^N	u	m^T	s^T	m^N	s^N	Period	θ^T	θ^N	Period	θ	r	τ
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)	(15)
AUS	95-07	0.072	0.062	0.065	0.304	0.0236	0.278	0.0184				80-07	0.13	52.4	1.9
AUT	94-07	0.037	0.044	0.042	0.126	0.0048	0.123	0.0057	04-05	0.17	0.27	80-07	0.18	52.8	6.6
BEL	01-07	0.077	0.079	0.078	0.067	0.0056	0.064	0.0055				82-03	0.05	65.2	5.7
CAN	87-07	0.082	0.084	0.083	0.269	0.0241	0.269	0.0247						52.9	2.8
DEU	95-07	0.101	0.091	0.094	0.067	0.0075	0.062	0.0062	06-07	0.21	0.40	80-07	0.09	60.6	3.4
DNK	94-04	0.064	0.061	0.062	0.245	0.0167	0.247	0.0161						78.2	4.5
ESP	92-07	0.147	0.161	0.156	0.097	0.0167	0.094	0.0181				80-04	0.03	47.2	9.4
FIN	91-07	0.087	0.118	0.107	0.137	0.0130	0.135	0.0180	02-07	0.21	0.2	81-07	0.09	65.1	3.9
FRA	75-04	n.a.	n.a.	0.081	0.067	0.0059	0.067	0.0059				89-07	0.07	51.8	3.7
GBR	88-07	0.073	0.066	0.068	0.163	0.0129	0.161	0.0114	01-07	0.30	0.48	80-07	0.24	58.3	2.9
IRL	86-97	0.130	0.154	0.144	0.048	0.0071	0.045	0.0082						58.2	2.0
ITA	93-07	0.094	0.098	0.097	0.062	0.0065	0.059	0.0064						10.1	1.7
JPN	03-07	0.033	0.033	0.033	0.171	0.0058	0.165	0.0056				80-07	0.27	50.1	3.8
KOR	92-07	0.041	0.027	0.035	0.262	0.0112	0.262	0.0072						37.5	13.0
NLD	83-04	n.a.	n.a.	0.064	0.047	0.0032	0.047	0.0032						68.2	3.0
NOR	83-04	n.a.	n.a.	0.045	0.305	0.0143	0.305	0.0143				80-07	0.18	53.5	2.0
SWE	95-07	0.056	0.060	0.059	0.233	0.0138	0.231	0.0148	05-07	0.17	0.17	82-07	0.19	54.9	4.8
USA	03-07	0.048	0.053	0.052	0.444	0.0224	0.440	0.0246	01-07	0.43	0.65	01-07	0.59	26.1	0.0
Average EU-12		0.087	0.093	0.091	0.124	0.0118	0.122	0.0125		0.21	0.30		0.12	55.9	4.3
Average OECD		0.079	0.083	0.081	0.174	0.0148	0.170	0.0154		0.24	0.34		0.18	52.4	4.2

Notes: Regarding sectoral unemployment rates, job finding and separation rates for DNK, the period 1994-2004 has to be read 1994-1998 and 2002-2004; u^j is the sectoral unemployment rate (source: ILO); m^j and s^j are the monthly job finding and job destruction rates in sector $j = T, N$, respectively (source: ILO); the monthly job destruction rate has been estimated by adopting the methodology developed by Shimer [2012] except for FRA, NLD, NOR and KOR; θ^j is the labor market tightness in sector j (source: Eurostat for European countrie, Labour Market Statistics from the Office for National Statistics for the U.K., Bureau of Labor Statistics for the U.S.); r is the average net unemployment benefit replacement rate over the period 1980-2007 (source: OECD Benefits and Wages Database); τ (with $x = \tau W$) is the firing cost expressed in monthly salary equivalents and is averaged over the period 1980-2005 (source: Fondazione De Benedetti).

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TECHNICAL CHANGE BIASED TOWARD THE TRADED SECTOR AND LABOR MARKET FRICTIONS

TECHNICAL APPENDIX

NOT MEANT FOR PUBLICATION

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This Technical Appendix presents the source and construction of the data used in the empirical and quantitative analysis, and provides summary statistics as well in section A. Section B gives additional empirical results. More details on the model as well as the derivations of the results which are stated in the text are provided in sections C-K. First, the appendix sets out the approach taken to solve the model. Second, it analyzes equilibrium dynamics, provides formal solutions, and investigates the adjustment toward the stable path following a productivity shock biased toward the traded sector. Third, we derive the steady-state effects of a productivity shock biased toward the traded sector. Fourth, we explore the case of total immobility and perfect mobility as well in order to highlight the role of the elasticity of the labor supply at the extensive margin.

A Data Description

A.1 Data for Empirical Analysis: Source and Construction

Coverage: Our sample consists of a panel of 18 countries: Australia (AUS), Austria (AUT), Belgium (BEL), Canada (CAN), Germany (DEU), Denmark (DNK), Spain (ESP), Finland (FIN), France (FRA), the United Kingdom (GBR), Ireland (IRL), Italy (ITA), Japan (JPN), Korea (KOR), the Netherlands (NLD), Norway (NOR), Sweden (SWE), and the United States (USA). The period is running from 1970 to 2007, except for Japan (1974-2007). These countries have the most extensive coverage of variables of our interest.

Sources: We use the EU KLEMS [2011] database (the March 2011 data release) for all countries of our sample with the exceptions of Canada and Norway. For these two countries, sectoral data are taken from the Structural Analysis (STAN) database provided by the OECD [2011]. Both the EU KLEMS and STAN databases provide annual data at the ISIC-rev.3 1-digit level for eleven industries.

The eleven 1-digit ISIC-rev.3 industries are split into tradables and non tradables sectors. To do so, we adopt the classification proposed by De Gregorio et al. [1994] who treat an industry as traded when it exports at least 10% of its output. Following Jensen and Kletzer [2006], we have updated the classification suggested by De Gregorio et al. [1994] by treating "Financial Intermediation" as a traded industry. Jensen and Kletzer [2006] use the geographic concentration of service activities within the United States to identify which service activities are traded domestically. The authors classify activities that are traded domestically as potentially traded internationally. The idea is that when a good or a service is traded, the production of the activity is concentrated in a particular region to take advantage of economies of scale in production.

Jensen and Kletzer [2006] use the two-digit NAICS (North American Industrial Classification System) to identify tradable and non tradable sectors. We map their classification into the NACE-ISIC-rev.3 used by the EU KLEMS database. The mapping was clear for all sectors except for "Real Estate, Renting and Business Services". According to the EU KLEMS classification, the industry labelled "Real Estate, Renting and Business Services" is an aggregate of five sub-industries: "Real estate activities" (NACE code: 70), "Renting of Machinery and Equipment" (71), "Computer and Related Activities" (72), "Research and Development" (73) and "Other Business Activities" (74). While Jensen and Kletzer [2006] find that industries 70 and 71 can be classified as tradable, they do not provide information for industries 72, 73 and 74. We decided to classify "Real Estate, Renting and Business Services" as non tradable.

Traded Sector comprises the following industries: Agriculture, Hunting, Forestry and Fishing; Mining and Quarrying; Total Manufacturing; Transport, Storage and Communication; and Financial Intermediation.

Non Traded Sector comprises the following industries: Electricity, Gas and Water Supply; Construction; Wholesale and Retail Trade; Hotels and Restaurants; Real Estate, Renting and Business Services; and Community Social and Personal Services.

Relevant to our work, the EU KLEMS and STAN database provides series, for each industry and year, on value added at current and constant prices, permitting the derivation of sectoral deflators of value added, as well as details on labor compensation and employment data, allowing the construction of sectoral wage rates. We describe below the construction for the data employed in Section 2 (mnemonics are given in parentheses):

- Sectoral value-added deflator P_t^j for $j = T, N$: value added at current prices (VA) over value added at constant prices (VA_QI) in sector j. Source: EU KLEMS database. The relative price of non tradables P_t corresponds to the ratio of the value added deflator of non traded goods to the value added deflator of traded goods: $P_t = P_t^N / P_t^T$.
- Sectoral labor L_t^j for $j = T, N$: total hours worked by persons engaged (H_EMP) in sector j. Source: EU KLEMS database.
- Sectoral nominal wage W_t^j for $j = T, N$: labor compensation in sector j (LAB) over total hours worked by persons engaged (H_EMP) in that sector. Source: EU KLEMS database.

The relative wage, Ω_t is calculated as the ratio of the nominal wage in the non traded sector W^N to the nominal wage in the traded sector: $\Omega_t = W^N_t / W^T_t$.

Because data source and construction are heterogenous across variables as a result of different nomenclatures, Table 11 provides a summary of the classification adopted to split value added and its demand components as well into traded and non traded goods.

Summary statistics of the data used in the empirical analysis are displayed in Table 12. As shown in the first three columns, all countries of our sample experience technological change biased toward the traded sector, an appreciation in the relative price of non tradables (except for Norway) and a decline in the ratio of the non traded wage relative to the traded wage.

To empirically assess the role of labor market institutions in the determination of the relative wage response to higher productivity growth in tradables relative to non tradables, we use three indicators aimed at capturing the stringency of labor market regulation. We detail below the construction and the source of these three indicators:

- The strictness of legal protection against dismissals for permanent workers is measured by the **employment protection legislation** index, $EPL_{i,t}$ in country i at time t, provided by OECD. Source for $EPL_{i,t}$: OECD Labour Market Statistics database. Data coverage: 1985-2007 (1990-2007 for KOR). This index can be misleading since regulation was eased for temporary contracts (in Spain) while the regulation for workers with permanent contracts hardly changed. To have a more accurate measure of legal protection against dismissals, we construct a new index denoted by $\text{EPL}^{adj}_{i,t}$ in country i at time t by adjusting $EPL_{i,t}$ for regular workers with the share $\text{share}^{perm}_{i,t}$ of permanent workers in the economy, i.e., $\text{EPL}^{adj}_{i,t} = \text{EPL}_{i,t} \times \text{share}^{perm}_{i,t}$. Source for $\text{share}^{perm}_{i,t}$: OECD Labour Market Statistics database. Data coverage: 1985-2007 (1990-2007 for KOR).
- The generosity of the unemployment benefit scheme, $r_{i,t}$ in country i at time t, is commonly captured by the **unemployment benefit replacement rate**. It is worthwhile noticing that the unemployment benefit rates are very similar across counties when considering short-term unemployment (less than one year) but display considerable heterogeneity for long-term unemployment. To have a more accurate measure of the generosity of the unemployment benefit scheme, we calculate r as the average of the net unemployment benefit (including social assistance and housing benefit) replacement rates (for two earnings levels and three family situations) for three durations of unemployment (1 year, 2&3 years, 4&5 years). Source: OECD, Benefits and Wages Database. Data coverage: 2001-2007. In order to have longer time series, we calculated r over the period running from 1970 to 2000, by using the growth rate of the historic OECD measure of benefit entitlements which is defined as the average of the gross unemployment benefit replacement rates for two earnings levels, three family situations and three durations of unemployment. Source: OECD, Benefits and Wages Database. Data coverage: 1970-2001 for all countries while data are unavailable for Korea.
- The worker bargaining power is measured by the collective **bargaining coverage**, $\text{BargCov}_{i,t}$, which corresponds to the employees covered by collective wage bargaining agreements as a proportion of all wage and salary earners in employment with the right to bargaining. Source: Data Base on Institutional Characteristics of Trade Unions, Wage Setting, State Intervention and Social Pacts, 1960-2010 (ICTWSS), version 3.0, Jelle Visser [2009]. Data coverage: 1970-2007 for AUS, AUT, CAN, DEU, DNK, FIN, GBR, IRL, ITA, JPN, SWE and USA, 1970-2005 for NLD and NOR, 1970-2002 for BEL and FRA, 1977-2004 for ESP and 2002-2006 for KOR.

Summary statistics of the labor market regulation indicators used in the empirical analysis are displayed in the three last columns Table 12.

A.2 Calibration of the Labor Market

To calibrate the labor market for the traded and the non traded sector, we need to estimate the sectoral unemployment rate, the job finding and the job destruction rate for each sector, and the sectoral labor market tightness. We provide below the source and construction of the data.

A.2.1 Source and Construction of Data

In this subsection, we first describe the data employed to calibrate some key features of OECD labor markets. Then, we present the dataset we use to estimate a set of sectoral search unemployment parameters. Summary statistics for the key indicators of the labor market are displayed in Table 13.

- **Sectoral unemployment rate**, u^j, is the number of unemployed workers U^j in sector $j = T, N$ as a share of the labor force $L^j + U^j$ in this sector. LABORSTA database from

Table 11: Construction of Variables and Data Sources

Variable	Countries covered	Period	Construction and aggregation	Database
Value added Y^T & Y^N (constant prices)	BEL, DEU, DNK, ESP, FIN, FRA, GBR, IRL, ITA, JPN (74-07), KOR, NLD, SWE, USA	1970-2007	T: Agriculture, Mining, Manufacturing, Transport, Finance Intermediation N: Electricity, Construction, Trade, Hotels, Real Estate, Personal Services	EU KLEMS
Value added P^TY^T & P^NY^N (current prices)	BEL, DEU, DNK, ESP, FIN, FRA, GBR, IRL, ITA, JPN (74-07), KOR, NLD, SWE, USA	1970-2007	T: Agriculture, Mining, Manufacturing, Transport, Finance Intermediation N: Electricity, Construction, Trade, Hotels, Real Estate, Personal Services	EU KLEMS
Labor L^T & L^N (total hours worked by persons engaged)	BEL, DEU, DNK, ESP, FIN, FRA, GBR, IRL, ITA, JPN (74-07), KOR, NLD, SWE, USA	1970-2007	T: Agriculture, Mining, Manufacturing, Transport, Finance Intermediation N: Electricity, Construction, Trade, Hotels, Real Estate, Personal Services	EU KLEMS
Labor compensation LAB^T & LAB^N (current prices)	BEL, DEU, DNK, ESP, FIN, FRA, GBR, IRL, ITA, JPN (74-07), KOR, NLD, SWE, USA	1970-2007	T: Agriculture, Mining, Manufacturing, Transport, Finance Intermediation N: Electricity, Construction, Trade, Hotels, Real Estate, Personal Services	EU KLEMS
Consumption C^T & C^N (constant prices)	BEL (95-07), DEU (91-07), DNK, ESP (95-07), FIN (75-07), FRA, ITA, GBR (90-07), IRL (96-07) JPN (80-07), KOR, NLD (80-07), SWE (93-07), USA	1990-2007	T: Food, Beverages, Clothing, Furnishings, Transport, Recreation, Other N: Housing, Health, Communication, Education, Restaurants, Recreation (Recreation is defined as 50% tradable and 50% non tradable)	COICOP
Government spending P^TG^T & P^NG^N (current prices)	BEL, DEU (91-07), DNK, ESP (95-07), FIN, FRA (95-07), GBR, IRL, ITA, JPN, KOR (00-07), NLD (95-07), SWE (95-07), USA	1990-2007	T: Energy, Agriculture, Manufacturing, Transport N: Public Services, Defense, Safety, Education, Health, Welfare, Housing, Environment, Recreation	OECD-FMI
Trade balance NX (constant prices)	BEL, DEU, DNK, ESP, FIN, FRA, GBR, IRL, ITA, JPN, KOR, NLD, SWE, USA	1970-2007	External balance of goods and services at current prices (source: OCDE) over price of traded goods (P^T)	authors' calculations
Price P^T & P^N (value added deflator)	BEL, DEU, DNK, ESP, FIN, FRA, GBR, IRL, ITA, JPN (74-07), KOR, NLD, SWE, USA	1970-2007	Value added at current prices (P^jY^j) over value added at constant prices (Y^j)	authors' calculations
Relative Price P (index 1995=100)	BEL, DEU, DNK, ESP, FIN, FRA, GBR, IRL, ITA, JPN (74-07), KOR, NLD, SWE, USA	1970-2007	Value added deflator of non traded goods (P^N) over value added deflator of traded goods (P^T)	authors' calculations
Wage W^T & W^N (nominal and per hour)	BEL, DEU, DNK, ESP, FIN, FRA, GBR, IRL, ITA, JPN (74-07), KOR, NLD, SWE, USA	1970-2007	Labor compensation (LAB^j) over total hours worked by hired persons (L^j)	authors' calculations
Relative Wage Ω (index 1995=100)	BEL, DEU, DNK, ESP, FIN, FRA, GBR, IRL, ITA, JPN (74-07), KOR, NLD, SWE, USA	1970-2007	Nominal wage in non tradables (W^N) over nominal wage in tradables (W^T)	authors' calculations
Sectoral Productivity A^T & A^N (index 1995=100)	BEL, DEU, DNK, ESP, FIN, FRA, GBR, IRL, ITA, JPN (74-07), KOR, NLD, SWE, USA	1970-2007	Measured by labor productivity $A^j = Y^j/L^j$	authors' calculations
Relative Productivity (index 1995 =100)	BEL, DEU, DNK, ESP, FIN, FRA, GBR, IRL, JPN (74-07), KOR, NLD, ESP, SWE, USA	1970-2007	Computed as the ratio A^T/A^N	authors' calculations

Table 12: Summary Statistics per Country

Countries	Variables					
	$\hat{p}$	$\hat{\omega}$	$\hat{a}^T - \hat{a}^N$	r	BargCov	EPL$_{adj}$
	(1)	(2)	(3)	(4)	(5)	(6)
AUS	0.91	-0.27	1.83	0.50	0.71	1.21
AUT	1.97	-0.72	2.89	0.50	0.97	2.48
BEL	2.26	-0.04	2.53	0.67	0.94	1.65
CAN	0.54	-0.42	1.55	0.54	0.36	0.81
DEU	0.85	-0.62	1.62	0.72	0.69	2.36
DNK	0.78	-0.91	2.21	0.61	0.82	1.93
ESP	2.62	-0.97	3.67	0.41	0.76	2.04
FIN	2.56	-0.78	4.22	0.59	0.86	2.02
FRA	2.14	-0.98	2.68	0.47	0.85	2.11
GBR	1.57	-0.50	2.31	0.63	0.45	1.02
IRL	2.55	-0.88	4.37	0.54	0.58	1.32
ITA	2.02	-0.92	3.05	0.08	0.83	2.53
JPN	2.60	-0.44	2.68	0.51	0.24	1.49
KOR	3.35	-2.15	6.49	0.38	0.11	1.98
NLD	1.86	-0.39	2.38	0.67	0.85	2.60
NOR	-0.37	-0.39	1.96	0.43	0.70	2.06
SWE	2.34	-0.11	2.76	0.48	0.89	2.31
USA	1.74	-0.23	2.64	0.26	0.20	0.24
Average	1.79	-0.65	2.88	0.50	0.66	1.79

Notes: $\hat{p}$ is the relative price of non tradables average growth rate, $\hat{\omega}$ is the relative wage of non tradables average growth rate and $(\hat{a}^T - \hat{a}^N)$ is the average growth rate of the labor productivity differential between tradables and non tradables. Data coverage for $\hat{p}$, $\hat{\omega}$ and $(\hat{a}^T - \hat{a}^N)$ is 1970-2007 (1974-2007 for Japan). r is the unemployment benefit replacement rate. Data coverage: 1970-2007 (2001-2007 for KOR). BargCov is the collective bargaining coverage. Data coverage: 1970-2007 for AUS, AUT, CAN, DEU, DNK, FIN, GBR, IRL, ITA, JPN, SWE and USA, 1970-2005 for NLD and NOR, 1970-2002 for BEL and FRA, 1977-2004 for ESP and 2002-2006 for KOR. EPL$_{adj}$ is the employment protection legislation index adjusted with the share of permanent workers in the economy. Data coverage: 1985-2007 (1990-2007 for KOR).

the International Labour Organization (ILO) provides annual data for unemployed and employed workers at the 1-digit ISIC-rev.3 level. To construct L^j and U^j for $j = T, N$, we map the classification used previously to compute series for sectoral wages, prices and real labor productivity indexes (see section A.1) into the 1-digit ISIC-rev.3 classification used by the LABORSTA database. The mapping was clear for all industries except for "Not classifiable by economic activity" (1-digit ISIC-Rev.3 code: X) when constructing L^j and U^j, and, "Unemployed seeking their first job" to identify U^j. These two categories have been split between tradables and non tradables according to the shares of total unemployment (excluding the two sectors) between tradables and non tradables by year and country. In a few rare cases, the sum of sectoral employment provided by ILO did not correspond to total unemployment. These differences were usually due to missing data for some industries in the sectoral databases. In these cases, we added these differences in level, keeping however the share of each sector constant. In Table 13 we provide a overview of the classifications used to construct traded and non traded sectors variables. Once industries have been classified as traded or non traded, series for unemployed and employed workers are constructed by adding unemployed and employed workers of all sub-industries k in sector $j = T, N$ in the form $U^j = \sum_{k \in j} U_k$ and $L^j = \sum_{k \in j} L_k$. Data coverage: AUS (1995-2007), AUT (1994-2007), BEL (2001-2007), CAN (1987-2007), DEU (1995-2007), DNK (1994-1998 and 2002-2004), ESP (1992-2007), FIN (1995-2007), GBR (1988-2007), IRL (1986-1997), ITA (1993-2007), JPN (2003-2007), KOR (1992-2007), SWE (1995-2007) and USA (2003-2007). Data for unemployed workers by economic activity are not available for FRA, NLD and NOR.

- **Labor market tightness**, θ^j for $j = T, N$, is calculated as the ratio of employment vacancies in sector j (V^j) to the number of unemployed workers in that sector (U^j). To construct the variables θ^j, we collect information on job vacancies and unemployed workers by economic activity. Sources for V^j: Job Openings and Labor Turnover Survey (JOLTS) provided by the Bureau of Labor Statistics (BLS) for USA and Eurostat database (NACE 1-digit) for a range of European Countries, Labour Market Statistics from the Office for National Statistics for the UK. Sources for U^j: Current Population Survey (CPS) published by the BLS for USA and LABORSTA (ILO) for European Countries.[58] As shown in Table 13, the level of detail in the definition of traded and non traded sectors differs across databases in two dimensions. First, the number of items to split disaggregated data varies across nomenclatures from a low eleven categories in the Eurostat database to a high of eighteen items in the LABORSTA database. Second, the definitions of items are not harmonized across the different sets of data. To generate sectoral variables in a consistent and uniform way, series on disaggregated data for vacancies and unemployed workers are added up to form traded and non traded sectors following, as close as possible, the classification we used for value added, hours worked and labor compensation. Once industries have been classified as traded or non traded, series for employment vacancies (unemployed workers resp.) are constructed by adding job openings (unemployed workers resp.) of all sub-industries k in sector $j = T, N$ in the form $V^j = \sum_{k \in j} V_k$ ($U^j = \sum_{k \in j} U_k$ resp.). Data coverage for V^j and U^j: AUT (2004-2005), DEU (2006-2007), FIN (2002-2007), GBR (2001-2007), SWE (2005-2007) and USA (2001-2007).

For reason of space, Table 13 does not provide the classification between tradables and non tradables for job vacancies for the United Kingdom. The classification is detailed below. The Office for National Statistics provides series for the UK that cover 19 sectors, according to SIC 2007 classification. Sectors have been aggregated into tradables (Financial and insurance activities; Information and communication; Manufacturing; Mining and quarrying; Transport and storage) and non tradables (Accomodation and food service activities; Administrative and support service activities; Arts, entertainment and recreation; Construction; Education; Electricity, gas, steam and air conditioning supply; Human health and social work activities; Other service activities; Public administration and defense; Compulsory social security; Real estate activities; Water supply, sewerage, waste and remediation activities; Wholesale and retail trade; repair of motor vehicles and motor cycles).

A.2.2 The Methodology

In this section, we present the approach we adopted to measure the job finding and employment exit rates by using readily accessible data. We apply the methodology developed by Shimer [2012] who assume that the labor force is fixed. Applying the same logic to our two-sector model, we need to impose that the labor force F^j is fixed at a sectoral level. The implication of such an assumption is twofold. First, we explicitly assume that there are no movements into and out of the labor force. Second, we assume that there are no movements between the traded and the non traded sectors. Reassuringly, Shimer [2012] shows that a two-state model where workers simply transit between employment and unemployment does a good job of capturing unemployment fluctuations. Because the reallocation of labor across sectors is relatively low, the second assumption should not substantially affect the results. In particular, Shimer [2012] finds that the job finding rate to worker averaged 0.44 over the post-war period for the U.S., while our own estimates indicate that the job finding rate averages about 0.40 from 2003 to 2007.

The presentation below borrows heavily from Elsby, Hobijn, and Sahin [2013]. We assume that during period t, all unemployed workers find a job according to a Poisson process with arrival rate $m^j(t) = -ln\left(1 - M^j(t)\right)$ and all employed workers lose their job according to a Poisson process with arrival rate $s^j(t) = -ln\left(1 - S^j(t)\right)$. We refer to $m^j(t)$ and $s^j(t)$ as the job finding and job destruction rates in sector j and to $M^j(t)$ and $S^j(t)$ as the corresponding probabilities.

The evolution over time of the unemployed workers, which we denote by $U^j(t)$, can be written as:

$$\dot{U}^j(t) = s^j(t)L^j(t) - m^j(t)U^j(t), \tag{59}$$

where $L^j(t)$ is employment in sector j; the evolution over time of the unemployed workers can be written alternatively by using the fact that $L^j(t) = F^j - U^j(t)$

$$\dot{U}^j(t) = s^j(t)\left(F^j - U^j(t)\right) - m^j(t)U^j(t), \tag{60}$$

where $s^j(t)$ is the monthly rate of inflow into unemployment, $m^j(t)$ is the monthly outflow rate from unemployment, and t indexes months.

Collecting terms, assuming that the job destruction rate and the job finding rate are constant within years and solving eq. (60), pre-multiplying by $e^{-(m+s)\tau}$, and integrating over the time interval $[t-12, t]$, leads to the temporal path for unemployed workers:

$$U^j(t) = \psi^j(t)\tilde{u}^j(t)F^j(t) + (1 - \psi(t))\,U^j(t-12), \tag{61}$$

[58]The JOLTS and CPS databases provide (not seasonally adjusted) monthly data on vacancies and unemployed workers. We convert monthly data series into a annual data series by summing the twelve monthly data points.

Table 13: Summary of Sectoral Classifications

Sector	EU KLEMS/STAN	LABORSTA Employment	LABORSTA Unemployment	JOLTS (BLS)	CPS (BLS)	EUROSTAT
Tradables	Agriculture, Hunting, Forestry and Fishing (AtB)	Agriculture, Hunting, Forestry and Fishing (A-B)	Agriculture, Hunting, Forestry (A) Fishing (B)		Agriculture	Agriculture and fishing
	Mining and Quarrying (C)	Mining and Quarrying (C)	Mining and Quarrying (C)	Mining and logging	Mining and quarrying	Mining and quarrying
	Total Manufacturing (D)	Manufacturing (D)	Manufacturing (D)	Manufacturing	Manufacturing	Manufacturing
	Transport and Storage and Communication (I)	Transport, Storage and Communications (I)	Transport, Storage and Communications (I)	Transportation	Transportation and utilities	Transport, storage and communication
				Information	Information	
	Financial Intermediation (J)	Financial Intermediation (J)	Financial Intermediation (J)	Finance and insurance	Financial activities	Financial intermediation
			Unemployed seeking their first job			
Non Tradables	Electricity, Gas and Water Supply (E)	Electricity, Gas and Water Supply (E)	Electricity, Gas and Water Supply (E)			Electricity, gas and water supply
	Construction (F)	Construction (F)	Construction (F)	Construction	Construction	Construction
	Wholesale and Retail Trade (G)	Wholesale and Retail Trade (G)	Wholesale and Retail Trade (G)	Wholesale trade	Wholesale and retail trade	Wholesale and retail trade
				Retail trade		
	Hotels and Restaurants (H)	Hotels and Restaurants (H)	Hotels and Restaurants (H)			Hotels and restaurants
	Real Estate, Renting and Business Activities (K)	Real Estate, Renting and Business Activities (K)	Real Estate, Renting and Business Activities (K)	Real estate and rental		Real estate, renting and business activities
				Business services	Business services	
	Community Social and Personal Services (LtQ)	Public Adm., Defence and Compulsory Social Security (L)	Public Adm., Defence and Compulsory Social Security (L)	Government	Government workers	Public adm. and community services
		Education (M)	Education (M)	Education and health	Education and health services	
		Health and Social Work (N)	Health and Social Work (N)			
		Other Community, Social and Personal Service Activities (O)	Other Community, Social and Personal Service Activities (O)	Leisure and hospitality	Leisure and hospitality	
		Households with Employed Persons (P)	Households with Employed Persons (P)			
		Extra-Territorial Organizations and Bodies (Q)	Extra-Territorial Organizations and Bodies (Q)			
		Not classifiable by economic activity (X)	Not classifiable by economic activity (X)	Other services	Other services	
			Unemployed seeking their first job			
Unclassified					Self-employed, unincorporated and unpaid family workers	

where $\tilde{u}^j$ is the long-run unemployment rate in sector j:

$$\tilde{u}^j(t) = \frac{s^j(t)}{s^j(t) + m^j(t)}, \tag{62}$$

and ψ^j is the annual rate of convergence to the long-run sectoral unemployment rate:

$$\psi^j(t) = 1 - e^{-\left(s^j(t)+m^j(t)\right)12}. \tag{63}$$

To infer the monthly outflow probability $M^j(t)$ and then the monthly job finding rate $m^j(t)$, we follow Shimer [2012] and write the dynamic equations of sectoral unemployment and sectoral short term unemployment, i.e.,

$$\dot{U}^j(t+d) = s^j(t)L^j(t) - m^j(t)U^j(t),, \tag{64a}$$
$$\dot{U}^{j,<d}(t+d) = s^j(t)L^j(t) - m^j(t)U^{j,<d}(t), \tag{64b}$$

where $U^{j,<d}(t+d)$ denotes short-term unemployment, i.e., the stock of unemployed workers who are employed at some time $\tau \in]t, t+d]$ but lose their job and thus are unemployed at time $t+d$; hence, by construction, $U^{j,<d}(t) = 0$ since all short-term unemployed workers were employed at time t. Combining (64a) and (64b) to eliminate $s^j(t)L^j(t)$ leads to a dynamic equation relating changes of unemployment to changes of short-term unemployment:

$$\dot{U}^j(t+d) = \dot{U}^{j,<d}(t+d) - m^j(t)\left(U^j(t) - U^{j,<d}(t)\right). \tag{65}$$

Solving eq. (65) above by integrating over $[t-d, t]$, and using the fact that at time t, short-term unemployment is such that $U^{j,<d}(t) = 0$, leads to:

$$U^j(t+d) = U^{j,<d}(t+d) + e^{-m^j(t)\,.d}U^j(t).$$

Inserting $e^{-m^j(t)\,.d} = \left(1 - M^{j,<d}(t)\right)$ where $M^{j,<d}$ is the probability that an unemployed worker exits unemployment within d months, one obtains:

$$U^j(t+d) - U^j(t) = U^{j,<d}(t+d) - M^{j,<d}(t)U^j(t). \tag{66}$$

Eq. (66) states that the change of unemployment in sector j is equal to the inflows into unemployment $U^{j,<d}(t+d)$ of workers who were employed at time t but are unemployed at time $t+d$ less the number of unemployed workers who find a job $M^{j,<d}(t)U^j(t)$. Solving (66) for $M^{j,<d}(t)$, it is possible to write the probability that an unemployed worker exits unemployment within d months as

$$M^{j,<d}(t) = 1 - \left[\frac{U^j(t+d) - U^{j,<d}(t+d)}{U^j(t)}\right]. \tag{67}$$

The probability of finding a job within d months given by eq. (67) can be mapped as the monthly job finding rate for unemployment duration $d = 1, 3, 6, 12$:

$$m^{j,<d}(t) = -\frac{1}{d}\ln\left(1 - M^{j,<d}(t)\right). \tag{68}$$

To estimate the monthly job finding rate, we use the duration of unemployment lower than one month. In this configuration, the probability of finding a job can be rewritten as follows:

$$M^{j,<1}(t) = 1 - \left[\frac{U^j(t) - U^{j,<1}(t)}{U^j(t-1)}\right]$$

or alternatively

$$1 - M^{j,<1}(t) = \frac{U^j(t) - U^{j,<1}(t)}{U^j(t-1)}. \tag{69}$$

Since $U^j(t-1)$ corresponds to monthly unemployment, we have to convert annual data on a monthly basis:

$$U^j(t-1) = \left(U^j(t-12)\right)^{1/12}\left(U^j(t)\right)^{11/12}. \tag{70}$$

Using (68) with $d = 1$, the monthly job finding rate is:

$$m^{j,<1}(t) = -\ln\left(U^j(t) - U^{j,<1}(t)\right) + \ln\left(U^j(t-1)\right), \tag{71}$$

where the construction of $U^j(t-1)$ is given by eq. (70) while the same logic applies to $U^j(t)$.

Since series for unemployment by duration are expressed in percentage, we define $\alpha^{j,<1}(t)$ the share of unemployment less than one month among total unemployment as follows:

$$\alpha^{j,<1}(t) = \frac{U^{j,<1}(t)}{U^j(t)}. \tag{72}$$

Because the share of short-term unemployment is not available by economic activity, we assume that $\alpha^{j,<1}(t)$ is identical across sectors:

$$\alpha^{j,<1}(t) = \alpha^{T,<1}(t) = \alpha^{N,<1}(t). \tag{73}$$

The job destruction rate can be estimated by solving this equation:

$$U^j(t) = \psi^j(t)\frac{s^j(t)}{s^j(t)+m^{j,<1}(t)}\left(U^j(t)+L^j(t)\right)+\left(1-\psi^j(t)\right)U^j(t-1), \tag{74}$$

where ψ^j is the monthly rate of convergence to the long-run sectoral unemployment rate:

$$\psi^j(t) = 1-e^{-\left(s^j(t)+m^{j,<1}(t)\right)}. \tag{75}$$

A.2.3 Computation of the job finding rate and the job separation rate at a sectoral level

To estimate the monthly job finding rate, $m^{j,<1}$, and the job destruction rate, s^j, for $j = T, N$, we proceed as follows:

- We estimate $\alpha^{<1}(t) = \alpha^{j,<1}(t) = \frac{U^{<1}(t)}{U(t)}$ where $U^{<1}(t)$ is unemployment of duration less than one month.
- Using the fact that $U^{j,<1}(t) = \alpha^{<1}(t)U^j(t)$, the probability of finding a job is

$$M^{j,<1}(t) = 1-\left[\frac{\left(1-\alpha^{<1}(t)\right)U^j(t)}{U^j(t-1)}\right], \tag{76}$$

  where $U^j(t-1)$ corresponds to monthly unemployment which is calculated as follows $U^j(t-1) = \left(U^j(t-12)\right)^{1/12}\left(U^j(t)\right)^{11/12}$ by using annual data.
- The monthly job finding rate is:

$$m^{j,<1}(t) = -\ln\left(1-M^{j,<1}(t)\right) \tag{77}$$

- The job destruction rate can be estimated by solving the following equation:

$$U^j(t) = \psi^j(t)\frac{s^j(t)}{s^j(t)+m^{j,<1}(t)}\left(U^j(t)+L^j(t)\right)+\left(1-\psi(t)\right)U^j(t-1), \tag{78}$$

  where ψ^j is the monthly rate of convergence to the long-run sectoral unemployment rate:

$$\psi^j(t) = 1-e^{-\left(s^j(t)+m^j(t)\right)}. \tag{79}$$

To compute $m^{j,<1}$ and s^j, we need series for unemployment by economic activity in order to construct U^j, and unemployment less than 1 month in order to estimate $\alpha^{<1}(t)$. For unemployment at the sectoral level, data are taken from ILOSTAT database (ILO) while unemployment less than one month is provided by OECD for unemployment by duration. Data coverage: AUS (1995-2007), AUT (1994-2007), BEL (2001-2007), CAN (1987-2007), DEU (1995-2007), DNK (1994-1998 and 2002-2004), ESP (1992-2007), FIN (1991-2007), GBR (1988-2007), IRL (1986-1997), ITA (1993-2007), JPN (2003-2007), SWE (1995-2007) and USA (2003-2007). Because we calibrate the model so that the initial steady state is consistent with the empirical properties of each OECD economy while the series for the sectoral job separation rates are computed when the economy is out of the steady-state, we need to compute values for s^j which are consistent with the steady-state sectoral unemployment rate $\tilde{u}^j = \frac{s^j}{s^j+m^j}$ given the computed value for m^j. The two first columns in Table 14 show the actual values for the sectoral unemployment rates while columns 3 and 4 give the values for steady-state sectoral unemployment rates computed by using its long-run equilibrium $\tilde{u}^j = \frac{s^j}{m^j+s^j}$ where the job finding rate m^j is taken from columns 5 and 7 of Table 10 and the job destruction rate has been computed by solving eq. (78). The two last columns of Table 14 show the difference between the actual and the predicted value. Reassuringly, because computed values for m^j and s^j by using (77) and (78) are averaged over a long enough time horizon so that the unemployment rate

Table 14: Comparison of Actual Values with Calculated Values for the Sectoral Unemployment Rates

Country	Actual		Calculated		Error	
	u^T	u^N	$\tilde{u}^T$	$\tilde{u}^N$	$u^T - \tilde{u}^T$	$u^N - \tilde{u}^N$
	(1)	(2)	(3)	(4)	(5)	(6)
AUS	0.072	0.062	0.084	0.066	-0.012	-0.004
AUT	0.037	0.044	0.036	0.037	0.001	0.007
BEL	0.077	0.079	0.075	0.078	0.002	0.001
CAN	0.082	0.084	0.086	0.086	-0.004	-0.002
DEU	0.101	0.091	0.100	0.094	0.001	-0.003
DNK	0.064	0.061	0.067	0.060	-0.003	0.001
ESP	0.147	0.161	0.146	0.155	0.001	0.006
FIN	0.087	0.118	0.088	0.119	-0.001	-0.001
GBR	0.073	0.066	0.071	0.068	0.002	-0.002
IRL	0.130	0.154	0.132	0.144	-0.002	0.010
ITA	0.094	0.098	0.104	0.097	-0.010	0.001
JPN	0.033	0.033	0.024	0.025	0.009	0.008
SWE	0.056	0.060	0.043	0.045	0.013	0.015
USA	0.048	0.053	0.047	0.052	0.001	0.001

should have reached its long-run value, actual and predicted values are close in most of the cases, except for Sweden, Australia and Italy (for u^T), and Ireland (for u^N). The values for sectoral job destruction rates shown in columns 6 and 8 of Table 10 are thus calculated by using the long-run equilibrium expression for the sectoral unemployment rate, i.e.,

$$s^j = \frac{m^j u^j}{1-u^j}, \tag{80}$$

where u^j is taken from columns 2 and 3 of Table 10 and m^j is taken from columns 5 and 7 of Table 10. Computed values for s^j using (80) are shown in columns 6 and 8 of Table 10.

For France, Korea, the Netherlands, and Norway, data are not available to compute the job finding and the job separation rate. We proceed as follows to get estimates of m and s when calibrating the model for each economy:

- Because data for unemployment by economic activity are not available for FRA, NLD and NOR, estimates for the job finding rate $m = m^j$ are taken from Hobijn and Sahin [2009]. Note that estimates are not available at a sectoral level so that we have to assume that the job finding rate is identical across sectors, i.e., $m^j = m$. Building on estimates by Hobijn and Sahin [2009], we set $m = 6.7\%$ for France (1975-2004), $m = 4.7\%$ for the Netherlands (1983-2004), and $m = 30.5\%$ for Norway (1983-2004). To compute the job separation rate, we use the steady-state expression for the unemployment rate $u = \frac{s}{s+m}$ where the unemployment rate is averaged over the appropriate period, i.e., 1975-2004 for France, 1983-2004 for the Netherlands and 1983-2004 for Norway. Series for harmonized unemployment rates are taken from Labor Force Survey, OECD.
- While we can construct series for unemployment by economic activity for Korea, series for unemployment by duration is not provided by the OECD for this economy. We thus average the job finding rates taken from Chang et al. [2004] over 1993-1994, i.e., $m = 26.2\%$ and compute the job destruction rate by using the steady-expression for the unemployment rate $u^j = \frac{s^j}{s^j+m}$ where u^j is the sectoral unemployment rate calculated by using the LABORSTA database from ILO.

A.3 Elasticity of substitution in consumption (ϕ): Empirical Strategy

When including physical capital investment and denoting recruiting costs by $F \equiv \kappa^T V^T + \kappa^N V^N$, according to the goods market equilibrium, we have:

$$\frac{Y^T - NX - I^T - G^T - F}{Y^N - I^N - G^N} = \frac{C^T}{C^N}, \tag{81}$$

where we used the fact that $\dot{B} - r^\star B = NX$ with B the net foreign asset position and NX net exports. Inserting the optimal rule for intra-temporal allocation of consumption (15), i.e., $\frac{C^T}{C^N} = \left(\frac{\varphi}{1-\varphi}\right) P^\phi$, into (81) leads to

$$\frac{Y^T - NX - I^T - G^T - F}{Y^N - I^N - G^N} = \left(\frac{\varphi}{1-\varphi}\right) P^\phi. \tag{82}$$

According to the market clearing condition, we could alternatively use data for consumption or for sectoral value added along with times series for its demand components to estimate ϕ. Unfortunately, classifications for valued added by industry and for consumption by items are different (because nomenclatures are different) and thus it is most likely that C^T differs from $Y^T - NX - G^T - I^T - F$, and C^N from $Y^N - G^N - I^N$ as well. Because time series for traded and non traded consumption display a short time horizon for half countries of our sample while data for sectoral value added and net exports are available for the 18 OECD countries of our sample over the period running from 1970 to 2007 (except for Japan: 1974-2007), we find appropriate to estimate ϕ by computing $Y^T - NX - E^T$ and $Y^N - E^N$ where $E^T \equiv G^T + I^T + F$ and $E^N \equiv G^N + I^N$. Yet, a difficulty shows up because the classification adopted to split government spending and investment expenditure into traded and non traded items is different from that adopted to break down value added into traded and non traded components. Moreover, the time horizon is short at a disaggregated level for most of the countries, especially for time series of G^j. To overcome these difficulties, we proceed as follows. Denoting the ratio of $E^T \equiv G^T + I^T + F$ to traded value added adjusted with net exports at current prices by $\upsilon_{E^T} = \frac{P^T E^T}{P^T Y^T - P^T NX}$, and denoting the ratio of $E^N \equiv G^N + I^N$ to non traded value added at current prices by $\upsilon_{E^N} = \frac{P^N E^N}{P^N Y^N}$, the goods market equilibrium (82) can be rewritten as follows:

$$\frac{\left(P^T Y^T - P^T NX\right)\left(1 - \upsilon_{E^T}\right)}{P^N Y^N \left(1 - \upsilon_{E^N}\right)} = \left(\frac{\varphi}{1-\varphi}\right) P^{\phi - 1},$$

or alternatively

$$\frac{\left(Y^T - NX\right)\left(1 - \upsilon_{E^T}\right)}{Y^N \left(1 - \upsilon_{E^N}\right)} = \left(\frac{\varphi}{1-\varphi}\right) P^{\phi}. \tag{83}$$

Setting

$$\alpha \equiv \ln \frac{\left(1 - \upsilon_{E^N}\right)}{\left(1 - \upsilon_{E^T}\right)} + \ln\left(\frac{\varphi}{1-\varphi}\right), \tag{84}$$

and taking logarithm, eq. (83) can be rewritten as follows:

$$\ln\left(\frac{Y^T - NX}{Y^N}\right) = \alpha + \phi \ln P. \tag{85}$$

Indexing time by t and countries by i, and adding an error term μ, we estimate ϕ by exploring the following empirical relationship:

$$\ln\left(\frac{Y^T - NX}{Y^N}\right)_{i,t} = f_i + f_t + \alpha_i t + \phi_i \ln P_{i,t} + \mu_{i,t}, \tag{86}$$

where f_i captures the country fixed effects, f_t are time dummies, and $\mu_{i,t}$ are the i.i.d. error terms. Because the term (84) is composed of ratios which may display a trend over time, we add country-specific trends, as captured by $\alpha_i t$. **Eq. (86) corresponds to eq. (53) in the text**.

Instead of using time series for sectoral value added, we can alternatively make use of series for sectoral labor compensation. Multiplying both sides by $\frac{P^T}{P^N}$ and then by $\frac{\rho^T}{\rho^N}$ with $\rho^j = \frac{W^j L^j}{P^j Y^j}$ the sectoral labor income share, eq. (83) can be rewritten as follows

$$\ln\left(\frac{W^T L^T - \rho^T P^T NX}{W^N L^N}\right) = \eta + (\phi - 1)\ln P. \tag{87}$$

where

$$\eta \equiv \ln \frac{\left(1 - \upsilon_{E^N}\right)}{\left(1 - \upsilon_{E^T}\right)} + \ln\left(\frac{\varphi}{1-\varphi}\right) + \ln \frac{\rho^T}{\rho^N}. \tag{88}$$

Indexing time by t and countries by i, and adding an error term μ, we estimate ϕ by exploring the following empirical relationship:

$$\ln\left(\gamma^T/\gamma^N\right)_{i,t} = g_i + g_t + \eta_i t + \delta_i \ln P_{i,t} + \zeta_{i,t}, \tag{89}$$

where $\delta_i = (\phi_i - 1)$; g_t are time dummies which capture common macroeconomic shocks. Because η_i is composed of preference parameters (i.e., φ), and (logged) ratios which may display trend over time, we introduce country fixed effects g_i, and add country-specific trends, as captured by $\eta_i t$. Once we have estimated δ_i, we can compute $\hat{\phi}_i = \hat{\delta}_i + 1$ where a hat refers to point estimate in this context. **Eq. (89) corresponds to eq. (54) in the text**.

Table 15: Panel Unit Root Tests (second generation)

Test	Stat	Variables			
		ω	p	$a^T - a^N$	$p - (a^T - a^N)$
Bai and Ng [2002]	$Z_{\hat{e}}^c$	0.267	0.151	0.038	0.530
	$P_{\hat{e}}^c$	0.251	0.150	0.050	0.498
Choi [2001]	P_m	0.000	0.988	0.992	0.407
	Z	0.053	1.000	1.000	0.653
	$L^\star$	0.047	1.000	1.000	0.662
Pesaran [2007]	$CIPS$	0.010	0.320	0.450	0.015
	$CIPS^\star$	0.010	0.320	0.450	0.015
Chang [2002]	S_N	1.000	1.000	1.000	1.000

Notes: For all tests, the null of a unit root is not rejected if p-value ≥ 0.05 at a 5% significance level. $\hat{r}$ is the estimated number of common factors. For the idiosyncratic components, $P_{\hat{e}}^c$ is a Fisher's type statistic based on p-values of the individual ADF tests. Under H_0, $P_{\hat{e}}^c$ has a χ^2 distribution. $Z_{\hat{e}}^c$ is the standardized Choi's type statistic. Under H_0, $Z_{\hat{e}}^c$ has a $N(0,1)$ distribution. For the idiosyncratic components, the estimated number of independent stochastic trends in the common factors is reported. The first estimated value is derived from the filtered test MQ_c and the second one is derived from the corrected test MQ_f. The P_m test is a modified Fisher's inverse chi-square test. The Z test is an inverse normal test. The $L^\star$ test is a modified logit test. All these three statistics have a standard normal distribution under H_0. $CIPS$ is the mean of individual Cross sectionally ADF statistics (CADF). $CIPS^\star$ denotes the mean of truncated individual CADF statistics. The S_N statistic corresponds to the average of individual non-linear IV t-ratio statistics. It has a $N(0,1)$ distribution under H_0. Corresponding p-values are in parentheses.

B Empirical results

B.1 Robustness Check for Panel Unit Root Tests

The common feature of first generation tests is the restriction that all cross-sections are independent. We also consider some second generation unit root tests that allow cross-unit dependencies. We consider the tests developed by: i) Bai and Ng [2002] based on a dynamic factor model, ii) Choi [2001] based on an error-component model, iii) Pesaran [2007] based on a dynamic factor model and iv) Chang [2002] who proposes the instrumental variable nonlinear test. The results of second generation unit root tests are shown in Table 15.

In all cases, except for the Choi [2001] and Pesaran's [2007] tests applied to ω and $p-(a^T-a^N)$, we fail to reject the presence of a unit root in the relative price, the relative wage, the productivity differential, and the difference $a^T - a^N$, when cross-unit dependencies are taken into account.

B.2 Robustness Check for Cointegration Tests

To begin with, we report the results of parametric and non parametric cointegration tests developed by Pedroni ([1999]), ([2004]). Cointegration tests are based on the estimated residuals of equations (5) and (6). Table 16 reports the tests of the null hypothesis of no cointegration. All Panel tests reject the null hypothesis of no cointegration between p and $a^T - a^N$ at the 1% significance level while three Panel tests reject the null hypothesis of no cointegration between ω and $a^T - a^N$ at the 5% significance level. Group-mean parametric t-test confirm cointegration between p and the labor productivity differential and between ω and $a^T - a^N$ at 5% and 1% significance level, respectively, while group-mean non parametric t-tests are somewhat less pervasive. Pedroni [2004] explores finite sample performances of the seven statistics. The results reveal that group-mean parametric t-test is more powerful than other tests in finite samples. By and large, panel cointegration tests provide evidence in favor of cointegration between the relative price and relative productivity, and between the relative wage and relative productivity.

As robustness checks, we compare our group-mean FMOLS estimates and group-mean DOLS estimates with one lag ($q = 1$), with alternative estimators. First, we consider the group-mean DOLS estimator with 2 lags ($q = 2$) and 3 lags ($q = 3$). Second, we estimate cointegration relationships (5) and (6) using the panel DOLS estimator (Mark and Sul [2003]). We also use alternative econometric techniques to estimate cointegrating relationships (4): the dynamic fixed effects estimator (DFE), the mean group estimator (MG, Pesaran and Smith [1995]), the pooled mean group estimator (PMG, Pesaran et al. [1999]). All results are displayed in Table 17 and show that estimates of $\hat{\beta}$ and $\hat{\gamma}$ are close to those shown in Table 2 of the paper, except for the dynamic fixed effects estimator which suggests a fall in ω of 0.1% instead of 0.2%.

Table 16: Panel cointegration tests results (p-values)

	wage equation	price equation
	eq. (5)	eq. (6)
Panel tests		
Non-parametric ν	0.000	0.000
Non-parametric ρ	0.012	0.003
Non-parametric t	0.004	0.002
Parametric t	0.046	0.000
Group-mean tests		
Non-parametric ρ	0.388	0.449
Non-parametric t	0.167	0.220
Parametric t	0.016	0.001

Notes: The null hypothesis of no cointegration is rejected if the p-value is below 0.05 (0.10 resp.) at 5% (10% resp.) significance level.

Table 17: Alternative Cointegration Estimates of β and γ

	Relative wage eq. (5)		Relative price eq. (6)	
	$\hat{\beta}$	$t(\beta = 0)$	$\hat{\gamma}$	$t(\gamma = 1)$
DOLS ($q = 2$)	-0.223^a (-27.69)	0.000	0.658^a (77.95)	0.000
DOLS ($q = 3$)	-0.220^a (-26.77)	0.000	0.673^a (79.22)	0.000
DOLS ($q = 4$)	-0.218^a (-26.51)	0.000	0.678^a (84.96)	0.000
DFE	-0.105^b (-2.51)	0.006	0.697^a (13.55)	0.000
MG	-0.145^a (-7.43)	0.000	0.608^a (17.25)	0.000
PMG	-0.164^a (-10.59)	0.000	0.668^a (31.03)	0.000
Panel DOLS ($q = 1$)	-0.214^a (-6.32)	0.000	0.621^a (22.39)	0.000
Panel DOLS ($q = 2$)	-0.216^a (-6.85)	0.000	0.620^a (22.62)	0.000
Panel DOLS ($q = 3$)	-0.213^a (-6.42)	0.000	0.624^a (23.88)	0.000

Notes: All regressions include country fixed effects. Heteroskedasticity and autocorrelation consistent t-statistics are reported in parentheses. ^{a} denotes significance at 1% level. The columns $t(\beta) = 0$ and $t(\gamma) = 1$ report the p-value of the test of $H_0 : \beta = 0$ and $H_0 : \gamma = 1$ respectively.

C First-Order Conditions

It is worthwhile noticing that we employ below in the formal analysis the term "short-run static solutions". This terminology refers to solutions of static optimality conditions which are inserted in dynamic optimality conditions in order to analyze the equilibrium dynamics. The term "short-run" refers to first-order conditions, and the term "static" indicates that the solution holds at each instant of time, and thus in the long-run.

C.1 Households

We set

$$\phi(t) \equiv \frac{1}{1-\frac{1}{\sigma_C}} C(t)^{1-\frac{1}{\sigma_C}} + v^T \left(L^T(t) + U^T(t)\right) + v^N \left(L^N(t) + U^N(t)\right), \tag{90}$$

where $v^j \left(L^j(t) + U^j(t)\right)$ is the disutility function from working and searching efforts. We drop the time index when it is obvious. The current-value Hamiltonian for the representative household's optimization problem is:

$$\begin{aligned} \mathcal{H}^H &= \phi + \lambda \left[r^\star A + W^T L^T + R^T U^T + R^N U^N - P_C(P) C - T\right] \\ &+ \xi^{T,\prime}\left[m^T U^T - s^T L^T\right] + \xi^{N,\prime}\left[m^N U^N - s^N L^N\right], \end{aligned} \tag{91}$$

where A, L^j $(j = T, N)$ are state variables; λ, $\xi^{j,\prime}$ (with $j = T, N$) are the corresponding co-state variables; C and U^j are the control variables.

Assuming that the representative agent takes m as given, first-order conditions for households are:

$$C = (P_C \lambda)^{-\sigma_C}, \tag{92a}$$

$$-v_F^T \left(L^T + U^T\right) = m^T \xi^{T,\prime} + R^T \lambda, \tag{92b}$$

$$-v_F^N \left(L^N + U^N\right) = m^N \xi^{N,\prime} + R^N \lambda, \tag{92c}$$

$$\dot{\lambda} = \lambda\left(\rho - r^\star\right), \tag{92d}$$

$$\dot{\xi}^{T,\prime} = \left(s^T + \rho\right)\xi^{T,\prime} - \left[\lambda W^T + v_F^T \left(L^T + U^T\right)\right], \tag{92e}$$

$$\dot{\xi}^{N,\prime} = \left(s^N + \rho\right)\xi^{N,\prime} - \left[\lambda W^N + v_F^N \left(L^N + U^N\right)\right], \tag{92f}$$

where $\xi^{j,\prime}$ (with $j = T, N$) is the utility value of the marginal job and λ the marginal utility of wealth.

Since $\xi^{j,\prime}$ represents the utility value from an additional job and $\bar{\lambda}$ corresponds to the marginal utility of wealth, the pecuniary value of the marginal job is $\xi^j(\tau) \equiv \frac{\xi^{j,\prime}(\tau)}{\lambda}$ for $\tau \in [t, \infty)$. Using this definition, we can rewrite (92d) as follows:

$$\dot{\xi}^j = \left(s^j + r^\star\right)\xi^j - \left(W^j + \frac{v_F^j}{\bar{\lambda}}\right), \tag{93}$$

Abstracting from search costs implies that the marginal rate of substitution between labor and consumption, $-\frac{v_F^j}{\lambda}$, has to be equal to the wage rate W^j. In this case, the shadow price of employment ξ^j is null. As long as agents face search costs, the real wage rate must exceed the disutility from entering the labor force $-\frac{v_F^j}{\lambda}$. Since the quantity $-\frac{v_F^j}{\lambda}$ can be viewed as being the worker's reservation wage, we will refer to $W^j + \frac{v_F^j}{\lambda}$ as the worker's surplus (by keeping in mind that $v_F^j < 0$).

Solving (93) forward and using the transversality condition $\lim_{t\to\infty} \xi^j L^j \exp\left(-\left(r^\star + s^j\right)t\right) = 0$, we get:

$$\xi^j(t) = \int_t^\infty \left[W^j(\tau) - W_R^j(\tau)\right] e^{\left(s^j + r^\star\right)(t-\tau)} \mathrm{d}\tau, \tag{94}$$

where W_R^j is the reservation wage given by

$$W_R^j \equiv -\frac{v_F^j}{\bar{\lambda}} = m^j\left(\theta^j\right)\xi^j + R^j. \tag{95}$$

Differentiating $\xi^j(t) L^j(t)$ w. r. t. time and substituting the law of motion for employment $\dot{L}^j(t)$

(11) and the dynamic optimality condition (93) yields:

$$\begin{aligned}
\frac{\mathrm{d}}{\mathrm{d}t}\left(\xi^j L^j\right) &= \dot{\xi}^j L^j + \xi^j \dot{L}^j = \left(s^j + r^\star\right)\xi^j L^j - \left(W^j + \frac{v_F^j}{\bar{\lambda}}\right) L^j + \xi^j \left(m^j U^j - s^j L^j\right), \\
&= r^\star \xi^j L^j - \left[\left(W^j + \frac{v_F^j}{\bar{\lambda}}\right) L^j - \xi^j m^j U^j\right], \\
&= r^\star \xi^j L^j - \left(W^j L^j + R^j U^j + \frac{v_F^j}{\bar{\lambda}} F^j\right),
\end{aligned}$$

where $F^j \equiv L^j + U^j$ is the labor force and we have inserted eqs. (92b)-(92c), i.e., we used the fact that $m^j \xi^j = -\frac{v_F^j}{\bar{\lambda}} - R^j$. Solving forward, making use of the transversality condition, we get:

$$\xi^j(t) L^j(t) = \int_t^\infty \left[\left(W^j L^j + R^j U^j\right) + \frac{v_F^j}{\bar{\lambda}} F^j\right] e^{-r^\star(\tau - t)} \mathrm{d}\tau. \tag{96}$$

Differentiating $\frac{v_F^j\left(U^j + L^j\right)}{\bar{\lambda}} = m^j\left(\theta^j\right)\xi^j + R^j$ w. r. t. time and inserting (93), we can derive the dynamic equation for job seekers in sector j:

$$\begin{aligned}
-\frac{v_{FF}^j}{\bar{\lambda}} \dot{U}^j &= m^j\left(\theta^j\right)\dot{\xi}^j + \alpha_V^j m^j\left(\theta^j\right)\xi^j \frac{\dot{\theta}^j}{\theta^j} + \frac{v_{FF}^j}{\bar{\lambda}} \dot{L}^j, \\
&= \left[\left(s^j + r^\star\right) + \alpha_V^j \frac{\dot{\theta}^j}{\theta^j}\right] m^j\left(\theta^j\right)\xi^j - m^j\left(\theta^j\right)\left(W^j + \frac{v_F^j}{\bar{\lambda}}\right) + \frac{v_{FF}^j}{\bar{\lambda}} \dot{L}^j.
\end{aligned}$$

where we used the fact that $\frac{\left(m^j\right)' \theta^j}{m^j} = \alpha_V^j$. Substituting $m^j \xi^j = -\frac{v_F^j}{\bar{\lambda}} - R^j$, we get:

$$\frac{v_{FF}^j}{\bar{\lambda}} \dot{U}^j = \left(\frac{v_F^j}{\bar{\lambda}} + R^j\right)\left[\left(s + r^\star\right) + \alpha_V^j \frac{\dot{\theta}^j}{\theta^j}\right] + m^j\left(\theta^j\right)\left(W^j + \frac{v_F^j}{\bar{\lambda}}\right) - \frac{v_{FF}^j}{\bar{\lambda}} \dot{L}^j. \tag{97}$$

C.2 Firms

We consider a traded sector which produces a good denoted by the superscript T that can be exported or consumed domestically. We also consider a non traded sector which produces a good denoted by the superscript N that can be consumed only domestically. Each sector consists of a large number of identical firms. Both the traded and non-traded sectors use labor, L^T and L^N, according to constant returns to scale production functions:

$$Y^T = A^T L^T, \quad \text{and} \quad Y^N = A^N L^N. \tag{98}$$

Firms post job vacancies V^j to hire workers and face a cost per job vacancy κ^j which is assumed to be constant and measured in terms of the traded good. Firms pay the wage W^j decided by the generalized Nash bargaining solution. We also consider that firms must pay a firing tax x^j per job loss which captures the extent of employment protection legislation (see e.g., Heijdra and Ligthart [2002], Veracierto [2008]).

As producers face a labor cost W^j per employee, a cost per hiring of κ^j, the profit function of the representative firm in the traded sector is:

$$\pi^T = A^T L^T - W^T L^T - \kappa^T V^T - x^T \,.\max\left\{0, -\dot{L}^T\right\}, \tag{99}$$

where x^T is a firing tax in the traded sector when $\dot{L}^T < 0$ otherwise $x^T = 0$.

Symmetrically, denoting by P the price of non traded goods in terms of traded goods, the profit function of the representative firm in the non traded sector is:

$$\pi^N = P A^N L^N - W^N L^N - \kappa^N V^N - x^N \,.\max\left\{0, -\dot{L}^N\right\}, \tag{100}$$

where x^N is a firing tax in the non traded sector when $\dot{L}^N < 0$ otherwise $x^N = 0$.

Denoting by f^j the rate at which a vacancy is matched with unemployed agents, the law of motion for labor is given by:

$$\dot{L}^j = f^j\left(\theta^j\right) - s^j L^j, \tag{101}$$

where $f^j V^j$ represents the flow of job vacancies which are fulfilled; note that f^j decreases with labor tightness θ^j.

The current-value Hamiltonian for the sector j's representative firm optimization problem is:

$$\mathcal{H}^j = \Xi^j L^j - W^j L^j - \kappa^j V^j + \left(\gamma^j + x^j\right)\left(f^j V^j - s^j L^j\right), \tag{102}$$

where Ξ^j is the marginal revenue of labor with $\Xi^T \equiv A^T$ and $\Xi^N \equiv PA^N$ and γ^j is the co-state variable associated to the labor motion equation (101).

First-order conditions can be written as follows:

$$\begin{aligned} \gamma^j + x^j &= \frac{\kappa^j}{f^j\left(\theta^j\right)}, & (103a)\\ \dot{\gamma}^j &= \gamma^j\left(r^\star + s^j\right) - \left(\Xi^j - x^j s^j - W^j\right), & (103b) \end{aligned}$$

where γ^j represents the pecuniary value of an additional job to the representative firm of sector $j = T, N$. This can be seen more formally by solving (103b) forward and using the appropriate transversality condition. This yields:

$$\gamma^j(t) = \int_t^\infty \left[\Xi^j(\tau) - W^j(\tau) - x^j s^j\right] e^{\left(s^j + r^\star\right)(t-\tau)} \mathrm{d}\tau. \tag{104}$$

Differentiating $\gamma^j(t)L^j(t)$ w. r. t. time and inserting the law of motion for employment $\dot{L}^j(t)$ together with the dynamic optimality condition (103b), we obtain:

$$\begin{aligned} \frac{\mathrm{d}}{\mathrm{d}t}\left(\gamma^j L^j\right) &= \dot{\gamma}^j L^j + \gamma^j \dot{L}^j = \gamma^j\left(r^\star + s^j\right) L^j + x^j s^j L^j - \left(\Xi^j - W^j\right) L^j + \gamma^j\left(f^j V^j - s^j L^j\right), \\ &= r^\star \gamma^j L^j - \left[\Xi^j L^j - W^j L^j - \gamma^j f^j V^j - x^j s^j L^j\right] = r^\star \gamma^j L^j - \pi^j, \end{aligned}$$

where we used the fact that $\gamma^j = \kappa^j / f^j - x^j$, $\pi^j = \Xi^j L^j - W^j L^j + x^j \dot{L}^j - \kappa^j V^j$ and $\dot{L}^j = f^j \theta^j - s^j L^j$. Using the first-order condition (103a) and solving forward, making use of the transversality condition, we get:

$$\begin{aligned} \gamma^j(t) L^j(t) &= \int_t^\infty \left[\Xi^j L^j - W^j L^j - \kappa^j V^j - x^j \,.\max\left\{0, -\dot{L}^j\right\}\right] e^{-r^\star(\tau-t)} \mathrm{d}\tau, \\ &= \int_t^\infty \pi^j e^{-r^\star(\tau-t)} \mathrm{d}\tau. & (105) \end{aligned}$$

D Derivation of the Wage Rate from Bargaining process

In this section, we derive the wage rate from a generalized Nash bargaining process. The representative firm of sector j posts job vacancies in order to hire workers. We assume that the wage rate is derived from a bargaining between the firm and the worker. Since all worker-firm pairings are identical and wages are renegotiated at each instant, the model is symmetric and the wage does not feature a pairing index k, i. e. , $W_k^j = W^j$. The wage rate W^j is set so as to maximize the following expression:

$$W^j(t) = \text{argmax } \mathcal{H}_W^j = \text{argmax } \left(\xi^j(t)\right)^{\alpha_W^j} \left(\gamma^j(t) + x^j\right)^{1-\alpha_W^j}, \quad 0 \le \alpha_W^j \le 1, \tag{106}$$

where α_W^j and $1 - \alpha_W^j$ correspond to the bargaining power of the worker and the firm, respectively. The first-order condition determining the current wage, $w(t)$ writes as follows:

$$\frac{\partial \mathcal{H}_W^j}{\partial W^j(t)} = \frac{\alpha_W^j \mathcal{H}_W^j}{\xi^j(t)} \frac{\partial \xi^j(t)}{\partial W^j(t)} + \frac{\left(1 - \alpha_W^j\right)\mathcal{H}_W^j}{\gamma^j(t) + x^j} \frac{\partial \gamma^j(t)}{\partial W^j(t)} = 0. \tag{107}$$

Differentiating (94) and (104) w.r.t. the wage rate W^j, we get: $\frac{\partial \xi^j(t)}{\partial W^j(t)} = 1$ and $\frac{\partial \gamma^j(t)}{\partial W^j(t)} = -1$; inserting these into (107):

$$\alpha_W^j\left(\gamma^j(t) + x^j\right) = \left(1 - \alpha_W^j\right)\xi^j(t). \tag{108}$$

By differentiating (108) w. r. t. time, inserting the dynamic equations for ξ^j given by (93) and for γ^j given by (103b), bearing in mind that $\gamma^j + x^j = \frac{1-\alpha_W^j}{\alpha_W^j}\xi^j$ (see eq. (107)), rearranging terms, leads to the wage rate:

$$W^j = \alpha_W^j\left(\Xi^j + r^\star x^j\right) + \left(1 - \alpha_W^j\right) W_R^j, \tag{109}$$

where $W_R^j = -v_F^j/\bar{\lambda}$ represents the reservation wage.

An alternative expression for the reservation wage W_R^j which is equal to $-v_F^j/\bar{\lambda} = m^j\left(\theta^j\right)\xi^j + R^j$ can be derived as follows. Eliminating ξ^j from (107) by making use of (123a), i.e., $\xi^j =$

$\frac{\alpha_W^j}{1-\alpha_W^j}\left(\gamma^j + x^j\right)$, inserting (103a), i.e., $\gamma^j + x^j = \kappa^j / f^j$, and using the fact that $m^j / f^j = \theta^j$, the reservation wage can be rewritten as follows:

$$
\begin{aligned}
W_R^j &= m^j\left(\theta^j\right)\xi^j + R^j, \\
&= m^j \frac{\alpha_W^j}{1-\alpha_W^j}\frac{\kappa^j}{f^j} + R^j, \\
&= \frac{\alpha_W^j}{1-\alpha_W^j}\kappa^j\theta^j + R^j. \qquad (110)
\end{aligned}
$$

E Solving the Model

E.1 Short-Run Static Solutions

In this subsection, we compute short-run static solutions for consumption and the relative price of non tradables. Static efficiency condition (92a) can be solved for consumption which of course must hold at any point of time:

$$C = C\left(\bar{\lambda}, P\right), \qquad (111)$$

with

$$
\begin{aligned}
C_{\bar{\lambda}} &= \frac{\partial C}{\partial \bar{\lambda}} = -\sigma_C \frac{C}{\bar{\lambda}} < 0, \qquad (112a) \\
C_P &= \frac{\partial C}{\partial P} = -\alpha_C \sigma_C \frac{C}{P} < 0, \qquad (112b) \\
& \qquad (112c)
\end{aligned}
$$

where σ_C corresponds to the intertemporal elasticity of substitution for consumption.

Denoting by ϕ the intratemporal elasticity of substitution between the tradable and the non tradable good and inserting short-run solution for consumption (92a) into intra-temporal allocations between non tradable and tradable goods, i.e., $C^N = P_C' C$ and $C^T = \left[P^C - P P_C'\right] C$, allows us to solve for C^T and C^N:

$$C^T = C^T\left(\bar{\lambda}, P\right), \quad C^N = C^N\left(\bar{\lambda}, P\right), \qquad (113)$$

where the partial derivatives are:

$$
\begin{aligned}
C^T_{\bar{\lambda}} &= -\sigma_C \frac{C^T}{\bar{\lambda}} < 0, \qquad (114a) \\
C^T_P &= \alpha_C \frac{C^T}{P}\left(\phi - \sigma_C\right) \lesseqgtr 0, \qquad (114b) \\
C^N_{\bar{\lambda}} &= -\sigma_C \frac{C^N}{\bar{\lambda}} < 0, \qquad (114c) \\
C^N_P &= -\frac{C^N}{P}\left[\left(1-\alpha_C\right)\phi + \alpha_C \sigma_C\right] < 0, \qquad (114d)
\end{aligned}
$$

where we use the fact that $-\frac{P_C'' P}{P_C'} = \phi\left(1-\alpha_C\right) > 0$ and $P_C' C = C^N$.

Inserting the short-run static solution for consumption in non tradables $C^N\left(\bar{\lambda}, P\right)$ given by (113) into the market clearing condition for non tradables (26) allows us to solve for the relative price of non tradables:

$$P = P\left(L^N, \bar{\lambda}, A^N\right), \qquad (115)$$

where

$$
\begin{aligned}
P_{L^N} &= \frac{\partial P}{\partial L^N} = \frac{A^N}{C^N_P} < 0, \qquad (116a) \\
P_{\bar{\lambda}} &= \frac{\partial P}{\partial \bar{\lambda}} = -\frac{C^N_{\bar{\lambda}}}{C^N_P} < 0, \qquad (116b) \\
P_{A^N} &= \frac{\partial P}{\partial A^N} = \frac{L^N}{C^N_P} < 0. \qquad (116c)
\end{aligned}
$$

Inserting (116) into (113), the short-run static solutions for C^T and C^N become:

$$C^T = C^T\left(L^N, \bar{\lambda}, A^N\right), \quad C^N = C^N\left(L^N, \bar{\lambda}, A^N\right), \qquad (117)$$

where the partial derivatives are:

$$\frac{\hat{C}^T}{\hat{\bar{\lambda}}} = -\frac{\sigma_C \phi}{[(1-\alpha_C)\phi + \alpha_C \sigma_C]} < 0, \tag{118a}$$

$$\frac{\hat{C}^T}{\hat{L^N}} = \frac{\hat{C}^T}{\hat{A^N}} = -\frac{(\phi - \sigma_C)}{[(1-\alpha_C)\phi + \alpha_C \sigma_C]} \frac{\omega_N}{\omega_C} \lesseqgtr 0, \tag{118b}$$

$$\frac{\hat{C}^N}{\hat{\bar{\lambda}}} = -\sigma_C + \sigma_C = 0, \tag{118c}$$

$$\frac{\hat{C}^N}{\hat{L^N}} = \frac{\hat{C}^N}{\hat{A^N}} = \frac{\omega_N}{\omega_C} > 0. \tag{118d}$$

We denote by a hat the rate of change of the variable and rewrite $\frac{C^N}{A^N L^N} = \frac{PC^N}{P_C C} \frac{P_C C}{Y} \frac{Y}{PA^N L^N} = \frac{\alpha_C \omega_C}{\omega_N}$ with α_C the non tradable content of consumption expenditure, ω_C the GDP share of consumption expenditure and ω_N the non tradable content of GDP.

E.2 Derivation of the Dynamic Equation of the Current Account

Using the fact that $A \equiv B + \gamma^T L^T + \gamma^N L^N$, differentiating with respect to time, noticing that $(\dot{\gamma^j L^j}) = r^\star \gamma^j L^j - \pi^j$, the accumulation equation of traded bonds is given by:

$$\begin{aligned} \dot{B} &= \dot{A} - \dot{\gamma}^T L^T - \gamma^T \dot{L}^T - \dot{\gamma}^N L^N - \gamma^N \dot{L}^N, \\ &= r^\star \left(A - \gamma^T L^T - \gamma^N L^N\right) + \pi^T + \pi^N + W^T L^T + W^N L^N + R^T U^T + R^N U^N - T - P_C C. \end{aligned}$$

Remembering that $\pi^j = \Xi^j - W^j L^j - \kappa^j V^j - x^j \, . \max \left\{0, -\dot{L}^j\right\}$, inserting the market clearing condition for the non traded good (26) and the balanced government budget (25), the current account equation reduces to:

$$\dot{B}(t) = r^\star B(t) + A^T L^T(t) - C^T(t) - G^T - \kappa^T V^T(t) - \kappa^N V^N(t). \tag{119}$$

E.3 Equilibrium Dynamics and Formal Solutions

E.3.1 Dynamic System

Differentiating (103a) w. r. t. time, using (103b) yields

$$\frac{\dot{\theta}^j}{\theta^j} = \frac{1}{1-\alpha_V^j} \frac{\dot{\gamma}^j}{\gamma^j + x^j}.$$

Eliminating $\gamma^j + x^j$ by using (103a), leads to the dynamic equation for labor market tightness θ^j:

$$\dot{\theta}^j(t) = \frac{\theta^j(t)}{\left(1-\alpha_V^j\right)} \left\{ \left(s^j + r^\star\right) - \frac{f^j\left(\theta^j(t)\right)}{\kappa^j} \left[\left(\Xi^j + r^\star x^j\right) - W^j\right] \right\}.$$

Setting the overall surplus from an additional job in sector j:

$$\Psi^j(t) = \left(\Xi^j(t) + r^\star x^j\right) + \frac{v_F^j(t)}{\bar{\lambda}}. \tag{120}$$

Inserting the Nash bargaining wage W^j given by (109) into $\left[\left(\Xi^j + r^\star x^j\right) - W^j\right]$, the dynamic equation for labor market tightness θ^j can be rewritten as follows:

$$\dot{\theta}^j(t) = \frac{\theta^j(t)}{\left(1-\alpha_V^j\right)} \left\{ \left(s^j + r^\star\right) - \frac{f^j\left(\theta^j(t)\right)\left(1-\alpha_W^j\right)\Psi^j(t)}{\kappa^j} \right\}. \tag{121}$$

The overall surplus from an additional job in the traded and the non traded sector is given by:

$$\Psi^T = \left(A^T + r^\star x^T\right) + \frac{v_F^T}{\bar{\lambda}}, \quad \Psi^N = \left[P\left(L^N, \bar{\lambda}, A^N\right) A^N + r^\star x^N\right] + \frac{v_F^N}{\bar{\lambda}}, \tag{122}$$

where the short-run static solution for the relative price of non tradables (115) has been inserted into the overall surplus from a match into the non traded sector. Partial derivatives are given by:

$$\Psi^T_{L^T} = \Psi^T_{U^T} = \frac{v^T_{FF}}{\bar{\lambda}} < 0, \tag{123a}$$

$$\Psi^N_{L^N} = P_{L^N} A^N + \frac{v^N_{FF}}{\bar{\lambda}} < 0, \tag{123b}$$

$$\Psi^N_{U^N} = \frac{v^N_{FF}}{\bar{\lambda}} < 0, \tag{123c}$$

$$\begin{aligned}\Psi^N_{A^N} &= P_{A^N} A^N + P = \frac{A^N L^N}{C^N_P} + P, \\ &= \frac{A^N L^N}{C^N_P}\left\{1 - \left[\left(1-\alpha_C\right)\phi + \alpha_C \sigma_C\right]\frac{\alpha_C \omega_C}{\omega_N}\right\} < 0,\end{aligned} \tag{123d}$$

$$\begin{aligned}\Psi^N_{\bar{\lambda}} &= P_{\bar{\lambda}} A^N - \frac{v^N_F}{\left(\bar{\lambda}\right)^2}, \\ &= -\frac{1}{\bar{\lambda}}\left\{\frac{\sigma_C P A^N}{\left[\left(1-\alpha_C\right)\phi + \alpha_C \sigma_C\right]} + \frac{v^N_F}{\bar{\lambda}}\right\} < 0,\end{aligned} \tag{123e}$$

where $P_{L^N} < 0$, $C^N_P < 0$, and we use the fact that $\frac{C^N}{A^N L^N} = \frac{PC^N}{P_C C}\frac{P_C C}{Y}\frac{Y}{PA^N L^N} = \frac{\alpha_C \omega_C}{\omega_N}$.

The adjustment of the open economy towards the steady-state is described by a dynamic system which comprises six equations. Because workers must search for a job to switch from one sector to another, i.e., cannot move from one sector to another instantaneously, the dynamic system is block recursive. The first (second) dynamic system consists of the law of motion of employment in the traded (non traded) sector described by (11), the dynamic equations for labor tightness and job seekers given by (30) and (32), respectively. We denote the steady-state value with a tilde.

Traded Sector

Linearizing the accumulation equation for traded labor (11) by setting $j = T$ and the dynamic equations for labor market tightness (121) and job seekers (97) in the traded sector, we get in matrix form:

$$\left(\dot{L}^T, \dot{\theta}^T, \dot{U}^T\right)^T = J^T\left(L^T(t) - \tilde{L}^T, \theta^T(t) - \tilde{\theta}^T, U^T(t) - \tilde{U}^T\right)^T \tag{124}$$

where J^T is given by

$$J^T \equiv \begin{pmatrix} -s^T & \left(m^T\right)' \tilde{U}^T & m^T\left(\tilde{\theta}^T\right) \\ -\frac{1-\alpha^T_W}{1-\alpha^T_V}\frac{\tilde{m}^T}{\kappa^T}\frac{v^T_{FF}}{\bar{\lambda}} & \left(s^T + r^\star\right) & -\frac{1-\alpha^T_W}{1-\alpha^T_V}\frac{\tilde{m}^T}{\kappa^T}\frac{v^T_{FF}}{\bar{\lambda}} \\ \left(2s^T + r^\star\right) + \frac{\alpha^T_W \tilde{m}^T}{1-\alpha^T_V} & -\left(m^T\right)' \tilde{U}^T & \left(s^T + r^\star\right) - \tilde{m}^T + \frac{\alpha^T_W}{1-\alpha^T_V}\tilde{m}^T \end{pmatrix}, \tag{125}$$

and where we used the fact that:

$$\begin{aligned}&\frac{\tilde{f}^T\left(1-\alpha^T_W\right)\tilde{\Psi}^T}{s^T + r^\star} = \kappa^T, \\ &\frac{v^T_F}{\bar{\lambda}} + R^T = -\tilde{m}^T \tilde{\xi}^T = -\frac{\tilde{m}^T \alpha^T_W \tilde{\Psi}^T}{s^T + r^\star}, \\ &1 + \frac{\alpha^T_V}{1-\alpha^T_V}\frac{\tilde{f}^T\left(1-\alpha^T_W\right)\tilde{\Psi}^T}{\kappa^T\left(s^T + r^\star\right)} = \frac{1}{1-\alpha^T_V}.\end{aligned}$$

The trace denoted by Tr of the linearized 3×3 matrix (125) is given by:

$$\mathrm{Tr}J^T = \left(s^T + r^\star\right) + r^\star + \frac{\tilde{m}^T}{1-\alpha^T_V}\left[\alpha^T_W - \left(1-\alpha^T_V\right)\right]. \tag{126}$$

The determinant denoted by Det of the linearized 3×3 matrix (125) is unambiguously negative:

$$\mathrm{Det}J^T = -\left(s^T + r^\star\right)\left(s^T + \tilde{m}^T\right)\left[\left(s^T + r^\star\right) + \frac{\alpha^T_W}{1-\alpha^T_V}\tilde{m}^T\right] < 0. \tag{127}$$

Assuming that the Hosios condition holds, i.e., setting $\alpha^T_W = 1 - \alpha^T_V$, the trace reduces to:

$$\mathrm{Tr}J^T = \left(s^T + r^\star\right) + r^\star., \tag{128}$$

while the determinant is given by:

$$\mathrm{Det}J^T = -\left(s^T + r^\star\right)\left(s^T + r^\star + \tilde{m}^T\right)\left(s^T + \tilde{m}^T\right) < 0. \tag{129}$$

From now on, for clarity purpose, we impose the Hosios condition in order to avoid unnecessary complications. We relax this assumption when analyzing steady-state effects and conducting a quantitative exploration of the effects of higher productivity of tradables relative to non tradables. Note that all conclusions related to the analysis of equilibrium dynamics hold whether the Hosios conditions is imposed or not.

Denoting by ν^T the eigenvalue in the traded sector, the characteristic equation for the matrix J (125) of the linearized system writes as follows:

$$\left(s^T + r^\star - \nu_i^T\right) \left\{ \left(\nu_i^T\right)^2 - r^\star \nu_i^T + \frac{\mathrm{Det}J^T}{s^T + r^\star} \right\} = 0. \tag{130}$$

The characteristic roots obtained from the characteristic polynomial of degree two can be written as follows:

$$\nu_i^T \equiv \frac{1}{2} \left\{ r^\star \pm \sqrt{\left(r^\star\right)^2 - 4 \frac{\mathrm{Det}J^T}{s^T + r^\star}} \right\} \gtrless 0, \quad i = 1, 2. \tag{131}$$

We denote by $\nu_1^T < 0$ and $\nu_2^T > 0$ the stable and unstable eigenvalues respectively which satisfy:

$$\nu_1^T < 0 < r^\star < \nu_2^T. \tag{132}$$

Let ν_3^T be the second unstable characteristic root which writes as:

$$\nu_3^T = s^T + r^\star > 0. \tag{133}$$

Since the system features one state variable, L^T, and one negative eigenvalue, two jump variables, θ^T and U^T, and two positive eigenvalues, the equilibrium yields a unique one-dimensional saddle-path. Inserting (126) and (127) into (131), the stable and unstable eigenvalues reduce to:

$$\nu_1^T = -\left(s^T + \tilde{m}^T\right), \quad \nu_2^T = \left(s^T + r^\star + \tilde{m}^T\right). \tag{134}$$

Non Traded Sector

Linearizing the accumulation equation for non traded labor (11) by setting $j = N$ and the dynamic equations for labor market tightness (121) and job seekers (97) in the non traded sector, we get in matrix form:

$$\left(\dot{L}^N, \dot{\theta}^N, \dot{U}^N\right)^T = J^N \left(L^N(t) - \tilde{L}^N, \theta^N(t) - \tilde{\theta}^N, U^N(t) - \tilde{U}^N\right)^T, \tag{135}$$

where J^N is given by

$$J^N \equiv \begin{pmatrix} -s^N & \left(m^N\right)' \tilde{U}^N & m^N\left(\tilde{\theta}^N\right) \\ -\frac{1-\alpha_W^N}{1-\alpha_V^N} \frac{\tilde{m}^N}{\kappa^N} \left(P_{L^N} A^N + \frac{v_{FF}^N}{\bar{\lambda}}\right) & \left(s^N + r^\star\right) & -\frac{1-\alpha_W^N}{1-\alpha_V^N} \frac{\tilde{m}^N}{\kappa^N} \frac{v_{FF}^N}{\bar{\lambda}} \\ \left(2s^N + r^\star\right) + \frac{\alpha_W^N \tilde{m}^N}{1-\alpha_V^N} \left(P_{L^N} A^N \frac{\bar{\lambda}}{v_{FF}^N} + 1\right) & -\left(m^N\right)' \tilde{U}^N & \left(s^N + r^\star\right) - \tilde{m}^N + \frac{\alpha_W^N}{1-\alpha_V^N} \tilde{m}^N \end{pmatrix}, \tag{136}$$

and where we used the fact that:

$$\begin{aligned} \frac{\tilde{f}^N \left(1 - \alpha_W^N\right) \tilde{\Psi}^N}{s^N + r^\star} &= \kappa^N, \\ \frac{v_F^N}{\bar{\lambda}} + R^N = -\tilde{m}^N \tilde{\xi}^N &= -\frac{\tilde{m}^N \alpha_W^N \tilde{\Psi}^N}{s^N + r^\star}, \\ 1 + \frac{\alpha_V^N}{1 - \alpha_V^N} \frac{\tilde{f}^N \left(1 - \alpha_W^N\right) \tilde{\Psi}^N}{\kappa^N \left(s^N + r^\star\right)} &= \frac{1}{1 - \alpha_V^N}. \end{aligned}$$

The trace denoted by Tr of the linearized 3×3 matrix (136) is given by:

$$\mathrm{Tr}J^N = \left(s^N + r^\star\right) + r^\star + \frac{\tilde{m}^N}{1 - \alpha_V^N} \left[\alpha_W^N - \left(1 - \alpha_V\right)\right]. \tag{137}$$

The determinant denoted by Det of the linearized 3×3 matrix (136) is unambiguously negative:

$$\begin{aligned} \mathrm{Det}J^N &= -\left(s^N + r^\star\right) \left\{ \left(s^N + \tilde{m}^N\right) \left[\left(s^N + r^\star\right) + \frac{\alpha_W^N}{1 - \alpha_V^N} \tilde{m}^N\right] \right. & (138) \\ &+ \left. \frac{1 - \alpha_W^N}{1 - \alpha_V^N} \frac{\tilde{m}^N}{\kappa^N} P_{L^N} A^N \frac{\tilde{m}^N}{\theta^N} \left(\frac{\alpha_W^N}{1 - \alpha_W^N} \kappa^N \tilde{\theta}^N \frac{\bar{\lambda}}{v_{FF}^N} - \alpha_V \tilde{U}^N\right) \right\} < 0, & (139) \end{aligned}$$

where $P_{L^N} < 0$.

Assuming that the Hosios condition holds, i.e., setting $\alpha_W^N = 1 - \alpha_V^N$, the trace reduces to:

$$\text{Tr}J^N = \left(s^N + r^\star\right) + r^\star, \tag{140}$$

while the determinant is given by:

$$\text{Det}J^N = -\left(s^N + r^\star\right)^2\left(s^N + \tilde{m}^N\right)\left\{\frac{\left(s^N + r^\star + \tilde{m}^N\right)}{\left(s^N + r^\star\right)} - \frac{P_{L^N}\tilde{L}^N}{\tilde{P}}\frac{\tilde{P}A^N}{\left(1-\alpha_V^N\right)\tilde{\Psi}^N}\left(\tilde{\chi}^N\sigma_L^N + \alpha_V\tilde{u}^N\right)\right\} < 0., \tag{141}$$

where we have rewritten the last term as follow:

$$\begin{aligned}
&\frac{1-\alpha_W^N}{1-\alpha_V^N}\frac{\tilde{m}^N}{\kappa^N}P_{L^N}A^N\frac{\tilde{m}^N}{\theta^N}\left(\frac{\alpha_W^N}{1-\alpha_W^N}\kappa^N\tilde{\theta}^N\frac{\bar{\lambda}}{v_{FF}^N} - \alpha_V\tilde{U}^N\right)\\
= \quad & -\frac{1-\alpha_W^N}{1-\alpha_V^N}\frac{\tilde{m}^N}{\kappa^N}P_{L^N}A^N\tilde{f}^N\tilde{F}^N\left(\tilde{\chi}^N\sigma_L^N + \alpha_V\tilde{u}^N\right),\\
= \quad & -\frac{s^N}{\tilde{u}^N\left(1-\alpha_V^N\right)}P_{L^N}\tilde{L}^NA^N\frac{\left(s^N + r^\star\right)}{\tilde{\Psi}^N}\left(\tilde{\chi}^N\sigma_L^N + \alpha_V\tilde{u}^N\right),\\
= \quad & -\left(s^N + r^\star\right)\left(s^N + \tilde{m}^N\right)\frac{P_{L^N}\tilde{L}^N}{\tilde{P}}\frac{\tilde{P}A^N}{\left(1-\alpha_V^N\right)\tilde{\Psi}^N} < 0,
\end{aligned}$$

and where we used the fact that $\frac{\alpha_W^N}{1-\alpha_W^N}\kappa^N\tilde{\theta}^N = -\tilde{\chi}^N\frac{v_F^N}{\bar{\lambda}}$, $\tilde{f}^N = \tilde{m}^N/\tilde{\theta}^N$, and $\frac{v_F^N}{v_{FF}^N\tilde{F}^N} = \sigma_L^N$ to get the second line, $\frac{\tilde{f}^N\left(1-\alpha_W^N\right)}{\kappa^N} = \frac{\left(s^N+r^\star\right)}{\tilde{\Psi}^N}$, $\tilde{m}^N\tilde{U}^N = s^N\tilde{L}^N$, and $\tilde{U}^N/\tilde{F}^N = \tilde{u}^N$ to get the third line, $\tilde{u}^N = \frac{s^N}{s^N+\tilde{m}^N}$, multiplying the numerator and the denominator by $\tilde{P}$ and rearranging terms to get the last line.

From now on, for clarity purpose, we impose the Hosios condition in order to avoid unnecessary complications. We relax this assumption when analyzing steady-state effects and conducting a quantitative exploration of the effects of higher productivity of tradables relative to non tradables.

Denoting by ν^N the eigenvalue, the characteristic equation for the matrix J (136) of the linearized system writes as follows:

$$\left(s^N + r^\star - \nu_i^N\right)\left\{\left(\nu_i^N\right)^2 - r^\star\nu_i^N + \frac{\text{Det}J^N}{s^N + r^\star}\right\} = 0. \tag{142}$$

The characteristic roots obtained from the characteristic polynomial of degree two write as follows:

$$\nu_i^N \equiv \frac{1}{2}\left\{r^\star \pm \sqrt{\left(r^\star\right)^2 - 4\frac{\text{Det}J^N}{s^N + r^\star}}\right\} \gtrless 0, \quad i = 1, 2. \tag{143}$$

We denote by $\nu_1^N < 0$ and $\nu_2^N > 0$ the stable and unstable eigenvalues respectively which satisfy:

$$\nu_1^N < 0 < r^\star < \nu_2^N. \tag{144}$$

As it will become useful later, $\nu_1^N\left(r^\star - \nu_1^N\right) = \frac{\text{Det}J^N}{s^N + r^\star}$ which can be rewritten as follows

$$\begin{aligned}
\frac{\text{Det}J^N}{s^N + r^\star} \quad = \quad & -\left(s^N + r^\star\right)\left(s^N + \tilde{m}^N\right)\left\{\frac{\left(s^N + r^\star + \tilde{m}^N\right)}{\left(s^N + r^\star\right)} + \frac{\omega_N}{\alpha_C\omega_C\left[\left(1-\alpha_C\right)\phi + \alpha_C\sigma_C\right]}\right.\\
\times \quad & \left.\frac{\tilde{P}A^N}{\left(1-\alpha_V^N\right)\tilde{\Psi}^N}\left(\tilde{\chi}^N\sigma_L^N + \alpha_V^N\tilde{u}^N\right)\right\} < 0.
\end{aligned} \tag{145}$$

where we used the fact that $\frac{C^N}{A^NL^N} = \frac{\alpha_C\omega_C}{\omega_N}$ and $P_{L^N} = \frac{A^N}{C_P^N} < 0$.

Let ν_3^N be the second unstable characteristic root which writes as:

$$\nu_3^N = s^N + r^\star > 0. \tag{146}$$

Since the system features one state variable, L^N, and one negative eigenvalue, two jump variables, θ^N and U^N, and two positive eigenvalues, the equilibrium yields a unique one-dimensional saddle-path.

E.4 Formal Solutions for $\theta^T(t)$ and $U^T(t)$

Setting the constant $D_2^T = 0$ to insure a converging adjustment for all macroeconomic aggregates, the stable paths are given by :

$$\begin{aligned} L^T(t) - \tilde{L}^T &= D_1^T e^{\nu_1^T t} && \text{(147a)} \\ \theta^T(t) - \tilde{\theta}^T &= \omega_{21}^T D_1^T e^{\nu_1^T t}, && \text{(147b)} \\ U^T(t) - \tilde{U}^T &= \omega_{31}^T D_1^T e^{\nu_1^T t}, && \text{(147c)} \end{aligned}$$

where $D_1^T = L_0^T - \tilde{L}^T$, and elements ω_{21}^T and ω_{31}^T of the eigenvector (associated with the stable eigenvalue ν_1^T) are given by:

$$\omega_{21}^T = \frac{\frac{1-\alpha_W^T}{1-\alpha_V^T} \frac{\tilde{m}^T}{\kappa^T} \frac{v_{FF}^T}{\lambda} \left(\tilde{m}^T + s^T + \nu_1^T \right)}{\tilde{m}^T \left(s^T + r^\star - \nu_1^T \right) + \frac{1-\alpha_W^T}{1-\alpha_V^T} \frac{\tilde{m}^T}{\kappa^T} \frac{v_{FF}^T}{\lambda} \left(m^T \right)' \tilde{U}^T} \lesseqgtr 0, \quad \text{(148a)}$$

$$\omega_{31}^T = \left(\frac{s^T + \nu_1^T}{\tilde{m}^T} \right) - \frac{\left(m^T \right)' \tilde{U}^T}{\tilde{m}^T} \omega_{21}^T \lesseqgtr 0. \quad \text{(148b)}$$

We have normalized ω_{11}^T to unity. Inserting $\nu_1^T = s^T + \tilde{m}^T$ (see (134)) into (148a) and (148b), eigenvectors reduce to:

$$\omega_{21}^T = 0, \quad \omega_{31}^T = -1. \quad \text{(149)}$$

From (149), the dynamics for labor market tightness θ^T degenerate while job seekers are negatively correlated with employment along a stable transitional path.

E.5 Formal Solutions for $\theta^N(t)$ and $U^N(t)$

Setting the constant $D_2^N = 0$ to insure a converging adjustment for all macroeconomic aggregates, the stable paths are given by:

$$\begin{aligned} L^N(t) - \tilde{L}^N &= D_1^N e^{\nu_1^N t} && \text{(150a)} \\ \theta^N(t) - \tilde{\theta}^N &= \omega_{21}^N D_1^N e^{\nu_1^N t}, && \text{(150b)} \\ U^N(t) - \tilde{U}^N &= \omega_{31}^N D_1^N e^{\nu_1^N t}, && \text{(150c)} \end{aligned}$$

where $D_1^N = L_0^N - \tilde{L}^N$, and elements ω_{21}^N and ω_{31}^N of the eigenvector (associated with the stable eigenvalue ν_1^N) are given by:

$$\omega_{21}^N = \frac{\frac{1-\alpha_W^N}{1-\alpha_V^N} \frac{\tilde{m}^N}{\kappa^N} \left[\tilde{m}^N \left(P_{L^N} A^N + \frac{v_{FF}^N}{\lambda} \right) + \left(s^N + \nu_1^N \right) \frac{v_{FF}^N}{\lambda} \right]}{\tilde{m}^N \left(s^N + r^\star - \nu_1^N \right) + \frac{1-\alpha_W^N}{1-\alpha_V^N} \frac{\tilde{m}^N}{\kappa^N} \frac{v_{FF}^N}{\lambda} \left(m^N \right)' \tilde{U}^N} \lesseqgtr 0, \quad \text{(151a)}$$

$$\omega_{31}^N = \left(\frac{s^N + \nu_1^N}{\tilde{m}^N} \right) - \frac{\left(m^N \right)' \tilde{U}^N}{\tilde{m}^N} \omega_{21}^N \lesseqgtr 0. \quad \text{(151b)}$$

We have normalized ω_{11}^N to unity.

E.6 Formal Solution for the Stock of Foreign Bonds $B(t)$

Substituting first the short-run static solutions for consumption in tradables given by (117), and using the fact that $V^j = U^j \theta^j$, the accumulation equation for traded bonds (119)can be written as follows:

$$\dot{B}(t) = r^\star B(t) + A^T L^T(t) - C^T \left(L^N(t), \bar{\lambda}, A^N \right) - G^T - \kappa^T \theta^T(t) U^T(t) - \kappa^N \theta^N(t) U^N(t). \quad \text{(152)}$$

Linearizing (152) in the neighborhood of the steady-state and inserting stable solutions given by (147) and (150) yields:

$$\dot{B}(t) = r^\star \left(B(t) - \tilde{B} \right) + \Lambda^T \left(L^T(t) - \tilde{L}^T \right) + \Lambda^N \left(L^N(t) - \tilde{L}^N \right), \quad \text{(153)}$$

where we set:

$$\begin{aligned} \Lambda^T &= A^T - \kappa^T \tilde{U}^T \omega_{21}^T - \kappa^T \tilde{\theta}^T \omega_{31}^T = A^T + \kappa^T \tilde{\theta}^T > 0, && \text{(154a)} \\ \Lambda^N &= -C_{L^N}^T - \kappa^N \tilde{U}^N \omega_{21}^N - \kappa^N \tilde{\theta}^N \omega_{31}^N, \\ &= -C_{L^N}^T - \kappa^N \tilde{U}^N \left(1 - \alpha_V^N \right) \omega_{21}^N - \frac{\kappa^N \tilde{\theta}^N \left(s^N + \nu_1^N \right)}{\tilde{m}^N} > 0, && \text{(154b)} \end{aligned}$$

where we have inserted (151b) and used the fact that $\left(m^N\right)' \theta^N / m^N = \alpha_V^N$ to get (154b); note that $C^T_{L^N} \simeq 0$ because our estimates of ϕ average about 1 while we set σ_C to one. The sign of (154b) follows from the fact that $\omega_{21}^N < 0$ (see (193)) and $s^N + \nu_1^N < 0$; the latter result stems from the fact that $\nu_1^T = -(s^T + \tilde{m}^T)$; because we have the following set of inequalities $\frac{\text{Det}J^N}{s^N + r^N} < \frac{\text{Det}J^T}{s^T + r^\star} < 0$, $\nu_1^N < -(s^N + \tilde{m}^N) < 0$ and thereby $s^N + \nu_1^N < 0$.

Solving the differential equation (153) yields:

$$B(t) = \tilde{B} + \left[\left(B_0 - \tilde{B}\right) - \frac{\Lambda^T D_1^T}{\nu_1^T - r^\star} - \frac{\Lambda^N D_1^N}{\nu_1^N - r^\star}\right] e^{r^\star t} + \frac{\Lambda^T D_1^T}{\nu_1^T - r^\star} e^{\nu_1^T t} + \frac{\Lambda^N D_1^N}{\nu_1^N - r^\star} e^{\nu_1^N t}. \tag{155}$$

Invoking the transversality condition for intertemporal solvency, and using the fact that $D_1^T = L_0^T - \tilde{L}^T$ and $D_1^N = L_0^N - \tilde{L}^N$, we obtain the linearized version of the nation's intertemporal budget constraint:

$$\tilde{B} - B_0 = \Phi^T \left(\tilde{L}^T - L_0^T\right) + \Phi^T \left(\tilde{L}^N - L_0^N\right), \tag{156}$$

where we set

$$\Phi^T \equiv \frac{\Lambda^T}{\nu_1^T - r^\star} = -\frac{\left(A^T + \kappa^T \tilde{\theta}^T\right)}{\left(s^T + \tilde{m}^T + r^\star\right)} < 0, \quad \Phi^N \equiv \frac{\Lambda^N}{\nu_1^N - r^\star} < 0. \tag{157}$$

Equation (157) can be solved for the stock of foreign bonds:

$$\tilde{B} = B\left(\tilde{L}^T, \tilde{L}^N\right), \quad B_{L^T} = \Phi^T < 0, \quad B_{L^N} = \Phi^N < 0. \tag{158}$$

For the national intertemporal solvency to hold, the terms in brackets of equation (155) must be zero so that the stable solution for net foreign assets finally reduces to:

$$B(t) - \tilde{B} = \Phi^T \left(L^T(t) - \tilde{L}^T\right) + \Phi^N \left(L^N(t) - \tilde{L}^N\right). \tag{159}$$

F Revisiting the Theory Developed by Balassa [1964] and Samuelson [1964]: Derivation of Equations in Section 2.1

This Appendix presents the formal analysis underlying the results described in section 2.1. For simplicity purposes, we abstract from firing costs. Additionally, we assume that the worker bargaining power α_W^j is symmetric across sectors.

As defined by eq. (120) that we repeat for convenience, the overall surplus from hiring in sector j, Ψ^j, is defined as the difference between the marginal product of labor (Ξ^j) and the reservation wage (W_R^j):

$$\Psi^j = \Xi^j - W_R^j. \tag{160}$$

Eq. (160) corresponds to eq. (2) in the text. The reservation wage, W_R^j, is equal to the expected value of a job, i.e., $m^j \xi^j$ with m^j the probability of finding a job, plus the unemployment benefit R^j:

$$W_R^j = \frac{\alpha_W}{1 - \alpha_W} \kappa^j \theta^j + R^j, \tag{161}$$

where we used the fact that $m^j \xi^j = \frac{\alpha_W}{1-\alpha_W} \kappa^j \theta^j$. Totally differentiating eq. (161), the change of the reservation wage in percentage is proportional to the labor market tightness:

$$\hat{W_R}^j = \chi^j \hat{\theta}^j, \tag{162}$$

where $\chi^j \equiv \frac{m^j \xi^j}{W_R^j}$ corresponds to the share of the surplus associated with a labor contract.

The product wage W^j paid to the worker in sector j is equal to the reservation wage W_R^j plus a share α_W of the overall surplus Ψ^j:

$$W^j = \alpha_W \Psi^j + W_R^j. \tag{163}$$

Eq. (163) corresponds to eq. (3) in the text. Totally differentiating (163), the change in the product wage in percentage is proportional to the changes in the labor market tightness and the overall surplus from an additional job:

$$\begin{aligned} \hat{w}^j &= \frac{\alpha_W \Psi^j}{W^j} \hat{\Psi}^j + \frac{W_R^j}{W^j} \hat{W}_R^j, \\ &= \frac{\alpha_W \Psi^j}{W^j} \hat{\Psi}^j + \frac{W_R^j \chi^j}{W^j} \hat{\theta}^j, \end{aligned} \tag{164}$$

where we substituted (162) to get the last line. Subtracting $\hat{w}^T$ from $\hat{w}^N$ yields the wage differential between the non traded and the traded sector:

$$\begin{aligned}\hat{w}^N - \hat{w}^T &= \frac{\alpha_W \Psi^N}{W^N}\hat{\Psi}^N + \frac{W_R^N}{W^N}\hat{W}_R^N - \frac{\alpha_W \Psi^T}{W^T}\hat{\Psi}^T + \frac{W_R^T}{W^T}\hat{W}_R^T, \\ &= -\frac{\chi W_R}{W}\left(\hat{\theta}^T - \hat{\theta}^N\right) - \frac{\alpha_W \Psi}{W}\left(\hat{\Psi}^T - \hat{\Psi}^N\right), \qquad (165)\end{aligned}$$

where we assume that initially, sectoral wages, W^j, the share of the surplus associated with a labor contract, χ^j, reservation wages, W_R^j, and overall surpluses, Ψ^j, are similar across sectors, i.e., $W^j \simeq W$, $\chi^j W_R^j \simeq \chi W_R$ and $\Psi^j \simeq \Psi$. **Eq. (160) corresponds to eq. (4) in the text**.

When a labor contract is concluded, a surplus Ψ^j is created. The firm obtains a share $1-\alpha_W$ of the surplus which is equal to the difference between the marginal product of labor and the Nash bargaining wage W^j:

$$(1-\alpha_W)\,\Psi^j = \Xi^j - W^j.$$

The equation above can be rewritten as follows:

$$\Xi^j = (1-\alpha_W)\,\Psi^j + W^j. \qquad (166)$$

Eq. (166) corresponds to eq. (5) in the text. According to the definition of the representative firm's profit (16), i.e., $\pi^j = \Xi^j L^j - W^j L^j - \kappa^j V^j$ (we set $x^j = 0$ since we abstract from the firing cost in this section for simplicity purposes), the share of the surplus obtained by the firm is equal to the dividend plus the hiring cost per worker:

$$(1-\alpha_W)\,\Psi^j = \frac{\pi^j + \kappa^j V^j}{L^j}. \qquad (167)$$

Totally differentiating (166) yields the change of the marginal revenue of labor in percentage:

$$\hat{\Xi}^j = \frac{(1-\alpha_W)\,\Psi^j}{\Xi^j}\hat{\Psi}^j + \frac{W^j}{\Xi^j}\hat{W}^j. \qquad (168)$$

Subtracting $\hat{\Xi}^T$ from $\hat{\Xi}^N$ while assuming that initially $W^j \simeq W$, $\Xi^j \simeq \Xi$, $\Psi^j \simeq \Psi$, leads to:

$$\hat{\Xi}^N - \hat{\Xi}^T = -\frac{(1-\alpha_W)\,\Psi}{\Xi}\left(\hat{\Psi}^T - \hat{\Psi}^N\right) + \frac{W}{\Xi}\left(\hat{W}^N - \hat{W}^T\right). \qquad (169)$$

Using the fact that $\hat{\Xi}^N = \hat{P} + \hat{A}^N$ and $\hat{\Xi}^T = \hat{A}^T$, one obtains a relationship between the relative price growth and both the productivity and the wage differential:

$$\hat{P} = \hat{A}^T - \hat{A}^N - \frac{(1-\alpha_W)\,\Psi}{\Xi}\left(\hat{\Psi}^T - \hat{\Psi}^N\right) + \frac{W}{\Xi}\left(\hat{W}^N - \hat{W}^T\right). \qquad (170)$$

Eq. (170) corresponds to eq. (6) in the text.

G Graphical Apparatus

Before turning to the derivation of steady-state effects, we investigate graphically the long-run effects of a productivity differential.

G.1 Steady-State

Using (110), the steady-state of the open economy is described by the following set of equations:

$$\tilde{C} = \left[P_C\left(\tilde{P}\right)\bar{\lambda}\right]^{-\sigma_C}, \tag{171a}$$

$$s^T\tilde{L}^T = m^T\left(\tilde{\theta}^T\right)\tilde{U}^T, \tag{171b}$$

$$s^N\tilde{L}^N = m^N\left(\tilde{\theta}^N\right)\tilde{U}^N, \tag{171c}$$

$$\left(\tilde{L}^T + \tilde{U}^T\right) = \left[\bar{\lambda}\left(\frac{\alpha_W^T}{1-\alpha_W^T}\kappa^T\tilde{\theta}^T + R^T\right)\right]^{\sigma_L^T}, \tag{171d}$$

$$\left(\tilde{L}^N + \tilde{U}^N\right) = \left[\bar{\lambda}\left(\frac{\alpha_W^N}{1-\alpha_W^N}\kappa^N\tilde{\theta}^N + R^N\right)\right]^{\sigma_L^N}, \tag{171e}$$

$$\frac{\kappa^T}{f^T\left(\tilde{\theta}^T\right)} = \frac{\left(1-\alpha_W^T\right)\tilde{\Psi}^T}{s^T + r^\star}, \tag{171f}$$

$$\frac{\kappa^N}{f^N\left(\tilde{\theta}^N\right)} = \frac{\left(1-\alpha_W^N\right)\tilde{\Psi}^N}{s^N + r^\star}, \tag{171g}$$

$$A^N\tilde{L}^N = \tilde{C}^N, \tag{171h}$$

$$r^\star\tilde{B} + A^T\tilde{L}^T - \tilde{C}^T - \kappa^T\tilde{\theta}^T\tilde{U}^T - \kappa^N\tilde{\theta}^N\tilde{U}^N, \tag{171i}$$

and the intertemporal solvency condition

$$\tilde{B} - B_0 = \Phi^T\left(\tilde{L}^T - L_0^T\right) + \Phi^T\left(\tilde{L}^N - L_0^N\right), \tag{171j}$$

where $C^N = P_C'C$ and $C^T = (1-\alpha_C)P_C C$ and we used the fact that $V^j = U^j\theta^j$. The steady-state equilibrium defined by ten equations jointly determines $\tilde{C}$, $\tilde{L}^T$, $\tilde{L}^N$ $\tilde{U}^T$, $\tilde{U}^N$, $\tilde{\theta}^T$, $\tilde{\theta}^N$, $\tilde{P}$, $\tilde{B}$, $\bar{\lambda}$.

G.2 Isoclines and Stable Path in the (θ^T, L^T)-space

The labor market in the traded sector can be summarized graphically by Figure 6(a) that traces out two schedules in the (θ^T, L^T)-space. More precisely, eliminating $\tilde{U}^T$ from eq. (171d) by using (171b), i.e., $\tilde{U}^T = \frac{s^T\tilde{L}^T}{\tilde{m}^T}$, the system which comprises eqs. (171b), (171d) and (171f) can be reduced to two equations:

$$\tilde{L}^T = \frac{\tilde{m}^T}{\tilde{m}^T + s^T}\left[\bar{\lambda}\left(\frac{\alpha_W^T}{1-\alpha_W^T}\kappa^T\tilde{\theta}^T + R^T\right)\right]^{\sigma_L^T}, \tag{172a}$$

$$\frac{\kappa^T}{f^T\left(\tilde{\theta}^T\right)} = \frac{\left(1-\alpha_W^T\right)}{\left(s^T + r^\star\right)}\tilde{\Psi}^T, \tag{172b}$$

where $\tilde{m}^T = m^T\left(\tilde{\theta}^T\right)$ and $\tilde{f}^T = f^T\left(\tilde{\theta}^T\right)$; using the fact the reservation wage $W_R^T = -\frac{v_F^T}{\bar{\lambda}}$ is equal to $\left(\frac{\alpha_W^T}{1-\alpha_W^T}\kappa^T\tilde{\theta}^T + R^T\right)$ (see eq. (110)), the overall surplus from hiring in the traded sector is given by:

$$\tilde{\Psi}^T \equiv \left(A^T + r^\star x^T\right) - \left(\frac{\alpha_W^T}{1-\alpha_W^T}\kappa^T\tilde{\theta}^T + R^T\right). \tag{173}$$

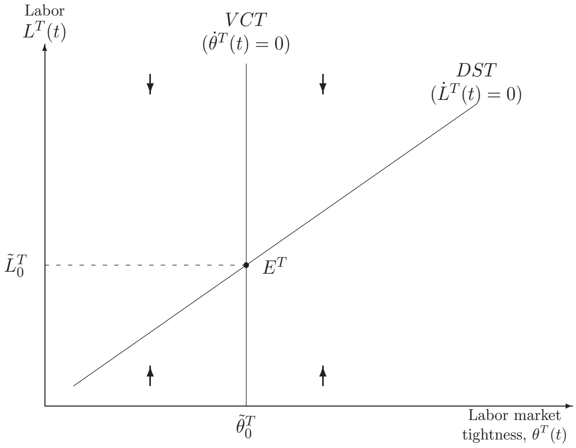
Totally differentiating eq. (172a) yields

$$\hat{\tilde{L}}^T = \sigma_L^T\hat{\bar{\lambda}} + \left[\alpha_V^T\tilde{u}^T + \sigma_L^T\tilde{\chi}^T\right]\hat{\tilde{\theta}}^T, \tag{174}$$

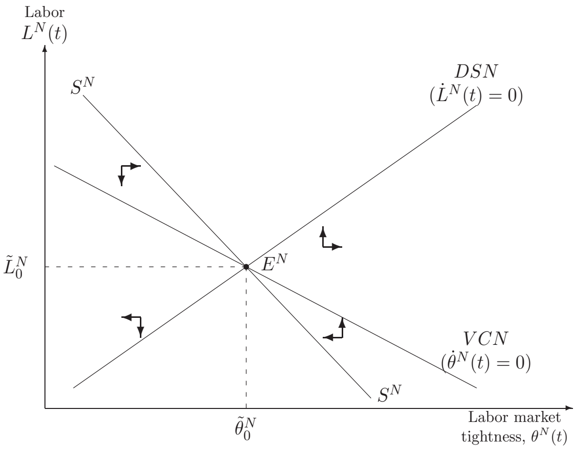
where $\tilde{u}^T = \frac{s^T}{s^T+\tilde{m}^T}$ and $0 < \tilde{\chi}^T = \frac{\frac{\alpha_W^T}{1-\alpha_W^T}\kappa^T\tilde{\theta}^T}{W_R^T} < 1$. The slope of the $\dot{L}^T = 0$ schedule in the (θ^T, L^T)-space writes as:

$$\left.\frac{\hat{\tilde{L}}^T}{\hat{\tilde{\theta}}^T}\right|_{\dot{L}^T=0} = \left[\alpha_V^T\tilde{u}^T + \sigma_L^T\tilde{\chi}^T\right] > 0. \tag{175}$$

Hence the decision of search (henceforth labelled DST) schedule is upward-sloping in the (θ^T, L^T)-space. According to (174), a fall in the marginal utility of wealth $\bar{\lambda}$ shifts downward the DST-schedule.



(a) (θ^T, L^T)-space



(b) (θ^N, L^N)-space

Figure 6: Phase Diagrams

Totally differentiating eq. (172b) yields

$$\hat{\tilde{\theta}}^T \left[\left(1 - \alpha_V^T\right) \tilde{\Psi}^T + \tilde{\chi}^T W_R^T \right] = A^T \hat{A}^T, \tag{176}$$

where we used (171f) and the fact that $-\left(f^T\right)' \theta^T / f^T = \left(1 - \alpha_V^T\right)$. The slope of the $\dot{\theta}^T = 0$ schedule in the (θ^T, L^T)-space can be written as:

$$\left. \frac{\hat{\tilde{L}}^T}{\hat{\tilde{\theta}}^T} \right|_{\dot{\theta}^T = 0} = +\infty. \tag{177}$$

Hence the vacancy creation (henceforth labelled VCT) schedule is a vertical line in the (θ^T, L^T)-space. According to (176), a rise in labor productivity in the traded sector A^T shifts to the right the VCT-schedule.

Having determined the patterns of isoclines in the (θ^T, L^T)-space, we now analyze the slope of the stable path. To determine the pattern of the stable path, we have to estimate:

$$\frac{\frac{L^T(t) - \tilde{L}^T}{\tilde{L}^T}}{\frac{\theta^T(t) - \tilde{\theta}^T}{\tilde{\theta}^T}} = \frac{1}{\omega_{21}^T} \frac{\tilde{\theta}^T}{\tilde{L}^T}. \tag{178}$$

Using the fact that $\omega_{21}^T = 0$ (see (149)), the slope of the stable branch labelled SS^T in the (θ, L)-space rewrites as:

$$\left. \frac{\hat{\tilde{L}}^T}{\hat{\tilde{\theta}}^T} \right|_{SS^T} = +\infty. \tag{179}$$

According to (179), the stable branch coincides with the VCT-schedule (see Figure 6(a)) as the dynamics for θ^T degenerate.

G.3 Isoclines and Stable Path in the (θ^N, L^N)-space

The labor market in the non traded sector can be summarized graphically by Figure 6(b) that traces out two schedules in the (θ^N, L^N)-space. More precisely, eliminating $\tilde{U}^N$ from eq. (171e) by using (171c), i.e., $\tilde{U}^N = \frac{s^N \tilde{L}^N}{\tilde{m}^N}$, and inserting the short-run static solution for the relative price of non tradables given by (115) implies that the system which comprises eqs. (171c), (171e), (171g), and (171h) can be reduced to two equations:

$$\tilde{L}^N = \frac{\tilde{m}^N}{\tilde{m}^N + s^N}\left[\bar{\lambda}\left(\frac{\alpha_W^N}{1-\alpha_W^N}\kappa^N\tilde{\theta}^N + R^N\right)\right]^{\sigma_L^N}, \tag{180a}$$

$$\frac{\kappa^N}{f^N\left(\tilde{\theta}^N\right)} = \frac{\left(1-\alpha_W^N\right)}{\left(s^N + r^\star\right)}\tilde{\Psi}^N, \tag{180b}$$

where $\tilde{m}^N = m^N\left(\tilde{\theta}^N\right)$ and $\tilde{f}^N = f^N\left(\tilde{\theta}^N\right)$; using the fact the reservation wage $W_R^N = -\frac{v_F^N}{\bar{\lambda}}$ is equal to $\left(\frac{\alpha_W^N}{1-\alpha_W^N}\kappa^N\tilde{\theta}^N + R^N\right)$ (see eq. (110)), the overall surplus from hiring in the non traded sector is given by:

$$\tilde{\Psi}^N \equiv \left[\left(P\left(L^N, \bar{\lambda}, A^N\right)A^N + r^\star x^N\right)\right] - \left(\frac{\alpha_W^N}{1-\alpha_W^N}\kappa^N\tilde{\theta}^N + R^N\right). \tag{181}$$

Totally differentiating eq. (180a) yields

$$\hat{\tilde{L}}^N = \sigma_L^N\hat{\bar{\lambda}} + \left[\alpha_V^N\tilde{u}^N + \sigma_L^N\tilde{\chi}^N\right]\hat{\tilde{\theta}}^N, \tag{182}$$

where $\tilde{u}^N = \frac{s^N}{s^N+\tilde{m}^N}$ and $0 < \tilde{\chi}^N = \frac{\frac{\alpha_W^N}{1-\alpha_W^N}\kappa^N\tilde{\theta}^N}{W_R^N} < 1$. The slope of the $\dot{L}^N = 0$ schedule in the (θ^N, L^N)-space writes as:

$$\left.\frac{\hat{\tilde{L}}^N}{\hat{\tilde{\theta}}^N}\right|_{\dot{L}^N=0} = \left[\alpha_V^N\tilde{u}^N + \sigma_L^N\tilde{\chi}^N\right] > 0. \tag{183}$$

Hence the decision of search (henceforth labelled DSN) schedule is upward-sloping in the (θ^N, L^N)-space. According to (182), a fall in the marginal utility of wealth $\bar{\lambda}$ shifts downward the DSN-schedule.

Totally differentiating eq. (180b) yields

$$\hat{\tilde{\theta}}^N\left[\left(1-\alpha_V^N\right)\tilde{\Psi}^N + \tilde{\chi}^N W_R^N\right]$$
$$= -\frac{\tilde{P}A^N\left\{\omega_N\hat{\tilde{L}}^N + \sigma_C\alpha_C\omega_C\hat{\bar{\lambda}} + \left[\omega_N - \omega_C\alpha_C\left(\left(1-\alpha_C\right)\phi + \alpha_C\sigma_C\right)\right]\hat{A}^N +\right\}}{\alpha_C\omega_C\left[\left(1-\alpha_C\right)\phi + \alpha_C\sigma_C\right]}, \tag{184}$$

where we used (171g) and the fact that $-\left(f^N\right)'\theta^N/f^N = \left(1-\alpha_V^N\right)$. The slope of the $\dot{\theta}^N = 0$ schedule in the (θ^N, L^N)-space is:

$$\left.\frac{\hat{\tilde{L}}^N}{\hat{\tilde{\theta}}^N}\right|_{\dot{\theta}^N=0} = -\frac{\left[\left(1-\alpha_V^N\right)\tilde{\Psi}^N + \tilde{\chi}^N W_R^N\right]}{PA^N}\frac{\alpha_C\omega_C\left[\left(1-\alpha_C\right)\phi + \alpha_C\sigma_C\right]}{\omega_N} < 0. \tag{185}$$

Hence the vacancy creation (henceforth labelled VCN) schedule is downward-sloping in the (θ^N, L^N)-space. According to (185), since $\left[\omega_N - \omega_C\alpha_C\left(\left(1-\alpha_C\right)\phi + \alpha_C\sigma_C\right)\right] \gtreqless 0$, a rise in labor productivity in the non traded sector A^N may shift to the left or to the right the VCN-schedule depending on whether ϕ takes high or low values; it is worthwhile mentioning that that technological change biased toward the traded sector shifts to the right the VCN-schedule by appreciating the relative price and thus by raising the marginal revenue of labor in the non traded sector, i.e., by increasing $\Xi^N \equiv PA^N$. Moreover, a fall in the marginal utility of wealth $\bar{\lambda}$ shifts to the right the VCN-schedule by appreciating the relative price of non tradables.

Having determined the patterns of isoclines in the (θ^N, L^N)-space, we now analyze the slope of the stable path. To do so, we use the third line of the Jacobian matrix (136) to rewrite the element ω_{2i}^N of the eigenvector:

$$\omega_{2i}^N = \frac{\left(2s^N + r^\star\right) + \left(s^N + r^\star - \nu_i^N\right)\left(\frac{s^N+\nu_i^N}{\tilde{m}^N}\right) + \tilde{m}^N\left(P_{L^N}A^N\frac{\bar{\lambda}}{v_{FF}^N} + 1\right)}{\frac{(m^N)'\tilde{U}^N}{\tilde{m}^N}\left(s^N + \tilde{m}^N + r^\star - \nu_i^N\right)}. \tag{186}$$

The first two terms in the numerator of (186) can be rewritten as follows:

$$\left(2s^N + r^\star\right) + \left(s^N + r^\star - \nu_i^N\right)\left(\frac{s^N + \nu_i^N}{s^N}\right) = s^N + \frac{\left(s^N + r^\star\right)\left(s^N + \tilde{m}^N\right) + \nu_i^N\left(r^\star - \nu_i^N\right)}{\tilde{m}^N}, \quad (187)$$

where $\nu_i^N\left(r^\star - \nu_i^N\right)$ is equal to the determinant of the Jacobian matrix (136) given by (141). To determine the pattern of the stable path in the (θ^N, L^N)-space, we have to estimate:

$$\frac{\frac{L^N(t)-\tilde{L}^N}{\tilde{L}^N}}{\frac{\theta^N(t)-\tilde{\theta}^N}{\tilde{\theta}^N}} = \frac{1}{\omega_{21}^N}\frac{\tilde{\theta}^N}{\tilde{L}^N}. \quad (188)$$

Inserting (145) into (188), the slope of the stable branch labelled $S^N S^N$ in the (θ^N, L^N)-space can be rewritten as follows:

$$\left.\frac{\hat{\tilde{L}}^N}{\hat{\tilde{\theta}}^N}\right|_{S^N S^N} = \frac{1}{\omega_{21}^N}\frac{\tilde{\theta}^N}{\tilde{L}^N} = -\frac{\left(s^N + \tilde{m}^N + r^\star - \nu_1^N\right)}{\left(s^N + r^\star\right)}\frac{\left(1-\alpha_V^N\right)\tilde{\Psi}^N}{\tilde{P}A^N}\frac{\alpha_C\omega_C\left[\left(1-\alpha_C\right)\phi + \alpha_C\sigma_C\right]}{\omega_N} < 0, \quad (189)$$

where we denote by a hat the rate of change relative to initial steady-state. According to (189), the stable branch SS^N is downward-sloping in the (θ^N, L^N)-space.

To get (189), we proceed as follows. We first have rewritten the numerator of eigenvector ω_{21}^N given by (186) (set $i = 1$) by using (187) and by inserting $\frac{\text{Det}J^N}{s^N + r^\star}$ (which is equal to $\nu_1^N\left(r^\star - \nu_1^N\right)$) given by (145):

$$s^N + \frac{\left(s^N + r^\star\right)\left(s^N + \tilde{m}^N\right) - \left(s^N + r^\star + \tilde{m}^N\right)\left(s^N + \tilde{m}^N\right)}{\tilde{m}^N} + \tilde{m}^N\left(P_{L^N}A^N\frac{\bar{\lambda}}{v_{FF}^N} + 1\right)$$

$$- \frac{\omega_N\tilde{P}A^N}{\alpha_C\omega_C\left[\left(1-\alpha_C\right)\phi + \alpha_C\sigma_C\right]}\frac{\left(s^N + r^\star\right)\left(s^N + \tilde{m}^N\right)\left(\tilde{\chi}^N\sigma_L^N + \alpha_V^N\tilde{u}^N\right)}{\left(1-\alpha_V^N\right)\tilde{\Psi}^N\tilde{m}^N}, \quad (190)$$

$$= -\frac{\omega_N\tilde{P}A^N}{\alpha_C\omega_C\left[\left(1-\alpha_C\right)\phi + \alpha_C\sigma_C\right]}\frac{\left(s^N + r^\star\right)\left(s^N + \tilde{m}^N\right)\alpha_V^N\tilde{u}^N}{\left(1-\alpha_V^N\right)\tilde{\Psi}^N\tilde{m}^N}. \quad (191)$$

To get the last line, we computed the following term $\tilde{m}^N\left(P_{L^N}A^N\frac{\bar{\lambda}}{v_{FF}^N} + 1\right)$ as follows:

$$\tilde{m}^N\left(P_{L^N}A^N\frac{\bar{\lambda}}{v_{FF}^N} + 1\right) = \tilde{m}^N\left(\frac{P_{L^N}\tilde{L}^N}{\tilde{P}}\frac{\tilde{P}A^N}{\tilde{L}^N}\tilde{F}^N\sigma_L^N\frac{\bar{\lambda}}{v_F^N} + 1\right),$$

$$= \tilde{m}^N\left\{\frac{\omega_N\tilde{P}A^N}{\alpha_C\omega_C\left[\left(1-\alpha_C\right)\phi + \alpha_C\sigma_C\right]}\frac{s^N + \tilde{m}^N}{\tilde{m}^N}\frac{\left(s^N + r^\star\right)\sigma_L^N\tilde{\chi}^N}{\alpha_W^N\tilde{\Psi}^N\tilde{m}^N} + 1\right\}, \quad (192)$$

where we used the fact that $\frac{v_F^N}{v_{FF}^N\tilde{F}^N} = \sigma_L^N$ to get the first line, $\frac{\tilde{L}^N}{\tilde{F}^N} = \frac{\tilde{m}^N}{s^N + \tilde{m}^N}$ and $\frac{P_{L^N}\tilde{L}^N}{\tilde{P}} = \frac{\omega_N\tilde{P}A^N}{\alpha_C\omega_C\left[(1-\alpha_C)\phi + \alpha_C\sigma_C\right]}$ to get the second line, $\tilde{m}^N\tilde{\xi}^N = \tilde{m}^N\frac{\alpha_W^N\tilde{\Psi}^N}{\left(s^N + r^\star\right)} = -\tilde{chi}^N\frac{v_F^N}{\bar{\lambda}}$ to get (192). Inserting (192) into (190), rearranging terms, we get (191).

Inserting first (192), and multiplying ω_{21}^N (setting setting $i = 1$ into (186)) by $\tilde{L}^N/\tilde{\theta}^N$, we get:

$$\omega_{21}^N\frac{\tilde{L}^N}{\tilde{\theta}^N} = -\frac{\frac{\omega_N\tilde{P}A^N}{\alpha_C\omega_C\left[(1-\alpha_C)\phi + \alpha_C\sigma_C\right]}\frac{\left(s^N + r^\star\right)\left(s^N + \tilde{m}^N\right)}{\left(1-\alpha_V^N\right)\tilde{\Psi}^N\tilde{m}^N}\frac{\tilde{L}^N}{\tilde{F}^N}}{\left(s^N + \tilde{m}^N + r^\star - \nu_1^N\right)}$$

$$= -\frac{\frac{\omega_N\tilde{P}A^N}{\alpha_C\omega_C\left[(1-\alpha_C)\phi + \alpha_C\sigma_C\right]}\frac{\left(s^N + r^\star\right)}{\left(1-\alpha_V^N\right)\tilde{\Psi}^N}}{\left(s^N + \tilde{m}^N + r^\star - \nu_1^N\right)} < 0, \quad (193)$$

where we used the fact that $\left(m^N\right)'\theta^N/m^N = \alpha_V^N$ and $\tilde{u}^N = \tilde{U}^N/\tilde{F}^N$ to get the first line, $\frac{\tilde{L}^N}{\tilde{F}^N} = \frac{\tilde{m}^N}{s^N + \tilde{m}^N}$ to get (193).

Because both the VCN-schedule and the stable branch $S^N S^N$ are downward sloping, we have now to determine whether the stable branch $S^N S^N$ is steeper or flatter than the VCN-schedule. To do so, we compute the following term which shows up in eq. (185):

$$\left(1-\alpha_V^N\right)\tilde{\Psi}^N + \tilde{\chi}^N W_R^N = \left(1-\alpha_V^N\right)\tilde{\Psi}^N\frac{\left(s^N + \tilde{m}^N + r^\star\right)}{\left(s^N + r^\star\right)}, \quad (194)$$

where we used the fact that $\tilde{\chi}^N W_R^N = \frac{\tilde{m}^N\alpha_W^N\tilde{\Psi}^N}{s^N + r^\star} = \frac{\tilde{m}^N\left(1-\alpha_V^N\right)\tilde{\Psi}^N}{s^N + r^\star}$. Since $\frac{\left(s^N + \tilde{m}^N + r^\star - \nu_1^N\right)}{\left(s^N + r^\star\right)} > \frac{\left(s^N + \tilde{m}^N + r^\star\right)}{\left(s + r^\star\right)}$, inspection of (185) and (189) implies that the $S^N S^N$-schedule is steeper than the VCN-schedule (see Figure 6(b)).

We turn now to the transitional adjustment along the stable path in the (L^N, U^N)-space by making use of (151b):

$$U^N(t) - \tilde{U}^N = \omega_{31}^N \left(L^N(t) - \tilde{L}^N\right), \tag{195}$$

where ω_{31}^N is given by eq. (151b). To sign the slope of the transitional path in the (L^N, U^N)-space, we use the third line of the Jacobian matrix (136) to rewrite the element ω_{21}^N of the eigenvector:

$$\omega_{21}^N = \frac{\left(2s^N + r^\star\right) + \left(s^N + r^\star - \nu_1^N\right)\left(\frac{s^N+\nu_1^N}{\tilde{m}^N}\right) + \frac{\tilde{m}^N \tilde{\Psi}_{L^N}}{\tilde{\Psi}_{U^N}}}{\frac{(m^N)'\tilde{U}^N}{\tilde{m}^N}\left(s^N + \tilde{m}^N + r^\star - \nu_1^N\right)}. \tag{196}$$

where $\tilde{\Psi}_{L^N}$ and $\tilde{\Psi}_{U^N}$ and the partial derivatives (evaluated at the steady-state) of the overall surplus from an additional job Ψ^N in the non traded sector:

$$\Psi_{L^N}^N = \frac{\partial \Psi^N}{\partial L^N} = P_{L^N} A^N + \frac{v_{FF}^N}{\bar{\lambda}} < 0, \tag{197a}$$

$$\Psi_{U^N}^N = \frac{\partial \Psi^N}{\partial U^N} = \frac{v_{FF}^N}{\bar{\lambda}} < 0. \tag{197b}$$

Inserting (196) into (151b) allows to rewrite ω_{31}^N as follows:

$$\begin{aligned}
\omega_{31}^N &= \left(\frac{s^N + \nu_1^N}{\tilde{m}^N}\right) - \frac{\left(m^N\right)'\tilde{U}^N}{\tilde{m}^N}\omega_{21}^N, \\
&= \left(\frac{s^N + \nu_1^N}{\tilde{m}^N}\right) - \frac{\left(2s^N + r^\star\right) + \left(s^N + r^\star - \nu_1^N\right)\left(\frac{s^N+\nu_1^N}{\tilde{m}^N}\right) + \frac{\tilde{m}^N \tilde{\Psi}_{L^N}}{\tilde{\Psi}_{U^N}}}{\left(s^N + \tilde{m}^N + r^\star - \nu_1^N\right)}, \\
&= \frac{\left(s^N + \nu_1^N\right) - \left(2s^N + r^\star\right) - \frac{\tilde{m}^N \tilde{\Psi}_{L^N}}{\tilde{\Psi}_{U^N}}}{\left(s^N + \tilde{m}^N + r^\star - \nu_1^N\right)}, \\
&= -\frac{\left[\left(s^N + r^\star - \nu_1^N\right) + \frac{\tilde{m}^N \tilde{\Psi}_{L^N}}{\tilde{\Psi}_{U^N}}\right]}{\left(s^N + \tilde{m}^N + r^\star - \nu_1^N\right)} < 0,
\end{aligned} \tag{198}$$

where $\nu_1^N < 0$ is the stable root for the non traded labor market. Since according to (197), $\tilde{\Psi}_{L^N} < 0$ and $\tilde{\Psi}_{U^N} < 0$, we have $\omega_{31}^N < 0$. Hence, as employment declines in the non traded sector, job seekers increase in this sector.

H Steady-State and Short-Run Effects of a Productivity Differential

In this section, we first derive the steady-state changes following a productivity differential between tradables and non tradables, i.e., $\hat{a}^T - \hat{a}^N > 0$. Steady-state values are denoted with a tilde while the rate of change relative to initial steady-state is denoted by a hat. Then, we analyze the dynamic adjustment toward the long-run equilibrium following technological change biased toward the traded sector.

H.1 Solving Analytically for the Steady-State

Eliminating $\tilde{U}^T$ from eq. (171d) by using (171b), i.e., $\tilde{U}^T = \frac{s^T \tilde{L}^T}{\tilde{m}^T}$, eliminating $\tilde{U}^N$ from eq. (171e) by using (171c), i.e., $\tilde{U}^N = \frac{s^N \tilde{L}^N}{\tilde{m}^N}$, and inserting the short-run static solution for the relative price of non tradables given by (115), inserting the short-run static solution for consumption in tradables given by (117) into the market clearing condition for traded goods (171i), the steady-state can be reduced to a system which comprises six equations:

$$\tilde{L}^T = \frac{\tilde{m}^T}{\tilde{m}^T + s^T}\left[\bar{\lambda}\left(\frac{\alpha_W^T}{1-\alpha_W^T}\kappa^T\tilde{\theta}^T + R^T\right)\right]^{\sigma_L^T}, \quad (199a)$$

$$\frac{\kappa^T}{f^T\left(\tilde{\theta}^T\right)} = \frac{\left(1-\alpha_W^T\right)}{\left(s^T + r^\star\right)}\left[\left(A^T + r^\star x^T\right) - \left(\frac{\alpha_W^T}{1-\alpha_W^T}\kappa^T\tilde{\theta}^T + R^T\right)\right], \quad (199b)$$

$$\tilde{L}^N = \frac{\tilde{m}^N}{\tilde{m}^N + s^N}\left[\bar{\lambda}\left(\frac{\alpha_W^N}{1-\alpha_W^N}\kappa^N\tilde{\theta}^N + R^N\right)\right]^{\sigma_L^N}, \quad (199c)$$

$$\frac{\kappa^N}{f^N\left(\tilde{\theta}^N\right)} = \frac{\left(1-\alpha_W^N\right)}{\left(s^N + r^\star\right)}\left\{\left[\left(P\left(\tilde{L}^N, \bar{\lambda}, A^N\right)A^N + r^\star x^N\right)\right] - \left(\frac{\alpha_W^N}{1-\alpha_W^N}\kappa^N\tilde{\theta}^N + R^N\right)\right\}, \quad (199d)$$

$$r^\star\tilde{B} + A^T\tilde{L}^T - C^T\left(\tilde{L}^N, \bar{\lambda}, A^N\right) - \kappa^T\frac{s^T\tilde{L}^T}{\tilde{f}^T} - \kappa^N\frac{s^N\tilde{L}^N}{\tilde{f}^N}, \quad (199e)$$

and the intertemporal solvency condition

$$\tilde{B} - B_0 = \Phi^T\left(\tilde{L}^T - L_0^T\right) + \Phi^T\left(\tilde{L}^N - L_0^N\right), \quad (199f)$$

where we abstract from government spending on tradables and non tradables, $\Phi^T = -\frac{\left(A^T + \kappa^T\tilde{\theta}^T\right)}{\left(s^T + \tilde{m}^T + r^\star\right)} < 0$ and $\Phi^N \equiv \frac{\Lambda^N}{\nu_1^N - r^\star} < 0$ (see (157)); to get (199e), we use the fact that $\tilde{U}^j = \frac{s^j\tilde{L}^j}{\tilde{m}^j}$and $f^j = m^j/\theta^j$. Note that the market clearing condition for non tradables (171h) can be solved for the relative price of non tradables. To avoid unnecessary complications, we set $G^N = 0$ so that eq. (171h) reduces to $Y^N = C^N$. The solution for the relative price of non tradables is $P = P\left(L^N, \bar{\lambda}, A^N\right)$. Totally differentiating the market clearing condition for non tradables, we get:

$$\hat{p} = \frac{-\hat{a}^N - \hat{l}^N - \sigma_C\hat{\bar{\lambda}}}{\left[\left(1-\alpha_C\right)\phi + \alpha_C\sigma_C\right]} \quad (200)$$

Inserting (200) into the short-run static solution for consumption in tradables (113), we get:

$$\hat{C}^T = -\frac{\left[\sigma_C\hat{\bar{\lambda}} + \alpha_C\left(\phi - \sigma_C\right)\left(\hat{a}^N + \hat{l}^N\right)\right]}{\left[\left(1-\alpha_C\right)\phi + \alpha_C\sigma_C\right]}. \quad (201)$$

As will become clear later, it is convenient to first solve the steady-state without the intertemporal solvency condition (199f), i.e., to solve the system comprising (199a)-(199e), which allows us to express the steady-state values in terms of the stock of traded bonds, the marginal utility of wealth and labor productivity indices A^j (with $j = T, N$). Totally differentiating the system of equations (199a)-(199e), using both (200) and (201), yields in matrix form:

$$\begin{pmatrix} 1 & -\left[\alpha_V^T\tilde{u}^T + \sigma_L^T\tilde{\chi}^T\right] & 0 & 0 & 0 \\ 0 & \left[\left(1-\alpha_V^T\right)\tilde{\Psi}^T + \tilde{\chi}^T W_R^T\right] & 0 & 0 & 0 \\ 0 & 0 & 1 & -\left[\alpha_V^N\tilde{u}^N + \sigma_L^N\tilde{\chi}^N\right] & 0 \\ 0 & 0 & \tilde{P}A^N & a_{44} & 0 \\ a_{51} & -\omega_V^T\left(1-\alpha_V^T\right) & a_{53} & -\omega_V^N\left(1-\alpha_V^N\right) \end{pmatrix}\begin{pmatrix} \hat{\tilde{L}}^T \\ \hat{\tilde{\theta}}^T \\ \hat{\tilde{L}}^N \\ \hat{\tilde{\theta}}^N \\ \mathrm{d}\tilde{B}/\tilde{Y} \end{pmatrix}$$

$$= \begin{pmatrix} \sigma_L^T\hat{\bar{\lambda}} \\ A^T\hat{a}^T \\ \sigma_L^N\hat{\bar{\lambda}} \\ -\tilde{P}A^N\sigma_C\hat{\bar{\lambda}} + \tilde{P}A^N\left\{\left[\left(1-\alpha_C\right)\phi + \alpha_C\sigma_C\right] - 1\right\}\hat{a}^N \\ -\left(1-\omega_N\right)\hat{a}^T - \frac{\left(1-\alpha_C\right)\omega_C\alpha_C\left(\phi-\sigma_C\right)}{\left[\left(1-\alpha_C\right)\phi+\alpha_C\sigma_C\right]}\hat{a}^N - \frac{\left(1-\alpha_C\right)\omega_C\sigma_C\phi}{\left[\left(1-\alpha_C\right)\phi+\alpha_C\sigma_C\right]}\hat{\bar{\lambda}} \end{pmatrix}, \quad (202)$$

where we used the fact that $\frac{C^T}{Y} = \frac{C^T}{P_C C}\frac{P_C C}{Y} = \left(1-\alpha_C\right)\omega_C$, and $\frac{Y^T}{Y} = \left(1-\omega_N\right)$, we set $\omega_V^j = \frac{\kappa V}{Y}$; the terms a_{44}, a_{51}, a_{53} are given by:

$$a_{44} = \left[\left(1-\alpha_V^N\right)\tilde{\Psi}^N + \tilde{\chi}^N\tilde{W}_R^N\right]\left[\left(1-\alpha_C\right)\phi + \alpha_C\sigma_C\right], \quad (203a)$$

$$a_{51} = \left[\left(1-\omega_N\right) - \omega_V^T\right], \quad (203b)$$

$$a_{53} = \left\{\frac{\left(1-\alpha_C\right)\omega_C\alpha_C\left(\phi-\sigma_C\right)}{\left[\left(1-\alpha_C\right)\phi + \alpha_C\sigma_C\right]} - \omega_V^N\right\}. \quad (203c)$$

System (199a)-(199e) can be solved for steady-state employment and labor market tightness in the traded and non traded sectors, and the stock of foreign assets as follows:

$$\tilde{L}^T = L^T\left(\bar{\lambda}, A^T\right), \tag{204a}$$
$$\tilde{\theta}^T = \theta^T\left(A^T\right), \tag{204b}$$
$$\tilde{L}^N = L^N\left(\bar{\lambda}, A^N\right), \tag{204c}$$
$$\tilde{\theta}^N = \theta^N\left(\bar{\lambda}, A^N\right), \tag{204d}$$
$$\tilde{B} = B\left(\bar{\lambda}, A^T, A^N\right), \tag{204e}$$

where partial derivatives are given by

$$\frac{\hat{\tilde{\theta}}^T}{\hat{a}^T} = \frac{A^T}{\left[\left(1-\alpha_V^T\right)\tilde{\Psi}^T + \tilde{\chi}^T W_R^T\right]} > 0, \tag{205a}$$

$$\frac{\hat{\tilde{L}}^T}{\hat{\bar{\lambda}}} = \sigma_L^T > 0, \tag{205b}$$

$$\frac{\hat{\tilde{L}}^T}{\hat{a}^T} = \frac{\left[\alpha_V^T \tilde{u}^T + \sigma_L^T \tilde{\chi}^T\right] A^T}{\left[\left(1-\alpha_V^T\right)\tilde{\Psi}^T + \tilde{\chi}^T W_R^T\right]} > 0, \tag{205c}$$

$$\frac{\hat{\tilde{\theta}}^N}{\hat{\bar{\lambda}}} = -\frac{\tilde{P}A^N\left(\sigma_L^N + \sigma_C\right)}{\left[\left(1-\alpha_V^N\right)\tilde{\Psi}^N + \tilde{\chi}^N W_R^N\right]\left[\left(1-\alpha_C\right)\phi + \alpha_C\sigma_C\right] + \tilde{P}A^N\left[\alpha_V^N \tilde{u}^N + \sigma_L^N \tilde{\chi}^N\right]} < 0, \tag{205d}$$

$$\frac{\hat{\tilde{\theta}}^N}{\hat{a}^N} = \frac{\tilde{P}A^N\left\{\left[\left(1-\alpha_C\right)\phi + \alpha_C\sigma_C\right] - 1\right\}}{\left[\left(1-\alpha_V^N\right)\tilde{\Psi}^N + \tilde{\chi}^N W_R^N\right]\left[\left(1-\alpha_C\right)\phi + \alpha_C\sigma_C\right] + \tilde{P}A^N\left[\alpha_V^N \tilde{u}^N + \sigma_L^N \tilde{\chi}^N\right]} > 0, \tag{205e}$$

$$\frac{\hat{\tilde{L}}^N}{\hat{\bar{\lambda}}} = \frac{\sigma_L^N\left[\left(1-\alpha_V^N\right)\tilde{\Psi}^N + \tilde{\chi}^N W_R^N\right]\left[\left(1-\alpha_C\right)\phi + \alpha_C\sigma_C\right] - \sigma_C\tilde{P}A^N\left[\alpha_V^N \tilde{u}^N + \sigma_L^N \tilde{\chi}^N\right]}{\left[\left(1-\alpha_V^N\right)\tilde{\Psi}^N + \tilde{\chi}^N W_R^N\right]\left[\left(1-\alpha_C\right)\phi + \alpha_C\sigma_C\right] + \tilde{P}A^N\left[\alpha_V^N \tilde{u}^N + \sigma_L^N \tilde{\chi}^N\right]} \gtrless 0, \tag{205f}$$

$$\frac{\hat{\tilde{L}}^N}{\hat{a}^N} = \frac{\tilde{P}A^N\left\{\left[\left(1-\alpha_C\right)\phi + \alpha_C\sigma_C\right] - 1\right\}\left[\alpha_V^N \tilde{u}^N + \sigma_L^N \tilde{\chi}^N\right]}{\left[\left(1-\alpha_V^N\right)\tilde{\Psi}^N + \tilde{\chi}^N W_R^N\right]\left[\left(1-\alpha_C\right)\phi + \alpha_C\sigma_C\right] + \tilde{P}A^N\left[\alpha_V^N \tilde{u}^N + \sigma_L^N \tilde{\chi}^N\right]} > 0, \tag{205g}$$

$$\frac{\mathrm{d}\tilde{B}/\tilde{Y}}{\hat{a}^T} = -\left\{\left(1-\omega_N\right) + \frac{\left\{\left[\left(1-\omega_N\right) - \omega_V^T\right]\left[\alpha_V^T \tilde{u}^T + \sigma_L^T \tilde{\chi}^T\right] - \omega_V^T\left(1-\alpha_V^T\right)\right\} A^T}{\left[\left(1-\alpha_V^T\right)\tilde{\Psi}^T + \tilde{\chi}^T W_R^T\right]}\right\} < 0, \tag{205h}$$

$$\begin{aligned}\frac{\mathrm{d}\tilde{B}/\tilde{Y}}{\hat{a}^N} &= -\left\{\frac{\tilde{P}A^N\left\{\left[\left(1-\alpha_C\right)\phi + \alpha_C\sigma_C\right] - 1\right\}\left[\alpha_V^N \tilde{u}^N + \sigma_L^N \tilde{\chi}^N\right]\left[\frac{(1-\alpha_C)\omega_C\alpha_C(\phi-\sigma_C)}{(1-\alpha_C)\phi+\alpha_C\sigma_C} - \omega_V^N\right]}{\left[\left(1-\alpha_V^N\right)\tilde{\Psi}^N + \tilde{\chi}^N W_R^N\right]\left[\left(1-\alpha_C\right)\phi + \alpha_C\sigma_C\right] + \tilde{P}A^N\left[\alpha_V^N \tilde{u}^N + \sigma_L^N \tilde{\chi}^N\right]}\right. \\ &+ \left.\frac{\left(1-\alpha_C\right)\omega_C\alpha_C\left(\phi-\sigma_C\right)}{\left[\left(1-\alpha_C\right)\phi + \alpha_C\sigma_C\right]}\right\} < 0, \end{aligned} \tag{205i}$$

$$\begin{aligned}\frac{\mathrm{d}\tilde{B}/\tilde{Y}}{\hat{\bar{\lambda}}} &= -\left\{\left[\left(1-\omega_N\right) - \omega_V^T\right]\sigma_L^T + \frac{\left(1-\alpha_C\right)\omega_C\sigma_C\phi}{\left[\left(1-\alpha_C\right)\phi + \alpha_C\sigma_C\right]}\right. \\ &+ \frac{\sigma_L^N\left[\frac{(1-\alpha_C)\omega_C\alpha_C(\phi-\sigma_C)}{(1-\alpha_C)\phi+\alpha_C\sigma_C} - \omega_V^N\right]\left[\left(1-\alpha_V^N\right)\tilde{\Psi}^N + \tilde{\chi}^N W_R^N\right]\left[\left(1-\alpha_C\right)\phi + \alpha_C\sigma_C\right]}{\left[\left(1-\alpha_V^N\right)\tilde{\Psi}^N + \tilde{\chi}^N W_R^N\right]\left[\left(1-\alpha_C\right)\phi + \alpha_C\sigma_C\right] + \tilde{P}A^N\left[\alpha_V^N \tilde{u}^N + \sigma_L^N \tilde{\chi}^N\right]} \\ &- \left.\frac{\tilde{P}A^N\sigma_C\left[\alpha_V^N \tilde{u}^N + \sigma_L^N \tilde{\chi}^N\right]\left[\frac{(1-\alpha_C)\omega_C\alpha_C(\phi-\sigma_C)}{(1-\alpha_C)\phi+\alpha_C\sigma_C} - \omega_V^N\right]}{\left[\left(1-\alpha_V^N\right)\tilde{\Psi}^N + \tilde{\chi}^N W_R^N\right]\left[\left(1-\alpha_C\right)\phi + \alpha_C\sigma_C\right] + \tilde{P}A^N\left[\alpha_V^N \tilde{u}^N + \sigma_L^N \tilde{\chi}^N\right]}\right\} \lesseqgtr 0. \end{aligned} \tag{205j}$$

H.2 The Dynamic Adjustment

The tilde is suppressed below for the purposes of clarity. We now explore effects of technological change biased toward the traded sector by focusing on the labor market. Figure 7(a) depicts the labor market equilibrium in the traded sector which can be summarized by two schedules:[59]

$$L^T = \frac{m^T}{m^T + s^T} \left(\bar{\lambda} W_R^T\right)^{\sigma_L^T}, \tag{206a}$$

$$\frac{\kappa^T}{f^T} = \frac{\left(1-\alpha_W^T\right)\left[\left(A^T + r^\star x^T\right) - W_R^T\right]}{s^T + r^\star}, \tag{206b}$$

where $W_R^T \equiv \left(\frac{\alpha_W^T}{1-\alpha_W^T}\kappa^T\theta^T + R^T\right)$ is the reservation wage in the traded sector. The first equation (206a) represents the decision of search schedule in the traded sector (henceforth DST) which is upward-sloping in the (θ^T, L^T)-space. The reason is that a rise in the labor market tightness raises the probability of finding a job and thus increases employment L^T by reducing the number of job seekers. Moreover, because we consider an endogenous labor force participation decision, the consecutive increase in the reservation wage induces agents to supply more labor. The second equation (206b) represents the vacancy creation schedule (henceforth VCT) which is a vertical line in the (θ^T, L)-space. Note that Figure 7(a) depicts the logarithm form of the system (206).

By raising the surplus from hiring, a rise in labor productivity in the traded sector A^T shifts to the right the VCT-schedule from VCT_0 to VCT_1. Because traded firms post more job vacancies, the labor market tightness θ_1^T exceeds its initial level θ_0^T. Note that θ^T jumps immediately to its new higher steady-state level while traded employment builds up over time along the isocline $\dot{\theta}^T = 0$ until the economy reaches the new steady-state. While increased labor market tightness raises traded employment by pushing up the reservation wage and reducing unemployment, the positive wealth effect moderates the expansionary effect on labor supply. Graphically, the fall in $\bar{\lambda}$ shifts to the right the DST-schedule. The new steady state is E_1^T.

Since we are interested in the movement of sectoral wages, it is useful to explore the long-run adjustment in the traded wage following a rise in labor productivity A^T. The labor market in the traded sector can alternatively be summarized graphically in the (θ^T, W^T)-space as shown in Figure 8(a). Using the fact $\left(1-\alpha_W^T\right)\Psi^T = A^T - W^T$, the VCT-schedule is downward sloping and convex toward the origin, reflecting diminishing returns in vacancy creation. The slope of the VCT-schedule in the (θ^T, W^T)-space is:

$$\left.\frac{\mathrm{d}W^T}{\mathrm{d}\theta^T}\right|^{VCT} = -\frac{\left(s^T + r^\star\right)\kappa^T\left(1-\alpha_V^T\right)}{f^T\theta^T} = -\frac{\left(1-\alpha_W^T\right)\Psi^T\left(1-\alpha_V^T\right)}{\theta^T} < 0. \tag{207}$$

The wage setting-schedule (WST henceforth) is upward sloping (see eq. (24)). Using the fact that $\left(F^T\right)^{1/\sigma_L^T}/\bar{\lambda} = W_R^T$, the WST-schedule is $W^T = \alpha_W^T\left(A^T + r^\star x^T\right) + \left(1-\alpha_W^T\right)W_R^T$ with a slope in the (θ^T, W^T)-space given by:

$$\left.\frac{\mathrm{d}W^T}{\mathrm{d}\theta^T}\right|^{WST} = \frac{\left(1-\alpha_W^T\right)\chi^T W_R^T}{\theta^T} = \alpha_W^T\kappa^T > 0. \tag{208}$$

A rise in A^T shifts to the right the VCT-schedule by stimulating labor demand which exerts an upward pressure on the the traded wage. Because workers get a fraction α_W^T of the increased surplus, the productivity shock shifts to the left the WST-schedule.[60] Hence, the new steady-state at F_1^T is associated with a higher traded wage. The higher the worker bargaining power, the larger the shift of the WST curve and thereby the more W^T increases. To see it formally, totally differentiating the Nash bargaining traded wage and eliminating θ^T by using the vacancy creation schedule (i.e., eq. (206b)) yields the deviation in percentage of the traded wage from its initial steady state:[61]

$$\hat{w}^T = \Omega^T\hat{a}^T > 0, \quad \Omega^T = \frac{\alpha_W^T\left[\left(1-\alpha_V^T\right)\left(s^T + r^\star\right) + m^T\right]}{\left[\left(1-\alpha_V^T\right)\left(s^T + r^\star\right) + \alpha_W^T m^T\right]}\frac{A^T}{W^T}, \tag{209}$$

where $\Omega^T > 0$ represents the sensitivity of the traded wage to a change in the labor productivity index A^T.

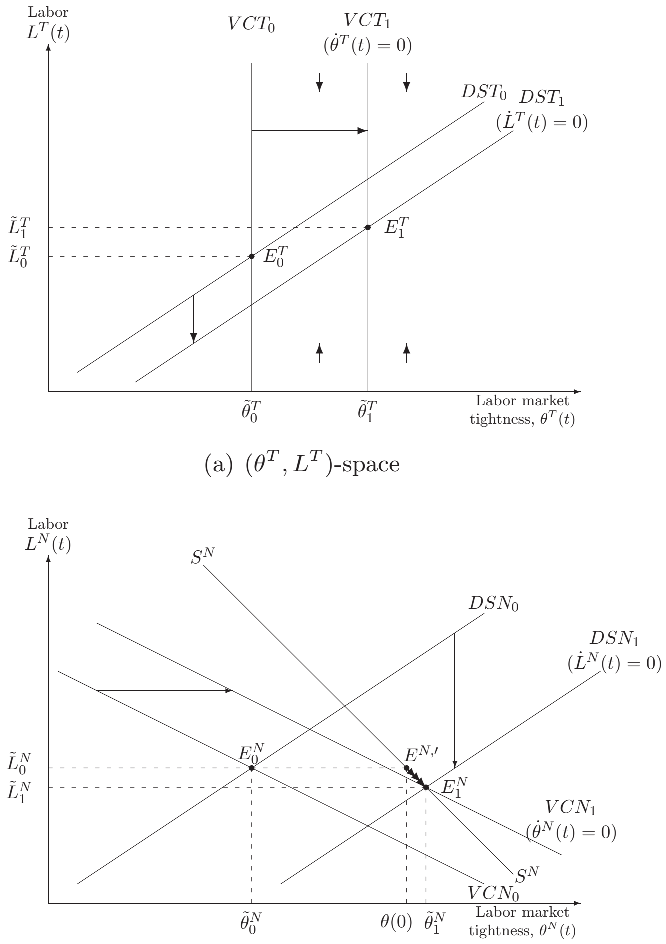
[59] Totally differentiating the DST- and VCT-schedule yields:

$$\hat{l}^T = \sigma_L^T\hat{\bar{\lambda}} + \left[\alpha_V^T u^T + \sigma_L^T\chi^T\right]\hat{\theta}^T, \quad \hat{\theta}^T = \frac{A^T}{\left[\left(1-\alpha_V^T\right)\tilde{\Psi}^T + \tilde{\chi}^T W_R^T\right]}\hat{a}^T.$$

The slope of the DST-schedule in the (θ^T, L^T)-space is given by $\left[\alpha_V^T u^T + \sigma_L^T\chi^T\right] > 0$.

[60] Note that the shift in the VCT-schedule dominates the shift in the WST-schedule because workers and firms have to share the surplus, i.e., $0 < \alpha_W^T < 1$.

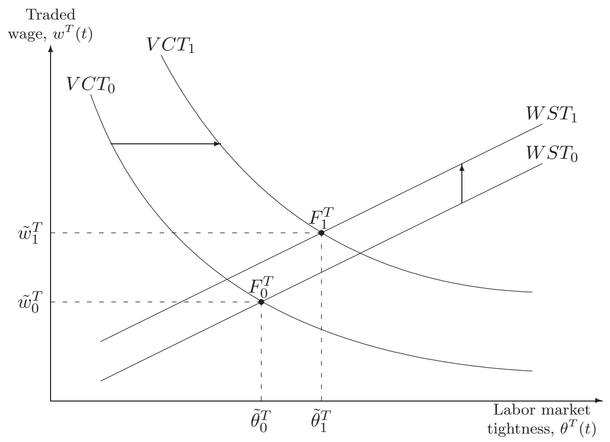
[61] To get (209), we used the fact that $\chi^T W_R^T = m^T\frac{\alpha_W^T\Psi^T}{s^T + r^\star}$.



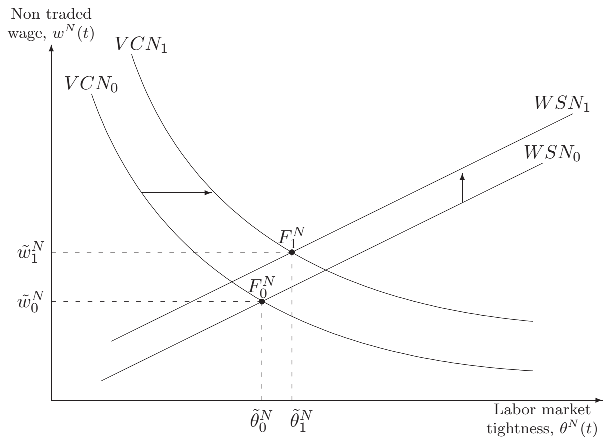
(a) (θ^T, L^T)-space

(b) (θ^N, L^N)-space

Figure 7: Effects of a Productivity Differential and the Stable Adjustment



(a) (θ^T, W^T)-space



(b) (θ^N, W^N)-space

Figure 8: Long-Run Sectoral Wage Effects of a Productivity Differential

We now turn to the non traded labor market equilibrium depicted in Figure 7(b) which is summarized by two schedules:

$$L^N = \frac{m^N}{m^N + s^N} \left(\bar{\lambda} W_R^N\right)^{\sigma_L^N}, \tag{210a}$$

$$\frac{\kappa^N}{f^N} = \frac{\left(1 - \alpha_W^N\right) \left[\left(P\left(L^N, \bar{\lambda}, A^N\right) A^N + r^\star x^N\right) - W_R^N\right]}{s^N + r^\star}, \tag{210b}$$

where we have inserted the short-run static solution for the relative price of non tradables (115) and $W_R^N \equiv \left(\frac{\alpha_W}{1-\alpha_W}\kappa^N \theta^N + R^N\right)$ is the reservation wage in the non traded sector. While eq. (210a) represents the decision of search schedule (henceforth DSN) which is upward-sloping in the (θ^N, L^N)-space, eq. (210b) corresponds to the vacancy creation schedule in the non traded sector (henceforth VCN). Note that whether we consider the traded or the non traded sector, the same logic applies to explain the positive relationship between the employment and the labor market tightness along the DSj-schedule (with $j = T, N$).

Totally differentiating eq. (210a) gives the slope of the DSN-schedule:

$$\hat{l}^N = \sigma_L^N \hat{\bar{\lambda}} + \left[\alpha_V^N u^N + \sigma_L^N \chi^N\right] \hat{\theta}^N.$$

The slope of the DSN-schedule in the (θ^N, L^N)-space is given by $\left[\alpha_V^N u^N + \sigma_L^N \chi^N\right] > 0$. Totally differentiating (210b) gives the slope of the VCN-schedule:

$$\begin{aligned} & \hat{\theta}^N \left[\left(1 - \alpha_V^N\right) \tilde{\Psi}^N + \tilde{\chi}^N W_R^N\right] \left[\left(1 - \alpha_C\right) \phi + \alpha_C \sigma_C\right] \\ = & -PA^N \left\{\hat{l}^N + \sigma_C \hat{\bar{\lambda}} + \left\{1 - \left[\left(1 - \alpha_C\right) \phi + \alpha_C \sigma_C\right]\right\} \hat{a}^N\right\}. \end{aligned}$$

The slope of the VCN-schedule is negative and given by:

$$\left.\frac{\hat{L}^N}{\hat{\theta}^N}\right|^{VCN} = -\frac{PA^N}{\left[\left(1 - \alpha_V^N\right) \tilde{\Psi}^N + \tilde{\chi}^N W_R^N\right] \left[\left(1 - \alpha_C\right) \phi + \alpha_C \sigma_C\right]} < 0.$$

As depicted in Figure 7(b), the VCN-schedule is downward-sloping in the (θ^N, L^N)-space. The reason is as follows. Because an increase in non traded labor raises output of this sector, the relative price of non tradables must depreciate for the market clearing condition (26) to hold. The fall in P drives down the surplus from hiring an additional worker in the non traded sector which results in a decline in labor market tightness θ^N as firms post less job vacancies.

Imposing $\sigma_C = 1$, a rise in A^N raises the surplus from hiring if and only if the elasticity of substitution ϕ between traded and non traded goods is larger than one. The reason is that only in this case, the share of non tradables in total expenditure rises which results in an expansionary effect on labor demand in the non traded sector. In Figure 7(b), we assume that $\sigma_C = \phi = 1$, so that the productivity shock does not impinge on the vacancy creation decision because the share of non tradables remains unchanged. Yet, by producing a positive wealth effect, higher labor productivity of non tradables shifts the VSN-schedule to the right by inducing agents to consume more which in turn raises P and thereby the surplus from hiring. The fall of the shadow value of wealth also shifts the DSN-schedule to the right as agents are induced to supply less labor. While θ^N is unambiguously higher at the new steady-state E_1^N, the positive wealth effect exerts two conflicting effects on L^N. In Figure 7(b), non traded employment falls in line with our numerical results.[62]

We now explore the long-run adjustment in the non traded wage which is depicted in Figure 8(b). As for the traded sector, the WSN-schedule is upward sloping while the VCN-schedule is downward sloping. Formally, using the fact $\left(1 - \alpha_W^N\right) \Psi^N = PA^N + r^\star x^N - W^N$, the wage setting and vacancy creation decisions are described by the following equalities:

$$W^N = \alpha_W^N \left(PA^N + r^\star x^N\right) + \left(1 - \alpha_W^N\right) W_R^N, \tag{211a}$$

$$W^N = \left(PA^N + r^\star x^N\right) - \frac{\kappa^N \left(s^N + r^\star\right)}{f^N}. \tag{211b}$$

Before analyzing in more details the effects of a productivity shock on the non traded wage, it is convenient to determine analytically the long-run response of W^N. Totally differentiating the wage setting decision in the non traded sector allows us to solve for the change in the labor market tightness $\hat{\theta}^N = \frac{PA^N\left(\hat{p} + \hat{a}^N\right)}{\left[\left(1-\alpha_V^N\right)\Psi^N + \chi^N W_R^N\right]}$. Totally differentiating the Nash bargaining non traded wage

[62] In all scenarios, we numerically find that L^N declines.

and plugging $\hat{\theta}^N$, yields the deviation in percentage of the non traded wage from its initial steady state:

$$\hat{w}^N = \Omega^N \left(\hat{p} + \hat{a}^N\right), \quad \Omega^N = \frac{\alpha_W^N \left[\left(1-\alpha_V^N\right)\left(s^N + r^\star\right) + m^N\right]}{\left[\left(1-\alpha_V^N\right)\left(s^N + r^\star\right) + \alpha_W^N m^N\right]} \frac{PA^N}{W^N}. \tag{212}$$

According to (212), the combined effects of higher labor productivity A^N and the appreciation of the relative price of non tradables pushes up the non traded wage in the long-run. Inserting the long-run change in the equilibrium value of the relative price of non tradables, i.e., $\hat{p} = \frac{(1+\Theta)\left(\hat{a}^T - \hat{a}^N\right)}{(\phi+\Theta)} - \frac{\mathrm{d}\upsilon_{NX}}{(\phi+\Theta)}$ (see eq. (49)), and using the fact that $\chi^N W_R^N = m^N \frac{\alpha_W^N \Psi^N}{s^N + r^\star}$ allows us to rewrite (212) as follows:

$$\hat{w}^N = \frac{\Omega^N}{\left(\phi + \Theta^N\right)} \left[\hat{a}^T \left(1 + \Theta^T\right) + \hat{a}^N \left(\phi - 1\right) - \mathrm{d}\upsilon_{NX}\right]. \tag{213}$$

Imposing the elasticity of substitution ϕ to be equal to one, labor productivity in the non traded sector does no longer impinge on W^N. In this case, the change in the non traded wage is only driven by $\hat{a}^T > 0$ which appreciates the relative price of non traded goods and thereby stimulates labor demand in that sector. Further assuming that labor market parameters are similar across sectors so that $\Theta^j \simeq \Theta$ and $\Omega^j \simeq \Omega$ (with $j = T, N$), we find that the non traded wage is equal to $\Omega \left[\hat{a}^T - \frac{\mathrm{d}\upsilon_{NX}}{(1+\Theta)}\right]$. By producing a long-run improvement in the trade balance NX and thereby stimulating the demand for tradables, a productivity shock exerts a negative impact on the relative wage W^N/W^T. As depicted in Figure 8(b), due to the *labor accumulation effect*, a productivity shock biased toward the traded sector induces smaller shifts in the VCN- and the WSN-schedule. Note that, as for the traded labor market, the shift in the VCN-schedule dominates the shift in the WSN-schedule because the worker bargaining power α_W^N is smaller than one.

I Solving Graphically for the Steady-State: Graphical Apparatus

The steady-state can be described by considering alternatively the goods market or the labor market.

I.1 The Goods Market: Graphical Apparatus

To build intuition about steady-state changes, we investigate graphically the long-run effects of a rise in the the ratio of sectoral productivity. To do so, it is convenient to rewrite the steady-state (199) as follows:

$$\frac{\tilde{C}^T}{\tilde{C}^N} = \frac{\varphi}{1-\varphi} \tilde{P}^\phi, \tag{214a}$$

$$\frac{\tilde{L}^T}{\tilde{L}^N} = \frac{\tilde{m}^T}{\tilde{m}^N} \frac{\left(s^N + \tilde{m}^N\right)}{\left(s^T + \tilde{m}^T\right)} \frac{\left[\bar{\lambda} \tilde{w}_R^T\right]^{\sigma_L^T}}{\left[\bar{\lambda} \tilde{w}_R^N\right]^{\sigma_L^N}}, \tag{214b}$$

$$\frac{\kappa^T}{f^T\left(\tilde{\theta}^T\right)} = \frac{\left(1-\alpha_W^T\right)\tilde{\Psi}^T}{\left(s^T + r^\star\right)}, \tag{214c}$$

$$\frac{\kappa^N}{f^N\left(\tilde{\theta}^N\right)} = \frac{\left(1-\alpha_W^N\right)\tilde{\Psi}^N}{\left(s^N + r^\star\right)}, \tag{214d}$$

$$\frac{\tilde{Y}^T\left(1 + \upsilon_B - \upsilon_V^T - \upsilon_V^N\right)}{\tilde{Y}^N} = \frac{\tilde{C}^T}{\tilde{C}^N}. \tag{214e}$$

We denote by $\upsilon_B \equiv \frac{r^\star \tilde{B}}{\tilde{Y}^T}$ the ratio of interest receipts to traded output, by $\upsilon_V^j \equiv \frac{\kappa^j \tilde{V}^j}{\tilde{Y}^T}$ the share of hiring cost in sector $j = T, N$ in traded output. Remembering that $\tilde{Y}^T = A^T \tilde{L}^T$ and $\tilde{Y}^N = A^N \tilde{L}^N$, the system (214) can be solved for $\tilde{C}^T/\tilde{C}^N$, $\tilde{L}^T/\tilde{L}^N$, $\tilde{\theta}^T$, $\tilde{\theta}^N$, and $\tilde{P}$, as functions of $A^T, A^N, \left(1 + \upsilon_B - \upsilon_V^T - \upsilon_V^N\right)$. Inserting these functions into $\tilde{Y}^N = \tilde{C}^N$ (see eq. (171h)), and $\tilde{B} - B_0 = \Phi^T\left(\tilde{L}^T - L_0^T\right) + \Phi^T\left(\tilde{L}^N - L_0^N\right)$ (see eq. (171j)), the system can be solved for $\tilde{B}$ and $\bar{\lambda}$ as functions of A^T and A^N. Hence, when solving the system (214), we assume that the stock of foreign bonds and the marginal utility of wealth are exogenous which allows us to separate intratemporal reallocation effects from the dynamic (or intertemporal) reallocation effects.

Because we restrict ourselves to the analysis of the long-run effects, the tilde is suppressed for clarity purpose. To characterize the steady-state, we focus on the goods market which can be summarized graphically by two schedules in the $(y^T - y^N, p)$-space, where we denote the logarithm of variables with lower-case letters.

To begin with, we characterize the goods market equilibrium. Inserting (214a) into the market clearing condition (214e) yields:

$$\frac{C^T}{C^N} = \frac{\varphi}{1-\varphi}P^{\phi} = \frac{Y^T\left(1+\upsilon_B-\upsilon_V^T-\upsilon_V^N\right)}{Y^N}. \tag{215}$$

The ratio of traded output to non traded output is:

$$\frac{Y^T}{Y^N} = \frac{1}{\left(1+\upsilon_B-\upsilon_V^T-\upsilon_V^N\right)}\frac{\varphi}{1-\varphi}P^{\phi}.$$

Denoting by $\upsilon_{NX} \equiv NX/Y^T$ the ratio of net exports to traded output, with $NX \equiv -\left(\upsilon_B-\upsilon_V^T-\upsilon_V^N\right)$, the above equation can be rewritten as follows:

$$\frac{Y^T}{Y^N} = \frac{\varphi}{1-\varphi}\frac{1}{(1-\upsilon_{NX})}P^{\phi}. \tag{216}$$

Totally differentiating (216) and denoting the percentage deviation from its initial steady-state by a hat yields the goods market equilibrium-schedule (GME henceforth):

$$\left(\hat{y}^T-\hat{y}^N\right)\Big|^{GME} = \phi\hat{p} - d\ln\left(1-\upsilon_{NX}\right). \tag{217}$$

Eq. (217) corresponds to eq. (40) in the text. According to (217), the GME-schedule is upward-sloping in the (y^T-y^N,p)-space and the slope of the GME-schedule is equal to $1/\phi$.

We now characterize the labor market equilibrium. To do so, we totally differentiate the decision of search-schedule (henceforth DS) given by eq. (214b); we have:

$$\left(\hat{l}^T-\hat{l}^N\right)\Big|^{DS} = \left(\sigma_L^T-\sigma_L^N\right)\hat{\bar{\lambda}} + \left[\alpha_V^T u^T + \sigma_L^T\chi^T\right]\hat{\theta}^T - \left[\alpha_V^N u^N + \sigma_L^N\chi^N\right]\hat{\theta}^N, \tag{218}$$

where we computed the following expressions:

$$\begin{aligned} \mathrm{d}\ln\left(\frac{m^j}{s^j+m^j}\right) &= \alpha_V^j u^j\hat{\theta}^j, \\ \hat{w}_R^j &= \chi^j\hat{\theta}^j. \end{aligned}$$

Totally differentiating the vacancy creation-schedule (henceforth VCj with $j=T,N$) in the traded and non traded sectors, given by eqs. (214c) and (214d), yields:

$$\hat{\theta}^T\Big|^{VCT} = \frac{A^T\hat{a}^T}{\left[\left(1-\alpha_V^T\right)\tilde{\Psi}^T + \chi^T W_R^T\right]}, \tag{219a}$$

$$\hat{\theta}^N\Big|^{VCN} = \frac{PA^N\left(\hat{p}+\hat{a}^N\right)}{\left[\left(1-\alpha_V^N\right)\tilde{\Psi}^N + \chi^N W_R^N\right]}. \tag{219b}$$

Inserting (219) into (218), and using the production functions to eliminate sectoral labor, i.e., $\hat{l}^T = \hat{y}^T - \hat{a}^T$ and $\hat{l}^N = \hat{y}^N - \hat{a}^N$, gives the labor market equilibrium schedule:

$$\begin{aligned} \left(\hat{y}^T-\hat{y}^N\right)\Big|^{GME} &= -\frac{PA^N\left[\alpha_V^N u^N + \sigma_L^N\chi^N\right]}{\left[\left(1-\alpha_V^N\right)\tilde{\Psi}^N + \chi^N W_R^N\right]}\hat{p} + \left(\sigma_L^T-\sigma_L^N\right)\hat{\bar{\lambda}} \\ &+ \left\{1+\frac{A^T\left[\alpha_V^T u^T + \sigma_L^T\chi^T\right]}{\left[\left(1-\alpha_V^T\right)\tilde{\Psi}^T + \chi^T W_R^T\right]}\right\}\hat{a}^T \\ &- \left\{1+\frac{PA^N\left[\alpha_V^N u^N + \sigma_L^N\chi^N\right]}{\left[\left(1-\alpha_V^N\right)\tilde{\Psi}^N + \chi^N W_R^N\right]}\right\}\hat{a}^N. \end{aligned} \tag{220}$$

In the following, we set

$$\Theta^T \equiv \frac{A^T\left[\alpha_V^T u^T + \sigma_L^T\chi^T\right]}{\left[\left(1-\alpha_V^T\right)\Psi^T + \chi^T W_R^T\right]} = \frac{A^T\left(s^T+r^\star\right)\left[\alpha_V^T u^T + \sigma_L^T\chi^T\right]}{\Psi^T\left[\left(1-\alpha_V^T\right)\left(s^T+r^\star\right) + \alpha_W^T m^T\right]} > 0, \tag{221a}$$

$$\Theta^N \equiv \frac{PA^N\left[\alpha_V^N u^N + \sigma_L^N\chi^N\right]}{\left[\left(1-\alpha_V^N\right)\Psi^N + \chi^N W_R^N\right]} = \frac{PA^N\left(s^N+r^\star\right)\left[\alpha_V^N u^N + \sigma_L^N\chi^N\right]}{\Psi^N\left[\left(1-\alpha_V^N\right)\left(s^N+r^\star\right) + \alpha_W^N m^N\right]} > 0, \tag{221b}$$

in order to write formal solutions in a compact form; to get the second equality in eqs. (222) and (221b), we used the fact that $\chi^j W_R^j = \frac{\alpha_W^j \Psi^j}{s^j + r^\star}$ at the steady-state. Assuming an elasticity of labor supply identical across sectors, i.e., $\sigma_L^j = \sigma_L$, so that the wealth effect does not impinge on the ratio of sectoral labor, and making use of (221), eq. (220) can be rewritten as follows:

$$\hat{y}^T - \hat{y}^N \Big|^{LME} = -\Theta^N \hat{p} + \left(1 + \Theta^T\right) \hat{a}^T - \left(1 + \Theta^N\right) \hat{a}^N. \tag{222}$$

Eq. (222) corresponds to eq. (41) in the text. According to (222), the LME-schedule is downward-sloping in the $(y^T - y^N, p)$-space and the slope of the LME-schedule is equal to $-\frac{1}{\Theta^N} < 0$. Moreover, assuming that the labor market parameters are similar across sectors, a productivity shock biased toward the traded sector unambiguously shifts to the right the LME-schedule.

I.2 The Labor Market: Graphical Apparatus

When focusing on the labor market, the model can be summarized graphically by two schedules in the $(l^T - l^N, \ln\left(\frac{\theta^T}{\theta^N}\right))$-space.

As will be useful later, we first solve for the relative price of non tradables by using the goods market clearing condition (216). Using production functions, i.e., $Y^j = A^j L^j$, solving (216) for the relative price yields:

$$P = \left[\left(\frac{1-\varphi}{1-\varphi}\right)(1 - \upsilon_{NX})\left(\frac{A^T}{A^N}\right)\left(\frac{L^T}{L^N}\right)\right]^{\frac{1}{\phi}}. \tag{223}$$

Applying the implicit function theorem, we have:

$$P = P\left[\left(\frac{L^T}{L^N}\right), (1 - \upsilon_{NX}), \left(\frac{A^T}{A^N}\right)\right], \tag{224}$$

where

$$\hat{p} = \frac{1}{\phi}\left[d\ln\left(\frac{L^T}{L^N}\right) + d\ln\left(\frac{A^T}{A^N}\right) + d\ln\left(1 - \upsilon_{NX}\right)\right]. \tag{225}$$

The Decision of Search Schedule in the $(l^T - l^N, \ln\left(\frac{\theta^T}{\theta^N}\right))$-space

Imposing $\sigma_L^j = \sigma_L$ into eq. (214b), the decision of search-schedule (DS henceforth) reduces to:

$$\frac{L^T}{L^N} = \frac{m^T}{m^N}\frac{m^N + s^N}{m^T + s^T}\left(\frac{W_R^T}{W_R^N}\right)^{\sigma_L}, \tag{226}$$

where $W_R^j \equiv \frac{\alpha_W^j}{1-\alpha_W^j}\kappa^j\tilde{\theta}^j + R^j$ is the reservation wage. **Eq. (226) corresponds to eq. (43) in the text**.

Taking logarithm and differentiating eq. (226) yields:

$$\hat{l}^T - \hat{l}^N = \left[\alpha_V u^T + \sigma_L \chi^T\right]\hat{\theta}^T - \left[\alpha_V u^N + \sigma_L \chi^N\right]\hat{\theta}^N, \tag{227}$$

where we used the fact that $d\ln\left(\frac{m^j}{m^j+s^j}\right) = \alpha_V u^j \hat{\theta}^j$ and $\hat{w}_R^j = \chi^j \hat{\theta}^j$ with $\chi^j = \frac{\frac{\alpha_W}{1-\alpha_W}\kappa^j\theta^j}{W_R^j}$.

Assuming that the labor markets display initially similar features across sectors, i.e., $u^j \simeq u$, $\chi^j \simeq \chi$, eq. (227) reduces to:

$$\left(\hat{\theta}^T - \hat{\theta}^N\right)\Big|^{DS} = \frac{1}{\left[\alpha_V u + \sigma_L \chi\right]}\left(\hat{l}^T - \hat{l}^N\right), \tag{228}$$

Eq. (228) corresponds to eq. (44) in the text. Inspection of (228) reveals that the DS-schedule:

- is upward-sloping in the $(l^T - l^N, \ln\left(\frac{\theta^T}{\theta^N}\right))$-space;
- is steeper as the workers are more reluctant to shift hours worked across sectors (i.e., the elasticity of labor supply σ_L is smaller), the unemployment benefit scheme is more generous or the worker bargaining power α_W is lower (because higher unemployment benefits R or a lower worker bargaining power both reduce the share of the surplus associated with a labor contract in the marginal benefit of search χ).

The Vacancy-Creation Schedule in the $(l^T - l^N, \omega)$-space

Dividing eq. (199b) by eq. (199c) and imposing $\alpha_W^j = \alpha_W$ leads to:

$$\frac{\kappa^T}{\kappa^N}\frac{f^N}{f^T} = \frac{\Psi^T}{\Psi^N}\frac{s^N + r^\star}{s^T + r^\star}.$$

Using (22), i.e., $f^j = X^j \left(\theta^j\right)^{\alpha_V - 1}$, while assuming $\alpha_V^j = \alpha_V$, and the definition of the overall surplus, i.e., $\Psi^j \equiv \Xi^j + r^\star x^j - W_R^j$, the above equation can be rewritten as follows:

$$\frac{\kappa^T}{\kappa^N} \frac{\left(s^T + r^\star\right)}{\left(s^N + r^\star\right)} \frac{X^T}{X^N} \left(\frac{\theta^T}{\theta^N}\right)^{1-\alpha_V} = \frac{A^T + r^\star x^T - W_R^T}{P\left(.\right) A^N + r^\star x^N - W_R^N}, \tag{229}$$

where the relative price equation is given by eq. (224). **Eq. (229) corresponds to eq. (46) in the text**. The change in overall surplus Ψ^j in percentage is given by:

$$\hat{\Psi}^j = \frac{\Xi^j \hat{\Xi}^j - \chi^j W_R^j \hat{\theta}^j}{\Psi^j}. \tag{230}$$

Taking logarithm and differentiating eq. (229), inserting changes in the relative price (225) and in the overall surplus (230) leads to:

$$\begin{aligned}
\left(1 - \alpha_V\right) \left(\hat{\theta}^T - \hat{\theta}^N\right) &= \hat{\Psi}^T - \hat{\Psi}^N, \\
&= \frac{A^T \hat{a}^T - \chi^T W_R^T \hat{\theta}^T}{\Psi^T} - \frac{\left(PA^N\right)\left(\hat{p} + \hat{a}^N\right) - \chi^{TN} W_R^N \hat{\theta}^N}{\Psi^N}, \\
&= \frac{A^T \hat{a}^T - \chi^T W_R^T \hat{\theta}^T}{\Psi^T} - \frac{PA^N \hat{a}^N - \chi^N W_R^N \hat{\theta}^N}{\Psi^N} \\
&- \frac{PA^N}{\Psi^N \phi} \left[\left(\hat{l}^T - \hat{l}^N\right) + \left(\hat{a}^T - \hat{a}^N\right) + d\ln\left(1 - \upsilon_{NX}\right)\right].
\end{aligned} \tag{231}$$

Collecting terms, assuming that initially $\Xi^j \simeq \Xi$, $\Psi^j \simeq \Psi$, $W_R^j \simeq W_R$, $\chi^j \simeq \chi$, eq. (231) can be rewritten as follows:

$$\begin{aligned}
\left.\left(\hat{\theta}^T - \hat{\theta}^N\right)\right|^{VC} &= -\frac{\Xi}{\phi\left[\left(1-\alpha_V\right)\Psi + \chi W_R\right]} \left(\hat{l}^T - \hat{l}^N\right) \\
&+ \frac{\Xi\left[\left(\phi - 1\right)\left(\hat{a}^T - \hat{a}^N\right) - d\ln\left(1 - \upsilon_{NX}\right)\right]}{\phi\left[\left(1-\alpha_V\right)\Psi + \chi W_R\right]}.
\end{aligned} \tag{232}$$

Eq. (232) corresponds to eq. (47) in the text. Inspection of (232) reveals that the VC-schedule:

- is downward-sloping in the $(l^T - l^N, \ln\left(\frac{\theta^T}{\theta^N}\right))$-space with a slope equal to $-\frac{\Xi}{\phi\left[\left(1-\alpha_V\right)\Psi + \chi W_R\right]}$;
- is steeper as the elasticity of substitution between traded and non traded goods ϕ is smaller or the worker bargaining power is lower (because it reduces χW_R);
- shifts to the right following higher productivity of tradables relative to non tradables (i.e., $\left(\hat{a}^T - \hat{a}^N\right) > 0$) as long as $\phi > 1$ or when the country experiences a higher steady-state trade balance surplus, i.e., if $-d\ln\left(1 - \upsilon_{NX}\right) \simeq d\upsilon_{NX} > 0$;

J Long-Run Relative Price and Relative Wage Effects of Technological Change Biased Toward the Traded Sector

Equating demand for tradables in terms of non tradables given by eq. (217) and supply (222) yields

$$\begin{aligned}
\left(\hat{y}^T - \hat{y}^N\right) &= \phi\hat{p} - d\ln\left(1 - \upsilon_{NX}\right), \\
&= -\Theta^N \hat{p} + \left(1 + \Theta^T\right)\hat{a}^T - \left(1 + \Theta^N\right)\hat{a}^N.
\end{aligned}$$

Collecting terms leads to the deviation in percentage of the relative price from its initial steady-state:

$$\hat{p} = \frac{\left(1 + \Theta^T\right)\hat{a}^T - \left(1 + \Theta^N\right)\hat{a}^N}{\left(\phi + \Theta^N\right)} + \frac{\mathrm{d}\ln\left(1 - \upsilon_{NX}\right)}{\left(\phi + \Theta^N\right)}. \tag{233}$$

Eq. (233) corresponds to eq. (48) in the text.

To determine the long-run adjustment in the relative wage, $\Omega \equiv W^N/W^T$, we first derive the deviation in percentage of the sectoral wage. To do so, we totally differentiate (199b)-(199c) the vacancy creation equation

$$\begin{aligned}
\left(1 - \alpha_V\right)\hat{\theta}^j &= \hat{\Psi}^j, \\
&= \frac{\Xi^j \hat{\Xi}^j - \chi^j W_R^j \hat{\theta}^j}{\Psi^j},
\end{aligned} \tag{234}$$

where we use (230). Collecting terms leads to the deviation in percentage of the labor market tightness in sector $j = T, N$:

$$\hat{\theta}^j = \frac{\Xi^j}{\left[(1-\alpha_V)\Psi^j + \chi^j W_R^j\right]}\hat{\Xi}^j. \tag{235}$$

We repeat the Nash bargaining wage given by eq. (24) for convenience by imposing $\alpha_W^j = \alpha_W$:

$$W^j = \alpha_W\left(\Xi^j + r^\star x^j\right) + (1-\alpha_W) W_R^j. \tag{236}$$

Totally differentiating (236) and plugging the change in the labor market tightness leads to:

$$\begin{aligned}\hat{W}^j &= \frac{\alpha_W \Xi^j}{W^j}\hat{\Xi}^j + \frac{(1-\alpha_W)\chi^j W_R^j}{W^j}\hat{\theta}^j,\\ &= \frac{\Xi^j}{W^j}\frac{\left[\alpha_W(1-\alpha_V)\Psi^j + \chi^j W_R^j\right]}{\left[(1-\alpha_V)\Psi^j + \chi^j W_R^j\right]}.\end{aligned} \tag{237}$$

Using the fact that at the steady-state, we have $\chi^j W_R^j = m^j \xi^j = \frac{m^j \alpha_W \Psi^j}{s^j + r^\star}$, eq. (237) can be rewritten as follows:

$$\begin{aligned}\hat{W}^j &= \frac{\Xi^j}{W^j}\frac{\left[\alpha_W(1-\alpha_V)\Psi^j + \frac{m^j\alpha_W\Psi^j}{s^j+r^\star}\right]}{\left[(1-\alpha_V)\Psi^j + \frac{m^j\alpha_W\Psi^j}{s^j+r^\star}\right]},\\ &= \frac{\Xi^j}{W^j}\frac{\alpha_W\left[(1-\alpha_V)\left(s^j+r^\star\right)+m^j\right]}{\left[(1-\alpha_V)\left(s^j+r^\star\right)+\alpha_W m^j\right]}\hat{\Xi}^j.\end{aligned} \tag{238}$$

Eq. (238) corresponds to eq. (50) in the text. In order to write formal solutions in a compact form, we set:

$$\Omega^j \equiv \frac{\Xi^j}{W^j}\frac{\alpha_W\left[(1-\alpha_V)\left(s^j+r^\star\right)+m^j\right]}{\left[(1-\alpha_V)\left(s^j+r^\star\right)+\alpha_W m^j\right]}. \tag{239}$$

Using the fact that $\hat{\Xi}^N = \hat{p} + \hat{a}^N$ and $\hat{\Xi}^T = \hat{a}^T$, subtracting $\hat{w}^T$ from $\hat{w}^N$ by combining (238) and (239) and inserting (233) leads to the deviation in percentage of the relative wage:

$$\begin{aligned}\hat{\omega} &= \hat{w}^N - \hat{w}^T,\\ &= \Omega^N\left(\hat{p}+\hat{a}^N\right) - \Omega^T\hat{a}^T,\\ &= \left\{\Omega^N\left[\frac{\left(1+\Theta^T\right)\hat{a}^T + (\phi-1)\hat{a}^N}{\left(\phi+\Theta^N\right)}\right] - \Omega^T\hat{a}^T\right\} - \Omega^N\frac{\mathrm{d}\upsilon_{NX}}{\phi+\Theta^N}.\end{aligned} \tag{240}$$

Eq. (240) corresponds to eq. (51) in the text.

K The Role of Endogenous Sectoral Labor Force Participation Decision

In this section, we look at a special case of the model for which the sectoral labor force is inelastic, i.e. $\sigma_L = 0$, in order to highlight the role of an endogenous sectoral labor force participation decision in driving the long-run effects of technological change biased toward the traded sector. Then, we analyze the implications of $\sigma_L \to \infty$.

K.1 Equilibrium Dynamics when $\sigma_L = 0$

To begin with, we determine the dynamic system. Denoting by W_R^j the reservation wage in sector j, the first-order conditions for the traded and the non traded sector described by eqs. (92b)-(92c) respectively, implies that $F^j \equiv L^j + U^j = \left(\bar{\lambda} W_R^j\right)^{\sigma_L}$ with $W_R^j \equiv R^j + m^j\left(\theta^j\right)\xi^j$. Using the fact that $U^j = \left(\bar{\lambda} W_R^j\right)^{\sigma_L} - L^j$, the dynamic equation for employment (11) can be rewritten as follows:

$$\dot{L}^j = m^j\left(\theta^j\right)\left(\bar{\lambda} W_R^j\right)^{\sigma_L} - \left[s^j + m^j\left(\theta^j\right)\right]L^j.$$

Assuming that labor force is fixed, i.e., setting $\sigma_L = 0$, then the equation above reads as:

$$\dot{L}^j = m^j\left(\theta^j\right) - \left[s^j + m^j\left(\theta^j\right)\right]L^j. \tag{241}$$

Imposing $\alpha^j_W = \alpha_W$ and using the fact that $m^j\left(\theta^j\right)\xi^j = \frac{\alpha_W}{1-\alpha_W}\kappa^j\theta^j$ together with $-\frac{v^j_F}{\lambda} = W^j_R$ and $W^j_R \equiv R^j + m^j\left(\theta^j\right)\xi^j$, the Nash bargaining wage can be rewritten as follows:

$$\begin{aligned} W^j &= \alpha_W\left(\Xi^j + r^\star x^j\right) - \left(1-\alpha_W\right)\frac{v^j_F}{\bar{\lambda}}, \\ &= \alpha_W\left(\Xi^j + r^\star x^j + \kappa^j\theta^j\right) + \left(1-\alpha_W\right)R^j. \end{aligned} \tag{242}$$

We now determine the dynamic equation for the labor market tightness. Plugging (242) into (121) yields:

$$\begin{aligned} \dot{\theta}^j(t) &= \frac{\theta^j(t)}{\left(1-\alpha^j_V\right)}\left\{\left(s^j + r^\star\right) - \frac{f^j\left(\theta^j(t)\right)}{\kappa^j}\left[\left(\Xi^j + r^\star x^j\right) - W^j\right]\right\}, \\ &= \frac{\theta^j(t)}{\left(1-\alpha^j_V\right)}\left\{\left(s^j + r^\star\right) - \frac{f^j\left(\theta^j(t)\right)\left(1-\alpha_W\right)}{\kappa^j}\Psi^j\right\}, \end{aligned} \tag{243}$$

where the overall surplus from an additional job Ψ^j is:

$$\Psi^j \equiv \Xi^j + r^\star x^j - \frac{\alpha_W}{1-\alpha_W}\kappa^j\theta^j - R^j, \tag{244}$$

with $\Xi^T = A^T$ and $\Xi^N = PA^N$.

Traded Sector

Linearizing the accumulation equation for labor (241) and the dynamic equation for labor market tightness (243) in the traded sector, we get in matrix form:

$$\left(\dot{L}^T, \dot{\theta}^T\right)^T = J^T\left(L^T(t) - \tilde{L}^T, \theta^T(t) - \tilde{\theta}^T\right)^T \tag{245}$$

where J^T is given by

$$J^T \equiv \begin{pmatrix} -\left(s^T + \tilde{m}^T\right) & \left(\tilde{m}^T\right)'\left(1-\tilde{L}^T\right) \\ 0 & \left[\left(s^T + r^\star\right) + \tilde{m}^T\frac{\alpha_W}{1-\alpha_V}\right] \end{pmatrix}, \tag{246}$$

with $\tilde{m}^T = m^T\left(\tilde{\theta}\right)$.

The trace denoted by Tr of the linearized 2×2 matrix (245) is given by:

$$\text{Tr}J^T = r^\star + \frac{\tilde{m}^T}{1-\alpha_V}\left[\alpha_W - \left(1-\alpha_V\right)\right]. \tag{247}$$

The determinant denoted by Det of the linearized 2×2 matrix (125) is unambiguously negative:

$$\text{Det}J^T = -\left(s^T + \tilde{m}^T\right)\left[\left(s^T + r^\star\right) + \frac{\alpha_W}{1-\alpha_V}\tilde{m}^T\right] < 0. \tag{248}$$

From now on, for clarity purpose, we impose the Hosios condition in order to avoid unnecessary complications:

$$\alpha_W = \left(1-\alpha_V\right). \tag{249}$$

Denoting by ν^T the eigenvalue, the characteristic equation for the matrix J (246) of the linearized system writes as follows:

$$\left(\nu^T_i\right)^2 - r^\star\nu^T_i + \text{Det}J^T = 0. \tag{250}$$

The characteristic roots obtained from the characteristic polynomial of degree two can be written as follows:

$$\begin{aligned} \nu^T_i &\equiv \frac{1}{2}\left\{r^\star \pm \sqrt{\left(r^\star\right)^2 - 4\text{Det}J^T}\right\} \gtrless 0, \quad i = 1, 2, \\ &\equiv \frac{1}{2}\left\{r^\star \pm \sqrt{\left(r^\star\right)^2 + 4\left(s^T + \tilde{m}^T\right)^2 + 4r^\star\left(s^T + \tilde{m}^T\right)}\right\}, \\ &\equiv \frac{1}{2}\left\{r^\star \pm \left[r^\star + 2\left(s^T + \tilde{m}^T\right)\right]\right\}, \end{aligned} \tag{251}$$

where we used the fact that $\text{Det}J^T = -\left(s^T + \tilde{m}^T\right)\left(s^T + r^\star + \tilde{m}^T\right)$.

We denote by $\nu^T_1 < 0$ and $\nu^T_2 > 0$ the stable and unstable eigenvalues respectively which satisfy:

$$\nu^T_1 = -\left(s^T + \tilde{m}^T\right) < 0 < r^\star < \nu^T_2 = \left(s^T + r^\star + \tilde{m}^T\right). \tag{252}$$

Non Traded Sector

Linearizing the accumulation equation for non traded labor (241) by setting $j = N$ and the dynamic equation for labor market tightness (243) in the non traded sector by inserting first the solution for the relative price of non tradables (115), i.e., $P = P\left(L^N, \bar{\lambda}, A^N\right)$, we get in matrix form:

$$\left(\dot{L}^N, \dot{\theta}^N\right)^T = J^N \left(L^N(t) - \tilde{L}^N, \theta^N(t) - \tilde{\theta}^N\right)^T \tag{253}$$

where J^N is given by

$$J^N \equiv \begin{pmatrix} -\left(s^N + \tilde{m}^N\right) & \left(m^N\right)' \left(1 - \tilde{L}^N\right) \\ -\frac{1-\alpha_W}{1-\alpha_V} \frac{\tilde{m}^N}{\kappa^N} P_{L^N} A^N & \left[\left(s^N + r^\star\right) + \tilde{m}^N \frac{\alpha_W}{1-\alpha_V}\right] \end{pmatrix}, \tag{254}$$

$P_{L^N} = \frac{\partial P}{\partial L^N} = \frac{A^N}{C_P^N} < 0$.

The trace is:

$$\text{Tr}J^N = r^\star + \frac{\tilde{m}^N}{1-\alpha_V} \left[\alpha_W - (1 - \alpha_V)\right]. \tag{255}$$

The determinant denoted by Det of the linearized 2×2 matrix (254) is unambiguously negative:

$$\text{Det}J^N = -\left(s^N + \tilde{m}^N\right) \left[\left(s^N + r^\star\right) + \frac{\alpha_W}{1-\alpha_V} \tilde{m}^N\right] + \frac{1-\alpha_W}{1-\alpha_V} \frac{\tilde{m}^N}{\kappa^N} P_{L^N} A^N \left(m^N\right)' \left(1 - \tilde{L}^N\right) < 0. \tag{256}$$

Assuming that the Hosios condition (249) holds, the determinant (256) can be rewritten as follows:

$$\begin{aligned} \text{Det}J^N &= -\left(s^N + \tilde{m}^N\right)\left(s^N + r^\star\right) \left[\left(\frac{s^N + r^\star \tilde{m}^N}{s^N + r^\star}\right) - \frac{1-\alpha_W}{1-\alpha_V} \frac{\tilde{m}^N}{\kappa^N} \frac{P_{L^N} A^N m^{N,\prime}}{\left(s^N + r^\star\right)} \frac{\left(1 - \tilde{L}^N\right)}{\left(s^N + \tilde{m}^N\right)}\right], \\ &= -\left(s^N + \tilde{m}^N\right)\left(s^N + r^\star\right) \left[\left(\frac{s^N + r^\star \tilde{m}^N}{s^N + r^\star}\right) - \tilde{P} A^N \frac{P_{L^N} L^N}{\tilde{P}} \frac{\alpha_V \tilde{u}^N}{\left(1-\alpha_V\right) \tilde{\Psi}^N}\right] < 0, \end{aligned} \tag{257}$$

where we computed the following term:

$$\begin{aligned} & \frac{1-\alpha_W}{1-\alpha_V} \frac{\tilde{m}^N}{\kappa^N} \frac{P_{L^N} A^N m^{N,\prime}}{\left(s^N + r^\star\right)} \frac{\left(1 - \tilde{L}^N\right)}{\left(s^N + \tilde{m}^N\right)} \\ =& \frac{\left(1-\alpha_W\right)}{\left(s^N + r^\star\right)} \frac{\tilde{m}^N}{\tilde{\theta}^N \kappa^N} \frac{m^{N,\prime} \tilde{\theta}^N}{\tilde{m}^N} \frac{\tilde{m}^N \tilde{U}^N}{\left(1-\alpha_V\right)} \frac{P_{L^N} A^N}{\left(s^N + \tilde{m}^N\right)}, \\ =& \frac{\alpha_V}{\tilde{\Psi}^N} \frac{s^N \tilde{L}^N}{\left(1-\alpha_V\right)} \frac{P_{L^N} A^N}{\left(s^N + \tilde{m}^N\right)}, \\ =& \left(\frac{\alpha_V}{1-\alpha_V}\right) \frac{\tilde{u}^N}{\tilde{\Psi}^N} \frac{P_{L^N} L^N}{\tilde{P}} \tilde{P} A^N. \end{aligned} \tag{258}$$

To get (258), we used the fact that $\frac{(1-\alpha_W)\tilde{f}^N}{\kappa^N (s^N + r^\star)} = \frac{1}{\tilde{\Psi}^N}$, $1 - \tilde{L}^N = \tilde{U}^N$, $\tilde{m}^N \tilde{U}^N = s^N \tilde{L}^N$, and $\tilde{u}^N = \frac{s^N}{s^N + \tilde{m}^N}$.

We denote by $\nu_1^N < 0$ and $\nu_2^N > 0$ the stable and unstable eigenvalues respectively which satisfy:

$$\nu_1^N < 0 < r^\star < \nu_2^N. \tag{259}$$

K.2 Formal Solutions for $L^T(t)$ and $\theta^T(t)$

The stable paths for the labor market in the traded sector are given by :

$$L^T(t) - \tilde{L}^T = D_1^T e^{\nu_1^T t} \tag{260a}$$

$$\theta^T(t) - \tilde{\theta}^T = \omega_{21}^T D_1^T e^{\nu_1^T t}, \tag{260b}$$

where $D_1^T = L_0^T - \tilde{L}^T$, and element ω_{21}^T of the eigenvector (associated with the stable eigenvalue ν_1^T) is given by:

$$\omega_{21}^T = \frac{\left(s^T + \tilde{m}^T + \nu_1^T\right)}{m^{\prime,T} \left(1 - \tilde{L}^T\right)} = 0. \tag{261}$$

where we used the fact that $\nu_1^T = -\left(s^T + \tilde{m}^T\right)$ (see eq. (252)). From (260a), the dynamics for labor market tightness θ^T degenerate.

K.3 Formal Solutions for $L^N(t)$ and $\theta^N(t)$

The stable paths for the labor market in the non traded sector are given by :

$$
\begin{aligned}
L^N(t) - \tilde{L}^N &= D_1^N e^{\nu_1^N t} && (262a)\\
\theta^N(t) - \tilde{\theta}^N &= \omega_{21}^N D_1^T e^{\nu_1^N t}, && (262b)
\end{aligned}
$$

where $D_1^N = L_0^N - \tilde{L}^N$, and element ω_{21}^N of the eigenvector (associated with the stable eigenvalue ν_1^N) is given by:

$$
\begin{aligned}
\omega_{21}^N &= \frac{\left(s^N + \tilde{m}^N + \nu_1^N\right)}{m^{\prime,N}\left(1 - \tilde{L}^N\right)},\\
&= \frac{\frac{1-\alpha_W}{1-\alpha_V}\frac{\tilde{m}^N}{\kappa^N} P_{L^N} A^N}{\left(s^N + r^\star + \tilde{m}^N - \nu_1^N\right)} < 0. && (263)
\end{aligned}
$$

K.4 Formal Solution for the Stock of Foreign Bonds $B(t)$

Substituting first the short-run static solutions for consumption in tradables given by (117), and using the fact that $V^j = U^j \theta^j$, the accumulation equation for traded bonds (119) can be written as follows:

$$
\dot{B}(t) = r^\star B(t) + A^T L^T(t) - C^T\left(L^N(t), \bar{\lambda}, A^N\right) - \kappa^T \theta^T(t)\left(1 - L^T(t)\right) - \kappa^N \theta^N(t)\left(1 - L^N(t)\right), \quad (264)
$$

where we used the fact that $U^j = 1 - L^j$ when $\sigma_L = 0$.

Linearizing (264) in the neighborhood of the steady-state and inserting stable solutions given by (260) and (262) yields:

$$
\dot{B}(t) = r^\star\left(B(t) - \tilde{B}\right) + \Lambda^T\left(L^T(t) - \tilde{L}^T\right) + \Lambda^N\left(L^N(t) - \tilde{L}^N\right), \quad (265)
$$

where we set:

$$
\begin{aligned}
\Lambda^T &= A^T + \kappa^T \tilde{\theta}^T > 0, && (266a)\\
\Lambda^N &= -C^T_{L^N} - \kappa^N \tilde{U}^N \omega_{21}^N - \kappa^N \tilde{\theta}^N \omega_{31}^N,\\
&= -C^T_{L^N} + \kappa^N \tilde{\theta}^N\left[1 - \frac{\left(s^N + \tilde{m}^N + \nu_1^N\right)}{\alpha_V \tilde{m}^N}\right] > 0, && (266b)
\end{aligned}
$$

where we have inserted (151b) and used the fact that $\left(m^N\right)' \theta^N / m^N = \alpha_V$ to get (266b); note that $C^T_{L^N} \simeq 0$ as long as $\phi \simeq \sigma_C$ in line with evidence for a typical OECD economy. The sign of (266b) follows from the fact that $\omega_{21}^N < 0$ (see (263)).

Solving the differential equation (265) yields:

$$
B(t) = \tilde{B} + \left[\left(B_0 - \tilde{B}\right) - \frac{\Lambda^T D_1^T}{\nu_1^T - r^\star} - \frac{\Lambda^N D_1^N}{\nu_1^N - r^\star}\right] e^{r^\star t} + \frac{\Lambda^T D_1^T}{\nu_1^T - r^\star} e^{\nu_1^T t} + \frac{\Lambda^N D_1^N}{\nu_1^N - r^\star} e^{\nu_1^N t}. \quad (267)
$$

Invoking the transversality condition for intertemporal solvency, and using the fact that $D_1^T = L_0^T - \tilde{L}^T$ and $D_1^N = L_0^N - \tilde{L}^N$, we obtain the linearized version of the nation's intertemporal budget constraint:

$$
\tilde{B} - B_0 = \Phi^T\left(\tilde{L}^T - L_0^T\right) + \Phi^T\left(\tilde{L}^N - L_0^N\right), \quad (268)
$$

where we set

$$
\Phi^T \equiv \frac{\Lambda^T}{\nu_1^T - r^\star} = -\frac{\left(A^T + \kappa^T \tilde{\theta}^T\right)}{\left(s^T + \tilde{m}^T + r^\star\right)} < 0, \quad \Phi^N \equiv \frac{\Lambda^N}{\nu_1^N - r^\star} < 0. \quad (269)
$$

Equation (269) can be solved for the stock of foreign bonds:

$$
\tilde{B} = B\left(\tilde{L}^T, \tilde{L}^N\right), \quad B_{L^T} = \Phi^T < 0, \quad B_{L^N} = \Phi^N < 0. \quad (270)
$$

For the national intertemporal solvency to hold, the terms in brackets of equation (267) must be zero so that the stable solution for net foreign assets finally reduces to:

$$
B(t) - \tilde{B} = \Phi^T\left(L^T(t) - \tilde{L}^T\right) + \Phi^N\left(L^N(t) - \tilde{L}^N\right). \quad (271)
$$

K.5 Solving Graphically for the Steady-State

We investigate graphically the long-run effects of a rise in the the ratio of sectoral productivity. Assuming $\alpha_W^j = \alpha_W$ and setting $\sigma_L = 0$, the steady-state (214) reduces to a the following system which comprises five equations:

$$\frac{\tilde{C}^T}{\tilde{C}^N} = \frac{\varphi}{1-\varphi}\tilde{P}^{\phi}, \tag{272a}$$

$$\frac{\tilde{L}^T}{\tilde{L}^N} = \frac{\tilde{m}^T}{\tilde{m}^N}\frac{\left(s^N + \tilde{m}^N\right)}{\left(s^T + \tilde{m}^T\right)}, \tag{272b}$$

$$\frac{\kappa^T}{f^T\left(\tilde{\theta}^T\right)} = \frac{\left(1-\alpha_W^T\right)\tilde{\Psi}^T}{\left(s^T + r^\star\right)}, \tag{272c}$$

$$\frac{\kappa^N}{f^N\left(\tilde{\theta}^N\right)} = \frac{\left(1-\alpha_W^N\right)\tilde{\Psi}^N}{\left(s^N + r^\star\right)}, \tag{272d}$$

$$\frac{\tilde{Y}^T\left(1-\upsilon_{NX}\right)}{\tilde{Y}^N} = \frac{\tilde{C}^T}{\tilde{C}^N}, \tag{272e}$$

where $-\upsilon_{NX} = \upsilon_B - \upsilon_V^T - \upsilon_V^N$.

Goods Market

Because we restrict ourselves to the analysis of the long-run effects, the tilde is suppressed for the purposes of clarity. To characterize the steady-state, we focus on the goods market which can be summarized graphically by two schedules in the $(y^T - y^N, p)$-space, where we denote the logarithm of variables with lower-case letters.

The goods market equilibrium (GME)-schedule that we repeat for convenience is identical to (217):

$$\left(\hat{y}^T - \hat{y}^N\right)\Big|^{GME} = \phi\hat{p} - d\ln\left(1-\upsilon_{NX}\right). \tag{273}$$

The GME-schedule is upward-sloping in the $(y^T - y^N, p)$-space and the slope of the GME-schedule is equal to $1/\phi$.

The labor market equilibrium (LME)-schedule that we repeat for convenience is identical to (222),

$$\hat{y}^T - \hat{y}^N\Big|^{LME} = -\Theta^N\hat{p} + \left(1+\Theta^T\right)\hat{a}^T - \left(1+\Theta^N\right)\hat{a}^N. \tag{274}$$

except for the elasticity Θ^j of employment to the marginal revenue of labor which reduces to:

$$\Theta^T \equiv \frac{A^T\alpha_V^T u^T}{\left[\left(1-\alpha_V\right)\Psi^T + \tilde{\chi}^T W_R^T\right]} > 0, \tag{275a}$$

$$\Theta^N \equiv \frac{PA^N\alpha_V^N u^N}{\left[\left(1-\alpha_V\right)\Psi^N + \chi^N W_R^N\right]} > 0, \tag{275b}$$

The LME-schedule is downward-sloping in the $(y^T - y^N, p)$-space and the slope of the LME-schedule is equal to $-\frac{1}{\Theta^N}$. When $\sigma_L = 0$, Θ^j is smaller so that the LME-schedule is steeper.

Labor Market

Imposing $\sigma_L = 0$ into eq. (214b), the decision of search (DS)-schedule reduces to:

$$\frac{L^T}{L^N} = \frac{m^T}{m^N}\frac{m^N + s^N}{m^T + s^T}. \tag{276}$$

Taking logarithm and differentiating eq. (276) yields:

$$\hat{l}^T - \hat{l}^N = \alpha_V u^T\hat{\theta}^T - \alpha_V u^N\hat{\theta}^N. \tag{277}$$

Assuming that the labor markets display similar features across sectors, i.e., $u^j \simeq u$, eq. (277) reduces to:

$$\left(\hat{\theta}^T - \hat{\theta}^N\right)\Big|^{DS}_{\sigma_L=0} = \frac{1}{\alpha_V u}\left(\hat{l}^T - \hat{l}^N\right). \tag{278}$$

The DS-schedule is upward-sloping in the $(l^T - l^N, \ln\left(\frac{\theta^T}{\theta^N}\right))$-space. Comparing (278) with (228), it is straightforward to show that the DS-schedule becomes steeper when $\sigma_L = 0$. The VC-schedule is downward-sloping and identical to (232).

K.6 Relative Wage and Relative Price Effects of Technological Change Biased Toward the Traded Sector when $\sigma_L = 0$

Equating demand for tradables in terms of non tradables given by eq. (273) and supply (274) yields the deviation in percentage of the relative price from its initial steady-state (233). When assuming $\Theta^{j,\prime} \simeq \Theta'$, eq. (233) reduces to:

$$\hat{p} = \frac{(1+\Theta')\left(\hat{a}^T - \hat{a}^N\right)}{(\phi + \Theta')} + \frac{\mathrm{d}\ln(1-\upsilon_{NX})}{(\phi+\Theta')}, \tag{279}$$

where

$$\Theta' \equiv \frac{\Xi \alpha_V u}{\left[(1-\alpha_V)\Psi + \tilde{\chi} W_R\right]} < \Theta \equiv \frac{\Xi\left[\alpha_V u + \sigma_L \chi\right]}{\left[(1-\alpha_V)\Psi + \tilde{\chi} W_R\right]}, \tag{280}$$

with Θ given by (221). Assuming $\sigma_L = 0$ lowers the elasticity Θ of sectoral employment w.r.t. marginal revenue of labor. Intuitively, technological change induces firms to post more job vacancies which raises the labor market tightness and thus the probability of finding a job. When $\sigma_L > 0$, higher θ^j increases L^j through two channels: i) by triggering an outflow from unemployment, and ii) by inducing agents to increase the search intensity for a job. Because the latter effect vanishes if $\sigma_L = 0$, employment becomes less responsive to technological change, as captured by a lower Θ, i.e., $\Theta' < \Theta$ (see inequality (280)). Since $\Theta' < \Theta$, comparing eq. (279) with eq. (49) shows that when setting $\sigma_L = 0$, the labor market frictions effect captured by the first term on the RHS of eq. (279) is moderated or amplified depending on whether ϕ is larger or smaller than one. In the former case, traded output increases less so that the relative price of non tradables must appreciate by a smaller amount to clear the goods market. If $\phi < 1$, technological change biased toward the traded sector raises the share of non tradables and thus has an expansionary effect on labor demand in the non traded sector. When $\sigma_L = 0$, as detailed below, firms must increase wages by a larger amount. To compensate for the higher unit labor cost, non traded firms set higher prices so that p increases more. Whether ϕ is larger or smaller than one, technological change biased toward the traded sector exerts a larger negative impact on p when $\sigma_L = 0$ through the labor accumulation effect. The reason is that following higher net exports, because the reallocation of labor across sectors is absent, traded output increases less which in turn triggers a greater excess of demand for tradables, thus leading to a larger depreciation in the relative price of non tradables (i.e., a larger decline in p).

Equating labor supply (278) with labor demand (232) while assuming $\Theta^j \simeq \Theta$ and $\Omega^j \simeq \Omega$ leads to the deviation in percentage of the relative wage from its initial steady-state:

$$\hat{\omega} = -\frac{\Omega}{\phi + \Theta'}\left[(\phi - 1)\left(\hat{a}^T - \hat{a}^N\right) + \mathrm{d}\upsilon_{NX}\right]. \tag{281}$$

Eq. (281) shows that assuming a fixed labor force by setting $\sigma_L = 0$ amplifies both the labor market frictions effect (captured by the first term on the RHS of eq. (281)) and the labor market accumulation effect (captured by the second term on the RHS of eq. (281)). Intuitively, technological change shifts the VC-schedule along a steeper DS-schedule, thus resulting in larger changes in the ratio θ^T/θ^N and in the relative wage ω. As discussed in section 5.2, across all scenarios, even if the labor market frictions effect raises the relative wage (when setting $\phi < 1$), the labor market accumulation effect predominates. Setting $\sigma_L = 0$ amplifies the negative impact of the labor accumulation effect on the relative wage by such an amount that the model cannot account for the size of decline in the relative wage found in the data.

K.7 Relative Wage and Relative Price Effects of Technological Change Biased Toward the Traded Sector when $\sigma_L \to \infty$

In this subsection, we investigate the relative price and relative wage effects of higher productivity of tradables relative to non tradables when we let σ_L tend toward infinity. In this configuration, the case of perfect mobility of labor emerges.

As mentioned in section I, the steady-state can be characterized graphically by considering alternatively the goods market or the labor market. When we let σ_L tend toward infinity, eq. (221) implies that Θ, which captures the elasticity of sectoral employment w.r.t. the marginal revenue of labor, tends toward infinity. Inspection of (217) and (222) indicates that when $\sigma_L \to \infty$, the slope of the GME-schedule (equal to $1/\phi$) is unaffected while the LME-schedule (whose slope is equal to $1/\Theta^N$) becomes a horizontal line. Applying l'Hôpital's rule, eq. (233) reduces to:

$$\begin{aligned}\lim_{\sigma_L \to \infty} \hat{p} &= \frac{1+\Theta^T}{1+\Theta^N}\hat{a}^T - \hat{a}^N, \\ &= \frac{\Xi^T \chi^T\left[\left(1-\alpha_V^N\right)\Psi^N + \chi^N W_R^N\right]}{\Xi^N \chi^N\left[\left(1-\alpha_V^T\right)\Psi^T + \chi^T W_R^T\right]}\hat{a}^T - \hat{a}^N. \end{aligned}\tag{282}$$

According to our quantitative analysis, while labor market parameters are allowed to vary across sectors, the term in front of $\hat{a}^T$ is close to one. As a result, a 1 percentage point increase in the productivity differential between tradables and non tradables appreciates the relative price of non tradables by 1% approximately. Assuming that $\Theta^j \simeq \Theta$ and applying l'Hôpital's rule, the rate of change of the relative price described by eq. (49) reduces to:

$$\lim_{\sigma_L \to \infty} \hat{p} = \hat{a}^T - \hat{a}^N. \tag{283}$$

Consequently, a model with labor market frictions reaches the same conclusion as the standard neoclassical model with a competitive labor market as long as the elasticity of labor supply at the extensive margin tends toward infinity.

Inspection of (228) and (232) indicates that when $\sigma_L \to \infty$, the DS-schedule (whose slope is equal to $\frac{1}{[\alpha_V u + \sigma_L \chi]}$) becomes a horizontal line while the VC-schedule (whose slope is equal to $-\frac{\Xi}{\phi[(1-\alpha_V)\Psi + \chi W_R]}$) is unaffected. Applying l'Hôpital's rule, eq. (240) reduces to:

$$\begin{aligned} \lim_{\sigma_L \to \infty} \hat{\omega} &= \left[\Omega^N \frac{1+\Theta^T}{1+\Theta^N} - \Omega^T\right] \hat{a}^T, \\ &= \left\{\Omega^N \frac{\Xi^T \chi^T \left[\left(1-\alpha_V^N\right)\Psi^N + \chi^N W_R^N\right]}{\Xi^N \chi^N \left[\left(1-\alpha_V^T\right)\Psi^T + \chi^T W_R^T\right]} - \Omega^T\right\} \hat{a}^T. \end{aligned} \tag{284}$$

Assuming that $\Theta^j \simeq \Theta$ and applying l'Hôpital's rule, the rate of change of the relative wage described by eq. (52) reduces to:

$$\lim_{\sigma_L \to \infty} \hat{\omega} = \left(\Omega^N - \Omega^T\right) \hat{a}^T, \tag{285}$$

where Ω^j captures the elasticity of the sectoral wage w.r.t the marginal revenue of labor; according to (285), the effect of productivity of tradables relative to non tradables on the relative wage is proportional to $\Omega^N - \Omega^T$. More precisely, when we let $\sigma_L \to \infty$, while the ratio of labor market tightness remains unaffected if $\Theta^j \simeq \Theta$, technological change biased toward the traded sector may influence the relative wage as long as the elasticity of sectoral wage w.r.t. the marginal revenue of labor Ω^j varies across sectors. For our benchmark parametrization, we have $\Omega^j \simeq \Omega$ so that the relative wage is (almost) unaffected by a productivity differential.

In conclusion, a model with labor market frictions reaches the same conclusions as the standard neoclassical model with a competitive labor market as long as the elasticity of labor supply at the extensive margin tends toward infinity.

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