Bureau d'économie théorique et appliquée (BETA) UMR 7522

# Documents de travail

### « The monetary model of hyperinflation and the adaptive expectations : limits of the association and model validity »

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Document de Travail nº 2007-09

Février 2007

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# The monetary model of hyperinflation and the adaptive expectations: limits of the association and model validity

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#### Abstract:

This article highlights the strict association met in the literature between the adaptive expectations assumption and the correct running of the monetary model of hyperinflation. A complete resolution of the model is carried out under the adaptive expectations hypothesis. It is shown that the assumption of adaptive expectations is not sufficient to ensure the validity of the model for the explanation of monetary hyperinflation. This result raises the question of the field of validity of this model already posed by the introduction of rational expectations. The possibility of development of self-generating hyperinflationary bubbles strengthens the relevance of this question.

Key words: hyperinflation, seigniorage, hyperinflationary bubbles

JEL classification: E31

#### **1** Introduction

Hyperinflation is an unstable dynamic process where inflation speeds up. The modelling of hyperinflation started with the seminal work of Cagan (1956) within the New Quantity Theory of Money. Cagan defined hyperinflation as a speeding up inflation process where inflation rates exceed 50% monthly. He considered hyperinflationary episodes as purely monetary phenomena that can be studied by focusing only on the money market. This approach implies that the model deals with monetary hyperinflation where both inflation and money growth rates accelerate and explode. Cagan proposed the explanation of monetary hyperinflation as the result of an excessive real fiscal deficit financed through money creation or seigniorage revenues. Nevertheless, this first modelling couldn't produce monetary hyperinflation paths. Later, Evans and Yarrow (1981) and Bruno and Fischer (1987) completed the model by modelling the money supply process. However, since the articles of Buiter (1987) and Kiguel (1989) it is known that in some of its configurations the model is unable to support the standard explanation of hyperinflation, especially under the assumption of rational expectations.

The possible failure of the monetary model of hyperinflation is an important issue. The model provides the theoretical framework for stabilization policies and for many empirical investigations on hyperinflationary experiences. Empirical investigations relying on the theoretical framework of the monetary model of hyperinflation have been being published on a regular basis. Recently, there were Slavova (2003) on the Bulgarian experience of 1996-

1997, Choudhry (1998) on the last Russian experience during the Nineties, Petrovic and Vujosevic (1996), Bogetic *et al* (1999) or Petrovic and Mladenovic (2000) on the Serbian experience during the decade 90, or Georgoutsos and Kouretas (2004) on the famous German experience in the early Twenties. Then, the possible failure of this model implies that empirical studies relying on the monetary model of hyperinflation should be very careful which configuration of this model they deal with. This issue is of great importance since the majority of empirical studies rely on a rational expectations version of the model.

The monetary model of hyperinflation has a relatively simple structure and a rich set of solutions. However, the wealth of possible solutions of this model isn't an asset for it. On the contrary, it results in restricting the field of validity of the model for the analysis of hyperinflation. The introduction of rational expectations into the model has often been at the origin of these validity problems as shown in Buiter (1987) or Kiguel (1989). Therefore, it comes out that the monetary model of hyperinflation is usually associated in the literature with the adaptive expectations assumption. This arises since the study of this configuration allows several authors like Bruno and Fischer (1987, 1990), for instance, to support the highlighting and the explanation of monetary hyperinflation. In the same spirit, Evans (1995) stressed that the assumption of adaptive expectations is a sufficient condition to ensure the validity of the model.

The present article aims at highlighting the strict association met in the literature between the assumption of adaptive expectations and the correct running of the monetary model of hyperinflation. With that aim, a complete resolution of the model is carried out under the assumption of adaptive expectations. This completes the analyses made in Bruno and Fischer (1987, 1990), taken up again in Blanchard and Fischer (1990) and still recently in Walsh (2003). The main purpose of the paper is to show that the validity of the model doesn't depend on the way in which inflationary expectations are formed. The crucial issue is the presence of a sufficiently large adjustment lag of real cash balances to actual inflation rates.

The analysis of the dynamics of the model carried out in the second section of the article leads to the distinction of two configurations under the adaptive expectations hypothesis. The first configuration, which is thoroughly analysed in the third section, corresponds to a relatively slow adjustment of inflationary expectations. The second configuration, not explored in the literature, corresponds to a relatively fast adjustment of inflationary expectations. The fourth section carries out the thorough treatment of it. The results obtained in the fourth section justify a deeper investigation of this case from the point of view of economic policy theory in fifth section. Section 6 concludes the article.

#### 2 The model

The demand for real cash balances is the fundamental equation of the model. During hyperinflations real variables such as the real rate of interest and real output may be reasonably treated as constant since all the action involves money and prices. Therefore, since the demand for real cash balances depends on the nominal interest rate, it will depend only on the expected rate of inflation. Following Cagan (1956), we use a semi-logarithmic demand for real cash balances, known as Cagan demand for money. Then, expressed in real terms  $M_r^d$ , the demand for real cash balances can be written in the following way:

$$M_{rt}^{d} = e^{\gamma - \alpha \pi_{t}^{e}} \quad . \tag{1}$$

In this equation  $\pi^e$  represents the expected rate of inflation,  $\alpha$  and  $\gamma$  are parameters. The role of constant  $\gamma$  is to describe the influence of real income and real interest rate, which are supposed to be constant in this analysis. The positive constant  $\alpha$ , the semi-elasticity of money demand, describes the decreasing demand for real cash balances with respect to expected rate of inflation. In order to make more apparent the semi-logarithmic shape of the Cagan demand for money, equation (1) can be re-written as:

$$\log(M_{r\,t}^{d}) = \gamma - \alpha \pi_{t}^{e}. \tag{1}$$

Expected inflation is assumed to adjust adaptively to actual inflation:

$$\dot{\pi}_t^e = \beta \cdot (\pi_t - \pi_t^e) , \beta > 0, \qquad (2)$$

where  $\pi$  is the actual rate of inflation. We follow Cagan in using continuous time so that a variable with an upper point represents its derivative with respect to time. The parameter  $\beta$ , called « expectation coefficient » by Cagan, captures the speed of adjustment of expectations to observed actual inflation. A low  $\beta$  implies that expectations respond slowly to inflation forecast errors. A high  $\beta$  implies that expectations respond quickly to inflation forecast errors. At the limit where  $\beta$  tends to an infinite value we retrieve the perfect foresight case, which is in this determinist model equivalent to rational expectations hypothesis.

Concerning the adjustment between real cash balances and desired real cash balances we assume, like Cagan, instant clearing of the money market. Therefore, we have always equality between the level of holdings of real cash balances, M/P, and the level of desired real cash balances (where *M* is the nominal stock of money and *P* the general price level). Formally, we can write:

$$\left(\frac{M}{P}\right)_{t} = (M_{r}^{d})_{t}.$$
(3)

The model description is completed by stating the process explaining the money supply. The real fiscal deficit d is fully financed through money creation. Therefore, the process of money creation is driven by the following government budget constraint:

$$d_t = \frac{M_t}{P_t} \qquad . \tag{4}$$

As money creation from public authorities implies a transfer of real resources from the private sector to the government, seigniorage revenues can be interpreted as the outcome of a particular tax, the inflation tax. As long as the money issued by the public authorities is desired and used by private agents, the latter won't escape this inflation tax.

The later four equations make the monetary model of hyperinflation. In order to simplify the notations we omit, from there on, to write the index of time *t* to all variables.

From equation (4), the government budget constraint can be restated as follows:

$$d = \frac{M}{P} = \frac{M}{M} \cdot \frac{M}{P} \quad . \tag{5}$$

Following equation (3) describing the instant clearing of money market and according to the semi-logarithmic form of the demand for real cash balances given by (1), the government budget constraint can be re-written as:

$$d = \theta \cdot e^{\gamma - \alpha \pi^{\epsilon}} \quad , \tag{6}$$

where  $\theta$  is the growth rate of the nominal stock of money. The constraint (6) can also be written in the following way after isolating the expected rate of inflation:

$$\pi^{e} = \frac{1}{\alpha} \left( \log \theta + \gamma - \log d \right) . \tag{7}$$

The latter expression of the government budget constraint represents the equation of a curve *IS* in the framework ( $\theta$ ,  $\pi^e$ ), named "iso-seigniorage curve". The curve *IS* derived from (7) shows, for each rate of money growth, the expected rate of inflation needed to generate the required seigniorage revenues given by *d*. The iso-seigniorage curve *IS* represents the path followed by the economy. According to the logarithmic shape of equation (7), the curve *IS* is an increasing curve with a decreasing slope. Curve *IS* intersects the horizontal axis at  $\theta = de^{-\gamma}$ .

Further understanding of the model requires the specification of the dynamics of the model. By differentiating equation (3) with respect to time we obtain:

$$\theta - \pi = -\alpha \dot{\pi}^e \quad . \tag{8}$$

Introducing the value of  $\pi$  extracted from (8) into equation (2) gives:

$$\dot{\pi}^{e} = \frac{\beta}{1 - \alpha \beta} \left( \theta - \pi^{e} \right) \quad . \tag{9}$$

This latter equation shows the dynamic properties of the economy in the framework ( $\theta$ ,  $\pi^e$ ). In a steady-state equilibrium where the stock of real cash balances is constant we have:

$$\pi^e = \theta = \pi \quad , \tag{10}$$

At this stage any further investigation of the dynamics of the model requires the distinction of two cases:

• Case  $1 - \alpha\beta > 0$  or  $\beta < \alpha^{-1}$ , corresponding to the case where expected inflation adjusts relatively slowly to actual inflation. This is the case usually presented and treated in the literature.

• Case  $1 - \alpha\beta < 0$  or  $\beta > \alpha^{-1}$ , corresponding, on the contrary of the previous case, to a case where expected inflation responds relatively quickly to inflation forecast errors. This

case has not been explored in the literature. The treatment of this configuration is the focus of this article.

#### **3** Adaptive expectations and hyperinflation

In this section we examine the traditional version of the model corresponding to a relatively slow adjustment of expected inflation to actual inflation. This is the configuration generally presented in the literature as in Walsh (2003). Focusing on the case  $0 < \beta < \alpha^{-1}$  shows that the model dynamics are described by:

$$\begin{aligned} \dot{\pi}^{e} > 0 \quad \text{if} \quad \theta > \pi^{e} \quad , \\ \dot{\pi}^{e} < 0 \quad \text{if} \quad \theta < \pi^{e} \quad . \end{aligned}$$

$$(11)$$

The intersection of the 45° line with the curve *IS* determines, in the framework ( $\theta$ ,  $\pi^e$ ), the steady-state equilibrium points of the economy. The existence of steady-state equilibria depends of the size of the real fiscal deficit *d*. To see this, one should carry out the following analysis. In the framework ( $\theta$ ,  $\pi^e$ ) the steady-state equilibrium of the economy occurs when  $\theta = \pi^e$ , that means, according to (7), when:

$$\theta = \frac{1}{\alpha} (\log \theta + \gamma - \log d) . \tag{12}$$

Therefore, determining the steady-state equilibrium requires solving equation (12). To solve equation (12), we build the following function  $\Delta(\theta)$ :

$$\Delta(\theta) = \frac{1}{\alpha} \left( \log \theta + \gamma - \log d \right) - \theta \quad , \tag{13}$$

with the aim to determine the number of solutions of  $\Delta(\theta) = 0$  representing the number of steady-state equilibria. Function  $\Delta(\theta)$  is defined on  $]0; +\infty[$  and its limits at boundaries are respectively  $-\infty$  and  $-\infty$ . Calculating the first derivative of  $\Delta(\theta)$ ,  $\Delta'(\theta)$ , gives:

$$\Delta'(\theta) = \frac{1 - \alpha \theta}{\alpha \theta} \qquad . \tag{14}$$

Then, the variations of  $\Delta(\theta)$  are given by:

$$\Delta'(\theta) \begin{cases} > \\ = 0 \quad \text{according to} \quad \theta \begin{cases} < \\ = \alpha^{-1} \\ > \end{cases} \qquad (15)$$

According to the behaviour of function  $\Delta(\theta)$ , it appears that the existence of solutions to  $\Delta(\theta) = 0$  will depend on the value of  $\Delta(\alpha^{-1})$  which is given by:

$$\Delta(\alpha^{-1}) = \frac{1}{\alpha} (\gamma - 1 - \log(\alpha d)) .$$
 (16)

If the value of  $\Delta(\alpha^{-1})$  is strictly positive, which is the case when  $d < \frac{e^{\gamma^{-1}}}{\alpha} = d^*$ , equation  $\Delta(\theta) = 0$  has two solutions meaning that there are two distinct steady-state equilibria. For a zero value of  $\Delta(\alpha^{-1})$ , that is for  $d=d^*$ , there is a single steady-state equilibrium. If the value of  $\Delta(\alpha^{-1})$  is strictly negative, that is when fiscal deficit exceeds  $d^*$ , there isn't any steady-state equilibrium for the economy.

These results come from the existence of a Laffer curve for the steady state seigniorage revenues. In the case of the Cagan demand for money, the curve representing seigniorage revenues is a bell-shaped curve. That's why it is called a "Laffer curve" for the seigniorage revenues. Therefore, there is a maximal level of real deficit,  $\overline{d}$ , consistent with a stationary inflation rate, on one hand, and the possibility for the government to finance the same real budget deficit with two different stationary inflation rates, one called "low" and the other "high", as long as the real budget deficit remains lower than  $\overline{d}$ , on the other hand. For the economy it means that there is the possibility of two different steady-state equilibria, one of "low inflation" and the other of "high inflation". There is duality of steady-state equilibrium as long as the budget deficit remains lower than  $\overline{d}$ .

Assessing  $\overline{d}$  can be done in the following way. Calling *R* the steady-state amount of seigniorage revenues, the value of  $\overline{d}$  is the maximal value of *R*. Using (6) and (10) this value is given by:

$$\overline{d} = \max_{\pi} \{ R(\pi) \} = R^* = \max_{\pi} \{ \pi \cdot e^{\gamma - \alpha \pi} \} = \frac{1}{\alpha} e^{\gamma - 1} , \qquad (17)$$

and is exactly the value  $d^*$  showed previously:  $\overline{d} = d^*$ . The value of the stationary inflation rate corresponding to this maximum of seigniorage revenues is then:



 $\pi^* = \arg\max_{\pi} \left\{ \pi e^{\gamma - \alpha \pi} \right\} = \frac{1}{\alpha} \quad . \tag{18}$ 

Figure 1: Laffer curve for the steady state seigniorage revenues

Figure 1 shows the "Laffer curve" for the stationary seigniorage revenues. The issue of duality of the steady-state equilibrium clearly appears and so does the issue of financing a real budget deficit higher than  $d^*$  like  $d_1$  for instance. As can be seen on figure 1, there isn't any possibility to finance such a higher deficit with a stationary inflation rate. Therefore, this leaves the place for a non stationary way.

The iso-seigniorage curves  $IS_0$  and  $IS_1$  represented in figure 2 correspond, respectively, to the budget deficits  $d_0$  and  $d_1$  such that:

$$d_0 < d^* < d_1$$
 . (19)

The intersection of the 45° line with the curve  $IS_o$  determines two steady-state equilibria, points A and B. The point B, the high inflation steady-state equilibrium, is unstable whereas A, the low inflation equilibrium, is locally stable. The public authorities are able to finance their real budget deficit  $d_o$  with two stationary inflation rates  $\pi_A$  and  $\pi_B$ . If the budget deficit is  $d_I$  there isn't any steady-state equilibrium because the seigniorage revenues that can be reached with a stationary inflation rate are below the government needs. Financing this budget deficit will put the economy on a non stationary path. Figure 2 illustrates this point by showing the path followed by the economy on the curve  $IS_I$  where inflation and money growth rates escalate and explode.



Figure 2: Monetary hyperinflation dynamics

Consider the case of an economy in steady-state equilibrium A on figure 2. At this equilibrium point the government succeeds to finance its real budget deficit  $d_o$  through

π<sup>e</sup>

seigniorage revenues with a constant inflation rate of  $\pi_A$ . At point A actual and expected inflation rates and nominal stock of money growth rate are all equal:

$$\pi_A = \theta_A \quad . \tag{20}$$

Suppose that the budget deficit is increased to the level of  $d_1$ . The government needs a higher level of seigniorage revenues. Since the demand for real money balances depends on expected inflation, and because the adjustment process does not allow the expected inflation rate to jump immediately, the higher deficit can be financed by an increase in the rate of money growth. In terms of figure 2, since the expected inflation rate remains at its level immediately after the increase of the deficit, the higher monetary growth makes the economy jump from point A to point C on the new iso-seigniorage curve  $IS_1$  associated with the higher deficit.

An accelerating money supply growth enables, at this first stage, the public authorities to generate the required amount of seigniorage revenues. Since the level of desired real cash balances has not changed yet, the sudden rise of the nominal stock of money implies, through the adjustment of real cash balances holdings to its desired level, an increase in actual inflation rate in the economy (this doesn't appear directly in figure 2 since the framework is  $(\theta, \pi^e)$ ).

In a second stage, as expected inflation adjusts gradually to higher actual inflation, demand for real cash balances starts to decline. This decline of real cash balances implies decreasing seigniorage revenues. Budget balance requires that the government replies with a new increase of money growth rate. The outcome is a new rise of inflation rate and the economy begins its evolution from point C on  $IS_1$  towards "north-east" direction as shown in figure 2.

The accelerating process of money growth and expected inflation rates begins without having an end. Following the rise of money growth rate and the resulting rise of inflation rate, the government succeeds in financing its higher budget deficit because expected inflation adjust to actual inflation with a certain lag. During that lag the level of real cash balances will be higher than that that should prevail if actual inflation would have been correctly expected. As expected inflation adjusts to actual inflation, real cash balances decrease, then reducing seigniorage revenues. Budget balance requires the government to proceed with an accelerating money growth. Seigniorage revenues can be restored but only during the lag needed for expected inflation to adjust to actual inflation. The smaller is coefficient  $\beta$  the longer will be this lag.

By starting this process of accelerating money growth and inflation rates leading to monetary hyperinflation, public authorities take advantage from the imperfection of expected inflation adjustment. By misleading private agents systematically on their inflation forecasts, the government benefits from a higher level of seigniorage that should prevail otherwise. Public authorities can then benefit from a higher level of seigniorage than the level  $d^*$  by triggering monetary hyperinflation.

Concerning the design of a stabilisation program, suppose that following a budgetary crisis the economy experiences monetary hyperinflation and that the decision of stabilisation happens when the economy has reached point C' in figure 2. The aim of the government is to make the economy return on its initial steady state equilibrium A. Therefore, real budget deficit should be reduced to level  $d_o$ .

If government succeeds to reduce its deficit from  $d_1$  to  $d_0$  the economy will jump from C' to C" on  $IS_o$ . The escalating process of inflation and money growth rates is immediately interrupted. Following the expected inflation rate reached at point C' and the associated level of real cash balances, the reduction of seigniorage needs from  $d_1$  to  $d_0$  allows the reduction of the money growth rate from  $\theta_{C'}$  to  $\theta_{C''}$ . This implies an equivalent reduction of actual inflation rate. As expected inflation adjusts gradually to this lower actual inflation, a second stage of decrease of money growth and inflation can begin.

As the reduction of expected inflation implies a rise in real cash balances, it allows the government to slowdown the growth of the nominal money stock. In terms of figure 2, this process is illustrated by the evolution of the economy from point C" to point A. The slowdown of monetary growth implies the immediate slowdown of inflation and the lagged slowdown of expected inflation. This process goes on till the economy has reached its previous steady-state equilibrium at A where money growth rate, actual and expected inflation rates are all equal and remain constant.

#### 4 Adaptive expectations and model failure

The case not explored in the literature corresponds to a relatively fast adjustment of expected inflation to actual inflation. The case  $\beta > \alpha^{-1}$  determines the following model dynamics:

$$\begin{aligned} \dot{\pi}^{e} > 0 \quad \text{if} \quad \theta < \pi^{e} \quad , \\ \dot{\pi}^{e} < 0 \quad \text{if} \quad \theta > \pi^{e} \quad . \end{aligned}$$

$$(21)$$

The framework is the same as previously but dynamics are opposite. The curves  $IS'_o$  and  $IS'_l$ , represented in figure 3, are iso-seigniorage curves associated, respectively, with government budget deficits  $d_o$  and  $d_l$  ( $d_o < d^* < d_l$ ).

The same kinds of steady-state equilibria can be shown as those on figure 2. However, their dynamic properties are reverse: B', the high inflation equilibrium is locally stable, whereas A', the low inflation equilibrium, is unstable. In the literature, these properties are known as the "high inflation trap" issue. Confronted with the possibility to finance the same budget deficit with two different inflation rates the "high inflation trap" refers to the fact that the high inflation equilibrium is stable.

Suppose that initially the economy is at point B' experiencing the high inflation trap. If the budget deficit is increased to level  $d_1$ , the government needs for seigniorage revenues exceed the maximum level of seigniorage at steady-state. Therefore, budget balance will be reached in a non stationary way.

The rise of budget deficit to  $d_1$  implies, in terms of figure 3, the jump of the economy from B' to D on  $IS'_1$ . Since expected inflation adjust adaptively,  $\pi^e$  remains, at a first stage, constant and the rise of money growth rate respond to the higher budget deficit.

From point D dynamic forces lead the economy to move down in the "south-west" direction on iso-seigniorage curve *IS*'<sub>1</sub>. Money growth and expected inflation rates start to decline in a

process of continuous decrease of inflation. Buiter (1987) described such a process with the term "hyperdeflation" when he observed it within a similar framework under rational expectations. The operating mechanism is the same in this case as that described by Buiter (1987). In the case of the high inflation trap, the higher need of seigniorage requires a decrease of the inflation rate: this represents the "counter-intuitive" comparative static properties of the high inflation steady state equilibrium. The operating mechanism relies on a higher than unity elasticity of demand for money with respect to money growth rate. The process of continuous reductions of money growth and inflation rates allows the government to benefit from higher than  $d^*$  seigniorage revenues relying on this high elasticity of demand for real cash balances with respect to expected inflation. "Hyperdeflation" is the outcome of this process.



Figure 3: model failure

Nevertheless, it should be stressed that interpreting the triggering and development of this "hyperdeflation" is difficult because of the link between the initial required increase in money growth rate and the following triggering of "hyperdeflation". It is quite easy to understand the initial rise of money growth rate, but it is very difficult to explain the fact that this increase should be followed by a decline of expected inflation rate. That's why Bruno and Fischer (1987, 1990) wrote, about the "counter-intuitive" comparative static properties of the high inflation equilibrium, the following words:

« There is no very good explanation for the initial fall in the inflation rate. Given that the economy is on the wrong side of the Laffer curve, a decline in the inflation rate is needed to generate more revenue when the deficit rises. »

In Blanchard and Fischer (1989) it is possible to find the same kind of trouble when the authors present the monetary model of hyperinflation. Using the work of Bruno and Fischer

(1987, 1990) the authors question the plausibility of adaptive expectations (Blanchard and Fischer (1989, note 39, page 209)). Since the rational expectations hypothesis leads to the same kind of result this remark isn't consistent.

Moreover, it isn't possible to use the explanation suggested by Evans and Yarrow (1981) under rational expectations which states that following the rise of real cash balances due to the initial acceleration of money growth, instant clearing on the money market requires a decline of expected inflation rate. Under adaptive expectations scheme no independent motion of expectations can't happen. Therefore, this "portfolio" approach is not working. Despite this difficulty to explain the start of this operating process, there is no place for any monetary hyperinflation in this case.

The impossibility of any monetary hyperinflation within this case of the model raises the question of the failure of the model in its ability to analyse hyperinflation. A better understanding of this problem requires looking at the reasons for the disappearance of hyperinflation.

We have shown that the triggering and development of hyperinflation are the means used by the government to take profit from the lag of expected inflation to actual inflation. The escalation of money growth and inflation rates allow to systematically mislead the agents on the actual values of inflation rates implying a continuous over-evaluation of the real cash balances level. The public authorities take benefit from the lag of adjustment of real cash balances to their level which should prevail if inflation would be correctly perceived.

The case being analysed here  $(\alpha\beta > 1)$  corresponds to a relatively fast adjustment of expected inflation to actual inflation. The corresponding lag during that the government is able to mislead the agents on the actual inflation rates is relatively short and in any case not sufficient to be exploited. That's why there is no place for monetary hyperinflation in this configuration.

This configuration ( $\alpha\beta > 1$ ) presents the same dynamic properties as that studied by Buiter (1987) under rational expectations. It should be noticed that the rational expectations hypothesis is equivalent to the perfect foresight hypothesis in a determinist environment. Under the latter hypothesis there isn't any lag of real cash balances. Moreover, it is easy to verify that the case of perfect foresight is mathematically equivalent to the case of adaptive expectations with an infinite expectation coefficient. Re-writing equation (2) in the following way:

$$\frac{1}{\beta}\dot{\pi}^e = \pi - \pi^e \quad , \quad \beta > 0 \quad , \tag{22}$$

and considering an infinite value for the expectation coefficient  $\beta$ , equation (22) becomes:

$$0 = \pi - \pi^e \quad , \tag{23}$$

which is exactly the expression of perfect foresight:

$$\pi = \pi^e \quad . \tag{24}$$

Since the coefficient  $\beta$  measures the speed of adjustment of expected inflation to actual inflation, the perfect foresight hypothesis is, from a mathematical point of view, equivalent to the hypothesis of adaptive expectations without lag.

The analysis carried out in this section shows that the way of forecasting inflation, either adaptive or rational, is not the main factor responsible for the failure or the validity of the monetary model of hyperinflation. We clearly showed that assuming adaptive expectations is not sufficient to obtain hyperinflation in this model. This result is important not only for the understanding of the model, but also to dissipate the misunderstanding present in the literature. Evans (1995, page 47) writes, about the failure of the monetary model of hyperinflation, the following words:

< [...] replacing rational expectations with the assumption of adaptive expectations is sufficient to obtain the desired property in the model [...] >

The current section has clearly shown that it is absolutely not the case. Beyond the specification of the adaptive expectations rule, the main factor for obtaining hyperinflation in this model is the lag of real cash balances caused by the latter. Then, when Blanchard and Fischer (1989, page 201) state that « *quite crucial to the results is the way in which expectations are formed* » we understand now that this statement should be much more precise. The way in which expectations are formed is important to obtain monetary hyperinflation in the model, but only because of the sufficient lag for real cash balances it may cause.

#### 5 Model failure and public budget balance

The configuration  $\alpha\beta > 1$  can't highlight nor explain any monetary hyperinflation as it was the case in the configuration  $\alpha\beta < 1$ . The monetary model of hyperinflation is simple but rich in solutions. We continue the analysis of the configuration  $\alpha\beta > 1$  by considering the issue of stabilisation policy. The aim is to assess whether the model failure highlighted in that configuration has any consequences in the field of stabilisation policy theory affecting possibly the effectiveness of stabilisation policy.

We take the case previously studied where the economy is on curve  $IS'_1$  following the rise of real budget deficit to an excessive level (see figure 4). On this curve the economy is experiencing a process of continuous decline of inflation rates. We called this process "hyperdeflation" following Buiter (1987). The question is whether the public authorities may be able to put back the economy on a convergent path.

Assume that the decision to stabilise the economy takes place at the precise moment when economy reaches point D' in figure 4. The rise of budget deficit from  $d_0$  to  $d_1$  being the cause of the evolution of the economy on the path  $IS'_1$ , public authorities may consider to reduce the deficit to its previous level  $d_0$ . Such a measure of public deficit reduction allows the economy to return on path  $IS'_0$  by jumping from point D' to point E. At point E the economy is on a convergent path leading progressively to the high inflation steady-state equilibrium B'.

Stabilisation policy doesn't loose its effectiveness to put the economy on a path converging to the steady-state equilibrium. However, this result is quite different if one considers a zero budget deficit policy. Assume that rather than reducing the deficit from  $d_1$  to  $d_0$  public

authorities decide to reduce the budget deficit to zero. From the expression of the government budget constraint given by equation (6), it follows that a zero deficit implies:

$$\theta = 0 \tag{25}$$

In the framework  $(\theta, \pi^e)$ , this budget constraint is represented by the vertical axis. The dynamics of the configuration  $\alpha\beta > 1$  remain determined by (21).



Figure 4: budget balance and hyperinflationary bubbles

Consider that when reaching point D' in curve  $IS'_{1}$  on figure 4 the government implements a stabilisation policy to reduce the deficit to zero. Such a policy implies the jump of the economy from point D' to point F. From (21) the dynamic forces operating on the positive part of the vertical axis, and at point F in particular, are given by:

$$\dot{\pi}^e > 0 \qquad . \tag{26}$$

The consequence of this drastic policy is the triggering of a process of accelerating inflation. The triggering and development of this process happens with a constant nominal stock of money according to (25). The path followed by the economy is a hyperinflationary bubble. The circumstances around the triggering of the explosive bubble after a period of decreasing inflation are unclear.

Registering the shift of inflation evolution, the inflation rates expectations adjust adaptively but quite quickly to the new trend of accelerating inflation. Assuming a coefficient  $\alpha$  quite large (consistent with  $\alpha\beta > 1$ ), meaning that the demand for real cash balances is very elastic, the increase of expected inflation rates implies a huge reduction of desired real cash balances.

As the nominal stock of money is unchanged, this leads to a large excess of real cash balances holdings compared to the desired level, implying a big increase in the general price level. This leads to a higher rate of inflation. The process goes on and keeps accelerating according to the same scheme. The process of general price level increase is amplified from one stage to another by joint action of expected inflation rates adjusting quickly to actual inflation rates and high elasticity of the demand for money.

The evolution of the economy along a path of hyperinflationary bubble raises the question of the design of a possible stabilisation program according to the facts that public budget is balanced and the nominal stock of money is constant. The proposal made within this configuration seems as counter-intuitive as is the triggering of the price level bubble. If the economy is moving, from point F in figure 4, on the hyperinflationary bubble path, any policy aiming at restoring the real deficit  $d_0$  will put back the economy on a path converging to the high inflation steady-state equilibrium. By using paradoxical measures the government will succeed to stop the development of a paradoxical process in a model designed to explain monetary hyperinflation.

It is necessary to stress that the kind of hyperinflationary bubbles highlighted in this configuration isn't any rational bubbles since they have been produced under the adaptive expectations hypothesis. The kind of explosive bubbles produced in this configuration is the same one as that Cagan (1956) noticed the possibility for in its seminal article. Nevertheless, it should be reminded that the work initially developed by Cagan didn't model the endogenous money supply. Cagan considered the possibility of such explosive bubbles paths as the illustration of the capacity of his model to highlight accelerating inflation processes. However, these paths didn't correspond to the economic explanation brought by Cagan because the latter considered monetary hyperinflation. Some other authors like Goldman (1972) also showed the theoretical possibility of hyperinflationary bubbles by working on the original model of Cagan.

#### 6 Conclusion

This article explores the strict association met in the literature between the monetary model of hyperinflation and the hypothesis of adaptive expectations. This association has its origin in the problems of the capacity of the model to explain monetary hyperinflation under rational expectations. These problems of the validity of the model, highlighted by the articles of Buiter (1987) and Kiguel (1989), caused some misunderstandings among economists as it appears through the article of Cagan (1987) for the dictionary Palgrave. That led some authors like Evans (1995) to consider the adaptive expectations hypothesis as sufficient to ensure the validity of the model.

The analysis of the dynamic properties of the model under adaptive expectations requires the distinction of two different configurations. The first configuration corresponds to a relatively slow adjustment of expected inflation to actual inflation. This configuration usually treated in the literature fully ensures the highlighting and the explanation of monetary hyperinflation. Monetary hyperinflation is the result of an excessive public deficit financed through money creation. The main underlying operating mechanism relies on the lag of real cash balances to actual inflation. This lag is caused by the relatively slow adjustment of inflationary expectations to the actual inflation characteristic for this configuration.

The second configuration of the model corresponds to a relatively fast adjustment of expected inflation to actual inflation. This configuration hasn't been explored in the literature. Bruno and Fischer (1987, 1990) approached this configuration only from the point of view of the stability properties of the steady-state equilibria and the high inflation trap issue. They didn't consider the consequences of an increase of the public deficit beyond the steady-state conditions. The thorough analysis of this configuration shows that the hypothesis of adaptive expectations is not sufficient to ensure the validity of the model for the explanation of monetary hyperinflation. This configuration doesn't produce any monetary hyperinflation when the public deficit exceeds the maximal value of seigniorage revenues reachable in stationary situation. A process of continuous decline of the inflation rate takes place. This is exactly the same kind of paradox as that of "hyperdeflation" described by Buiter (1987). Therefore, the way in which expectations are formed is important to obtain monetary hyperinflation in the model, but only because of the sufficient lag for real cash balances it may cause. If this lag is not sufficient the model can't produce monetary hyperinflation.

Within this second configuration the model is valid for neither highlighting nor explaining monetary hyperinflation. The failure of the model in its ability to explain monetary hyperinflation brings the problem on the field of economic policy theory. Public deficit reductions remain efficient to put back the economy on a convergent path when a reduction of public deficit to its steady-state level is considered. However, considering a drastic policy of zero public deficit shows that this configuration produces hyperinflationary bubbles paths.

The possibility of accelerating inflation processes while the nominal stock of money remains constant raises a second aspect of the dysfunction of this configuration of the model. The model has been designed to explain monetary hyperinflation processes and not hyperinflationary bubbles. The hyperinflationary bubble process is self-generating and may be explained by the joint action of expected inflation rates quickly adjusting to actual inflation rates and the high elasticity of the demand for money accelerating the inflation.

The evolution of the economy along a hyperinflationary bubble path raises the question of the design of a stabilisation program when public budget is balanced and the nominal stock of money is constant. The stabilisation policy proposal made within this configuration seems as counter-intuitive as is the triggering of the price level bubble. It has been shown that restoring the public deficit to its initial level put back the economy on a convergent path. Therefore, that means that by using paradoxical measures the government will succeed to stop the development of a paradoxical process in a model designed to explain monetary hyperinflation.

Hyperinflationary bubbles paths should be taken very seriously since microeconomic foundations of the demand for money stress the consistency of such phenomena. Obstfeld and Rogoff (1983, 1986), for instance, showed that hyperinflationary bubbles paths are consistent with the individual optimizing behaviour and should not then be ruled out.

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